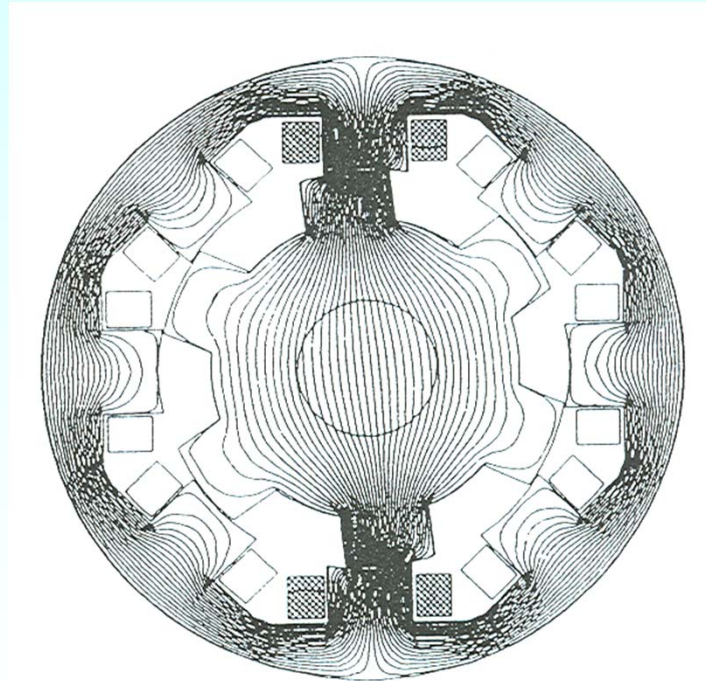


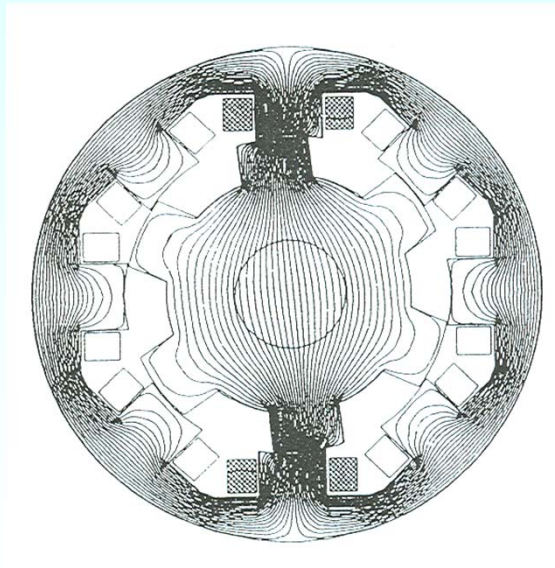
## 2. Reluctance machines



Source: Omekanda, A,  
ICEM, 1992

## 2. Reluctance machines

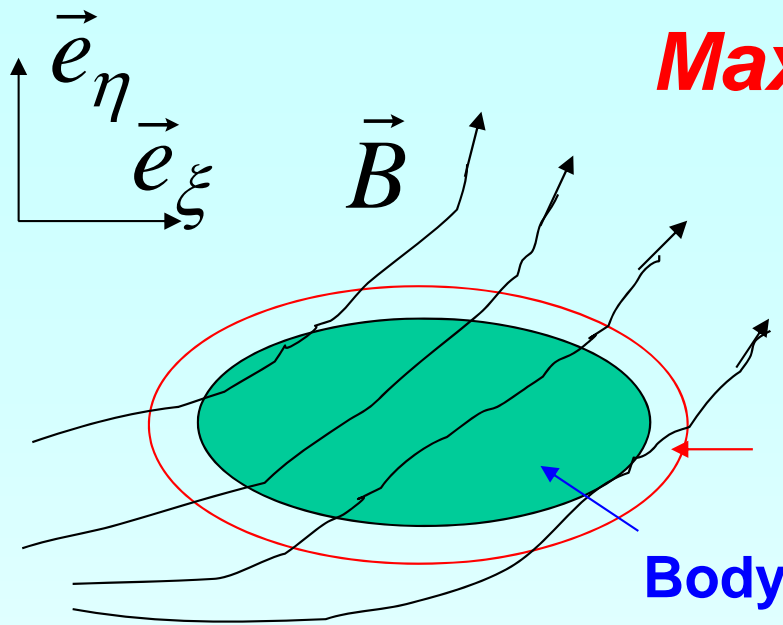
### 2.1 Switched reluctance drive



Source: Omekanda, A,  
ICEM, 1992



# Maxwell stress tensor



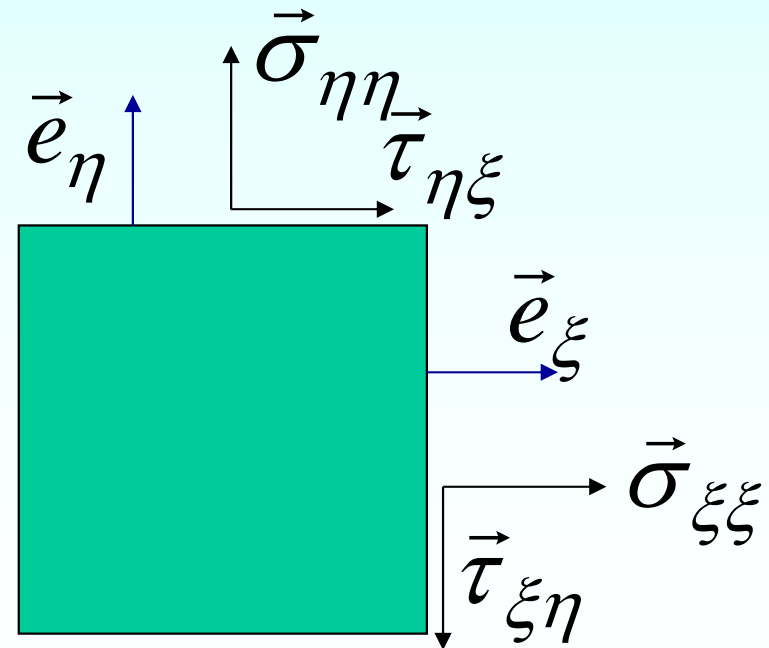
- Total magnetic force on a (magnetized) body is calculated by integrating the 9 components of *Maxwell's* stress tensor via surface *A*, which encloses the body outside in free space ( $\mu_0$ )

**Closed surface A**

**Body**

- *Maxwell's* stress tensor in 2 dimensions  $\xi, \eta$

$$\vec{T} = \begin{pmatrix} \sigma_{\xi\xi} & \tau_{\xi\eta} \\ \tau_{\eta\xi} & \sigma_{\eta\eta} \end{pmatrix} = \begin{pmatrix} \frac{B_\xi^2 - B_\eta^2}{2\mu_0} & \frac{B_\xi B_\eta}{\mu_0} \\ \frac{B_\eta B_\xi}{\mu_0} & \frac{B_\eta^2 - B_\xi^2}{2\mu_0} \end{pmatrix}$$



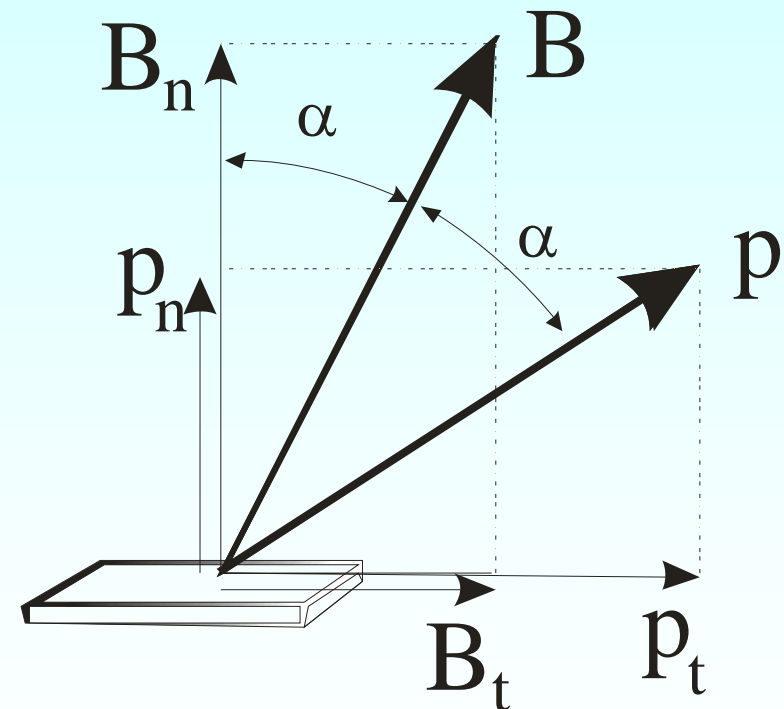
# Maxwell stress for force calculation

$$\left. \begin{aligned} \sigma &= \frac{B_n^2 - B_t^2}{2\mu_0} = p_n \\ \tau &= \frac{B_n B_t}{\mu_0} = p_t \end{aligned} \right\} \vec{p} = \vec{p}_n + \vec{p}_t$$

$$\tan \alpha = \frac{B_t}{B_n}$$

$$\frac{p_t}{p_n} = \tan 2\alpha = \frac{2}{\frac{1}{\tan \alpha} - \tan \alpha} = \frac{2B_n B_t}{B_n^2 - B_t^2}$$

$$\vec{F} = \oint_A \vec{p} \cdot d\vec{A}$$



Source: Reichert, K., VDE-Kurs El. Maschinen, 2009



# Maxwell stress does not allow calculating local forces

$$\vec{F} = \oint_A \vec{p} \cdot d\vec{A}$$

- Force integration must cover complete body.
- Local value  $p \cdot A$  has usually no physical meaning.
- In periodic structures the force per period can be determined.

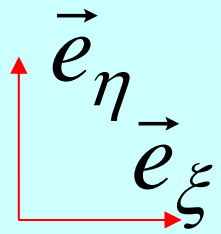
- Usually the magnetic force density is distributed within the ferromagnetic body according to the field and the permeability distribution. **It does NOT correspond** to the (equivalent) local surface forces, calculated from the MAXWELL stress.

- Only in ferromagnetic parts **with constant permeability** the magnetic force density **is localized in the body surface**, but is usually not equal with the MAXWELL stress components.

- Only in case of **infinite iron permeability** the magnetic force density, localized in the iron surface, **is identical with the MAXWELL stress components**.

$$\mu_{Fe} \rightarrow \infty : d\vec{F}(x, y) / dA = \vec{p}(x, y)$$

## Example: LORENTZ force



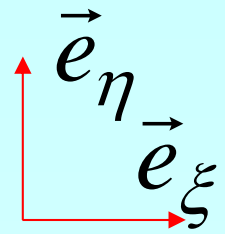
- LORENTZ force per current  $I$ :  $\vec{F}_c = I \cdot B_0 \cdot l_{Fe} \cdot \vec{e}_\xi$
- $N_s$  conductors under pole width  $b$ , total force:  
$$\vec{F} = 2N_s \vec{F}_c \Rightarrow F = 2N_s I \cdot B_0 \cdot l_{Fe}$$

- Current loading:  $\alpha = N_s I / b$

Current loading  $\alpha$

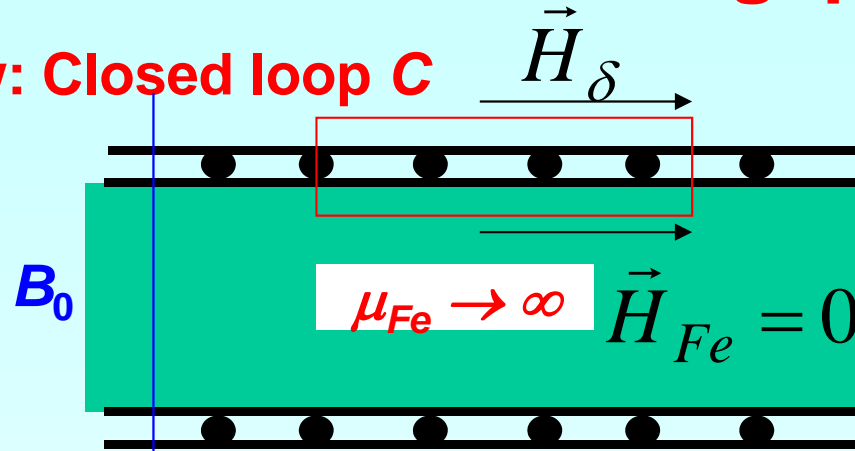
Force  $F$

$$F = 2 \cdot \alpha \cdot B_0 \cdot (b \cdot l_{Fe})$$



# Magnetic field in the air gap

Ampere's law: Closed loop C



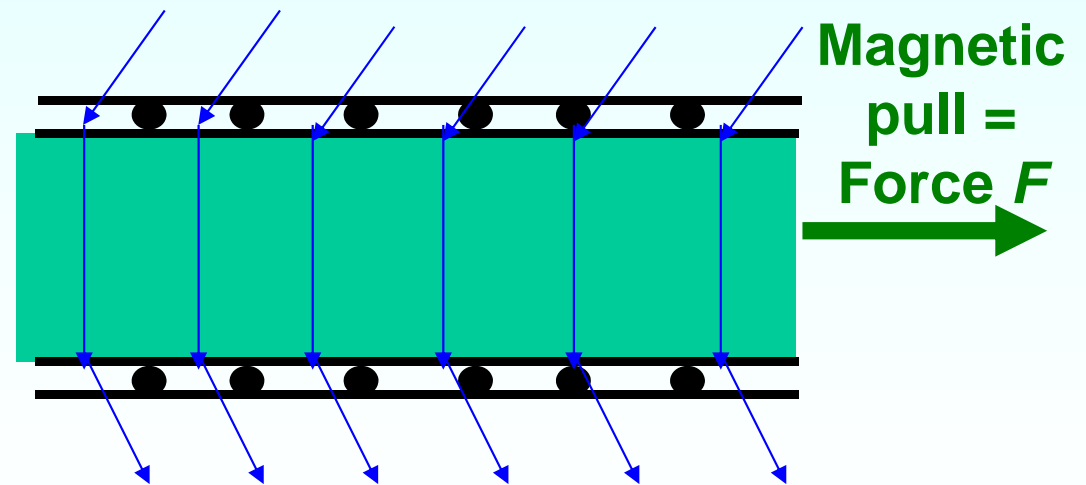
$$\Theta = \int_0^X \alpha(\xi) \cdot d\xi = \oint_C \vec{H} \cdot d\vec{s} = \int_0^X (H_{Fe} - H_\delta) d\xi = - \int_0^X H_\delta d\xi \Rightarrow H_\delta(\xi) = -\alpha(\xi)$$

$$\vec{B}_\xi = \mu_0 H_\delta(\xi) \cdot \vec{e}_\xi = -\mu_0 \alpha(\xi) \cdot \vec{e}_\xi$$

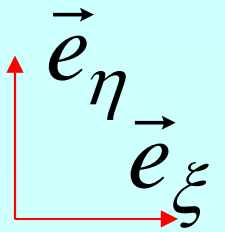
$$\vec{B}_\eta = -B_0 \cdot \vec{e}_\eta$$

$$\vec{B} = \vec{B}_\xi + \vec{B}_\eta$$

Resulting flux density  $B$



# Magnetic pull via *Maxwell stress*



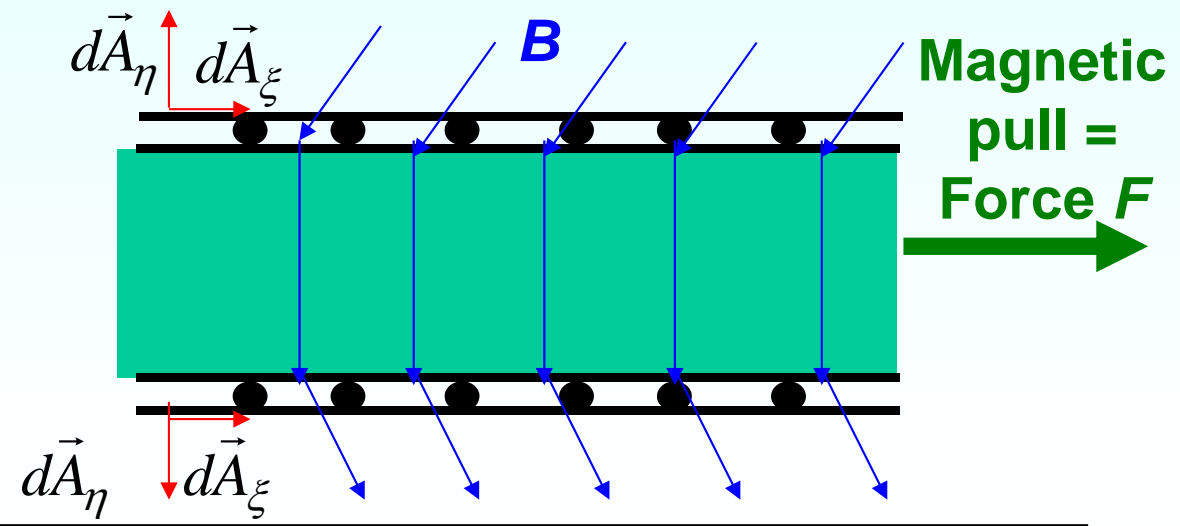
- Vertical stress component:  $\sigma_{\eta\eta} = \frac{B_\eta^2 - B_\xi^2}{2\mu_0}$

$$\vec{F}_\eta = \oint_A \vec{T} \cdot d\vec{A}_\eta = \int_{A_{upper}} \frac{B_\eta^2 - B_\xi^2}{2\mu_0} \cdot d\xi \cdot l_{Fe} - \int_{A_{lower}} \frac{B_\eta^2 - B_\xi^2}{2\mu_0} \cdot d\xi \cdot l_{Fe} = 0$$

- Horizontal stress component:  $\tau_{\eta\xi} = \frac{B_\eta B_\xi}{2\mu_0} = \frac{(-B_0) \cdot (-\mu_0 \alpha)}{\mu_0} = B_0 \cdot \alpha$

$$\vec{F}_\xi = \oint_A \vec{T} \cdot d\vec{A}_\xi = \int_{A_{upper}} \frac{B_\eta B_\xi}{2\mu_0} \cdot d\xi \cdot l_{Fe} + \int_{A_{lower}} \frac{B_\eta B_\xi}{2\mu_0} \cdot d\xi \cdot l_{Fe} = \vec{F}$$

$$\vec{F} = 2 \cdot (B_0 \cdot \alpha) \cdot b \cdot l_{Fe} \cdot \vec{e}_\xi$$



# Example: Reluctance force

- Inside iron:  $H_{Fe} = 0$ , no current layer = flux lines end perpendicular on iron surface = tangential flux density component ZERO:  $\tau_{\eta\xi} = \tau_{\xi\eta} = 0$

- Vertical stress component:  $\sigma_{\eta\eta} = \frac{B_{\eta}^2 - B_{\xi}^2}{2\mu_0} = \frac{B_{\eta}^2}{2\mu_0}$

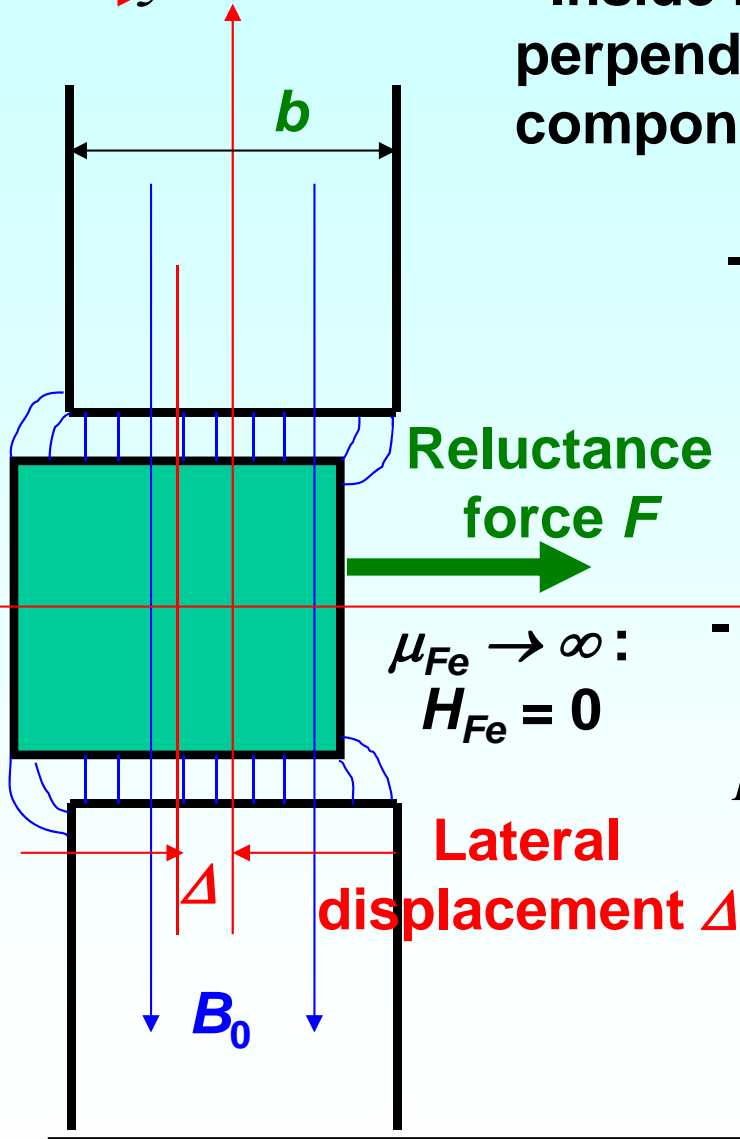
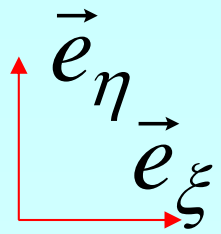
$$\vec{F}_{\eta} = \oint_A \vec{T} \cdot d\vec{A}_{\eta} = \left( \int_{A_{upper}} B_{\eta}^2 \cdot d\xi - \int_{A_{lower}} B_{\eta}^2 \cdot d\xi \right) \cdot \frac{l_{Fe}}{2\mu_0} = 0$$

- Horizontal stress component:  $\sigma_{\xi\xi} = \frac{B_{\xi}^2 - B_{\eta}^2}{2\mu_0} = \frac{B_{\xi}^2}{2\mu_0}$

$$\vec{F}_{\xi} = \oint_A \vec{T} \cdot d\vec{A}_{\xi} = \left( \int_{A_{left}} B_{\xi}^2 \cdot d\eta + \int_{A_{right}} B_{\xi}^2 \cdot d\eta \right) \cdot \frac{l_{Fe}}{2\mu_0} = \vec{F}$$

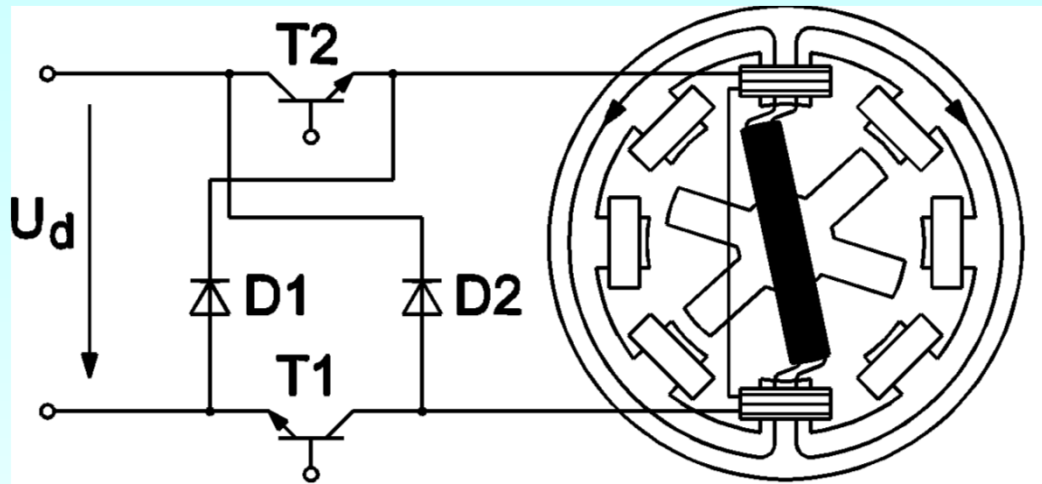
Reluctance force  $F$

$$\vec{F} = \int_{A_{right}} B_{\xi}^2 \cdot d\eta \cdot l_{Fe} / (2\mu_0)$$



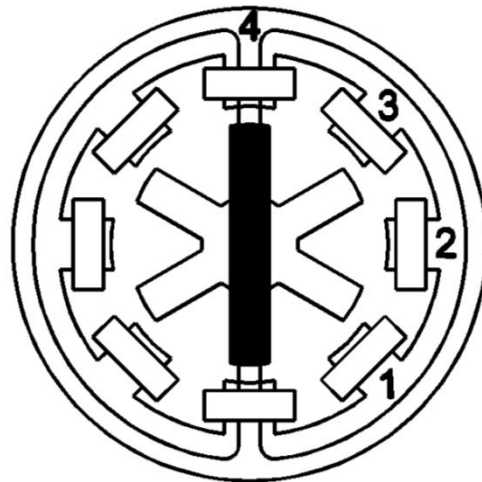
# Basic function of switched reluctance machine

Two pole, four phase switched reluctance machine (cross section):



T1, T2: Transistors  
D1, D2: free-wheeling diodes

One leg of a H-bridge inverter = each phase is operated  
**INDEPENDENTLY !**



Source: Hopper, E,  
*Elektrotechnik*, 1992

a)  
Phase "4" is energized by H-bridge inverter, fed from DC link  $U_d$

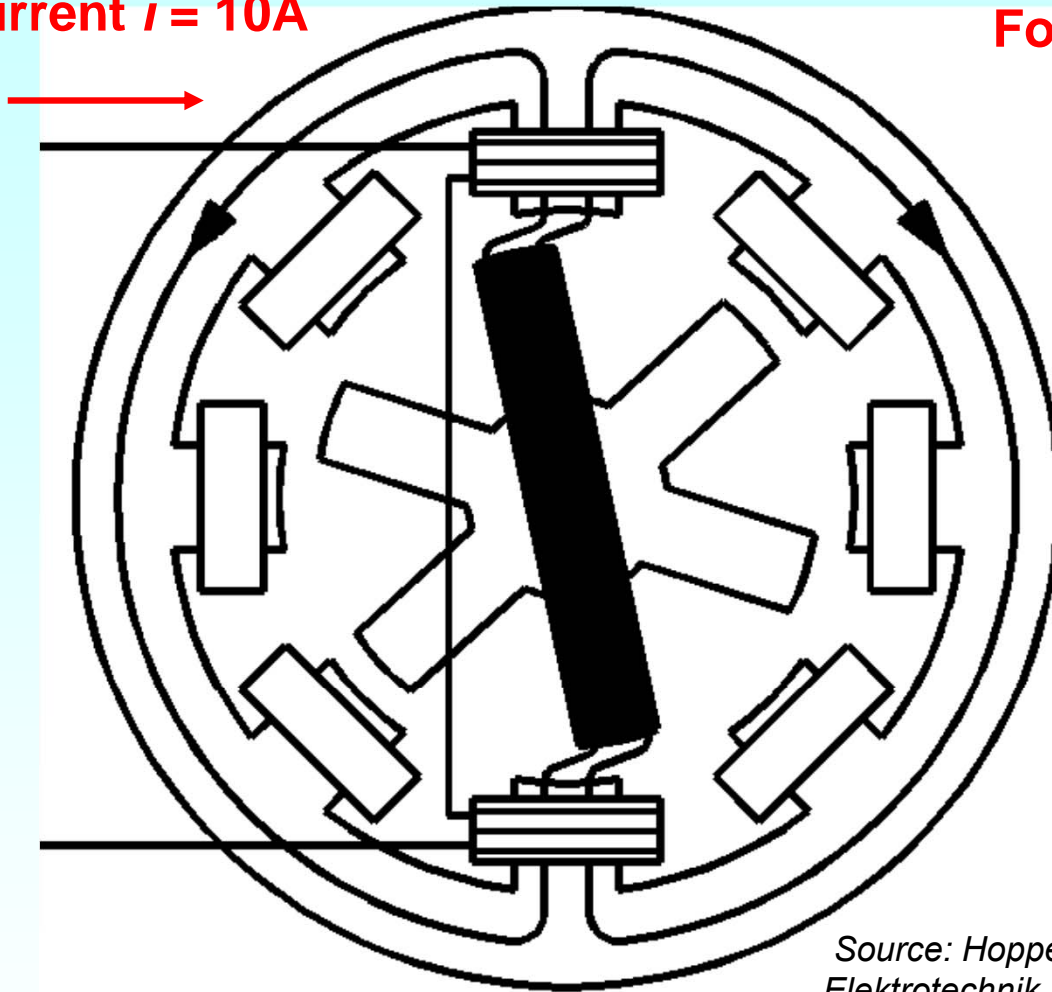
b)  
Tangential magnetic pull of flux lines drags next rotor teeth into aligned position with energized stator teeth, thus creating a torque

c)  
Next phase to be energized is no.1 to keep direction of rotation !

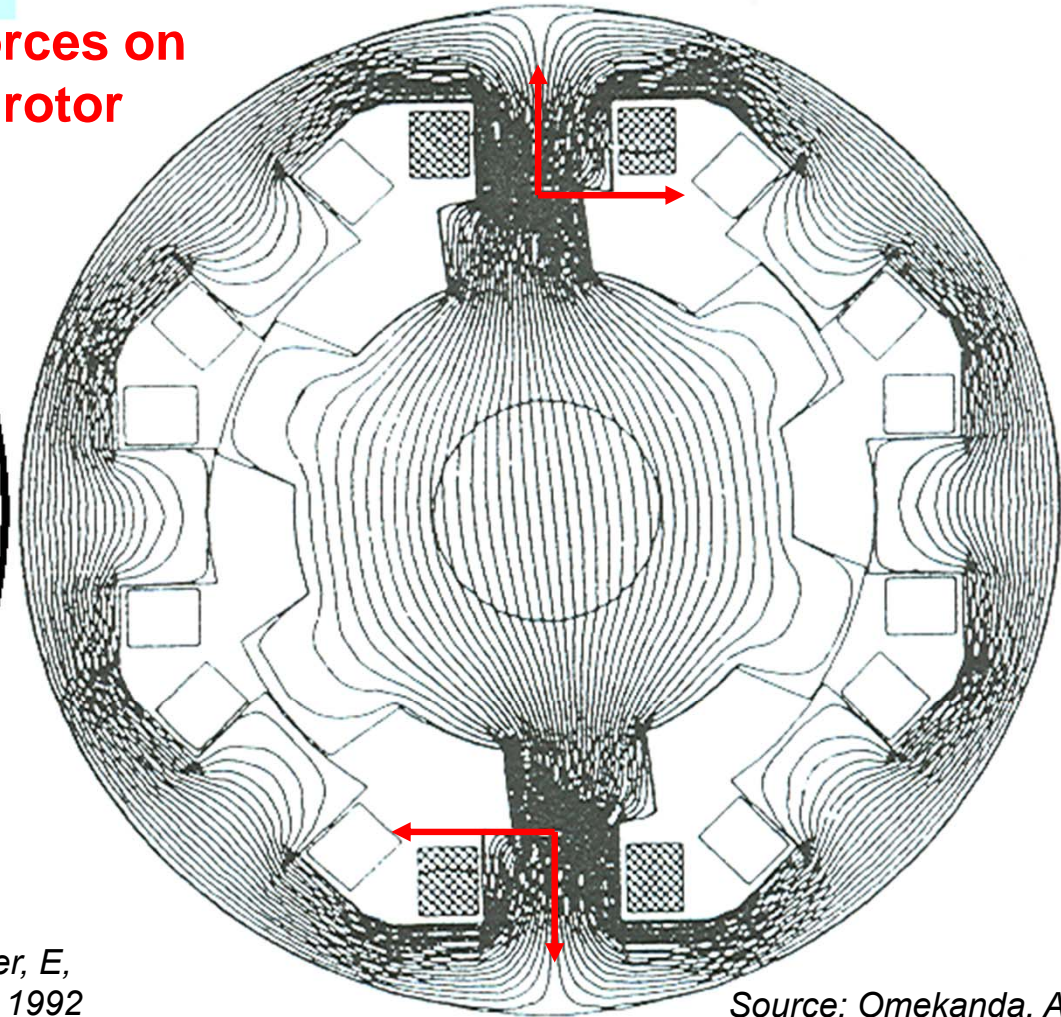


# Torque production in switched reluctance machine

Current  $i = 10\text{A}$



Forces on rotor



Source: Hopper, E,  
Elektrotechnik, 1992

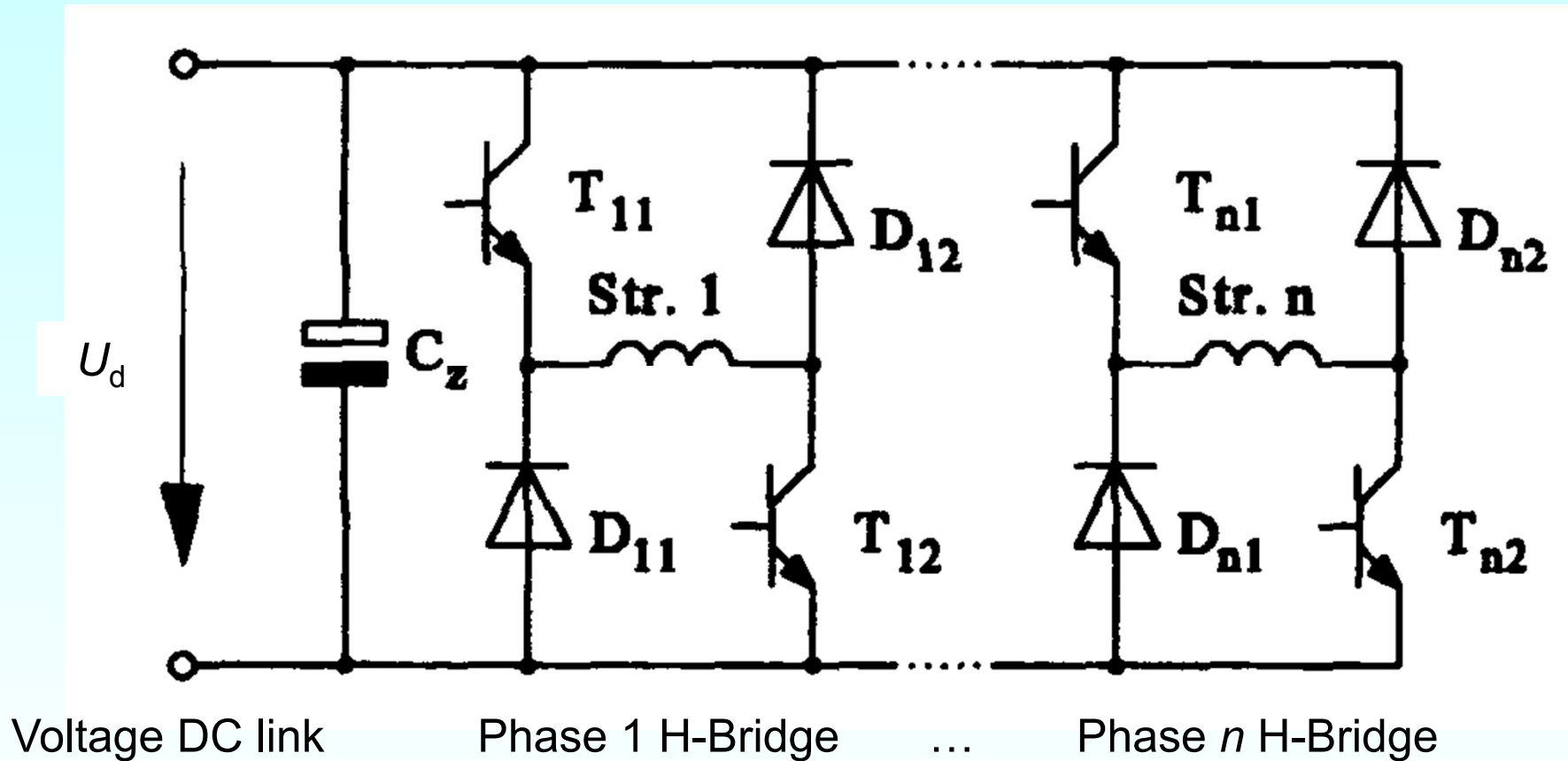
Source: Omekanda, A,  
ICEM, 1992

Numerical field calculation: Flux lines with energized phase "1"

**Data:** Outer stator diameter: 320 mm, air gap: 1 mm, iron stack length: 320 mm, shaft diameter: 70 mm, coil turns per tooth: 10, current per turn: 100 A DC



# H-Bridge inverter



Source: Schencke, T.: Drehmomentglättung von geschalteten Reluktanzmotoren durch eine angepasste Blechschnittgestaltung, Ilmenau, Technische Universität, Dissertation, 1997

# SR machine motor operation

- Torque is generated by **magnetic pull**, which is  $\sim B^2$ . **Unipolar** current (= block shaped current of one polarity) sufficient.
- **Reluctance structure**: The flux lines try to pass through the iron teeth with their high permeability and avoid the slot region.
- **Stepper motor principle**: Rotor moves stepwise without position sensor = cheap drive.
- **"Switched" reluctance motor principle**: With position sensor the rotor movement is completely controllable. No pull-out at overload is possible, as long as the inverter is able to impress current. Speed can be measured by using the rotor position sensor as speed sensor (**speed control**).

**Direction of rotation**: phases "1", "2", "3", "4", "1", ... **clockwise**  
"4", "3", "2", "1", "4", ... **counter-clockwise**

# SR generator operation

## Motor mode:

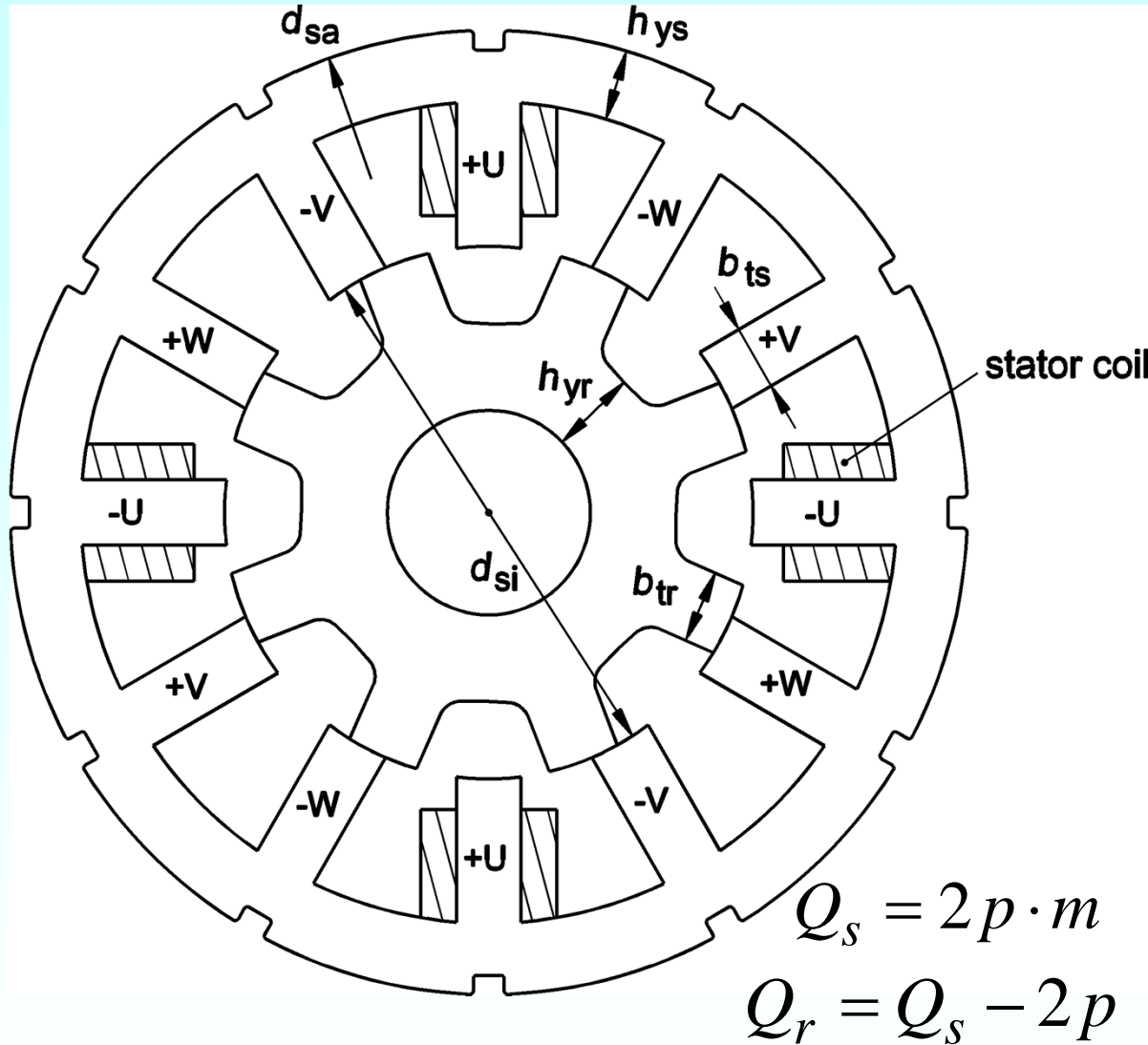
- By switching one phase after the other, the rotor keeps turning = **"switched" reluctance motors**.
- As rotor movement causes flux change in the stator coils, there a **voltage is induced** (back EMF).

## Generator mode:

- If the rotor is driven mechanically and the stator coils are energized when rotor moves from aligned to unaligned position, then the magnetic pull is **braking** the rotor.
- **Back EMF gives** - along with the stator current - generated electric power, which is fed to the inverter.



# Design features of SR machines



Cross section of a totally enclosed, air cooled 4-pole SR machine:  
 7.5 kW, 1500/min,  
 motor current (rms): 12 A,  
 stator outer/inner diameter:  
 210 / 120.9 mm, air gap: 0.45 mm

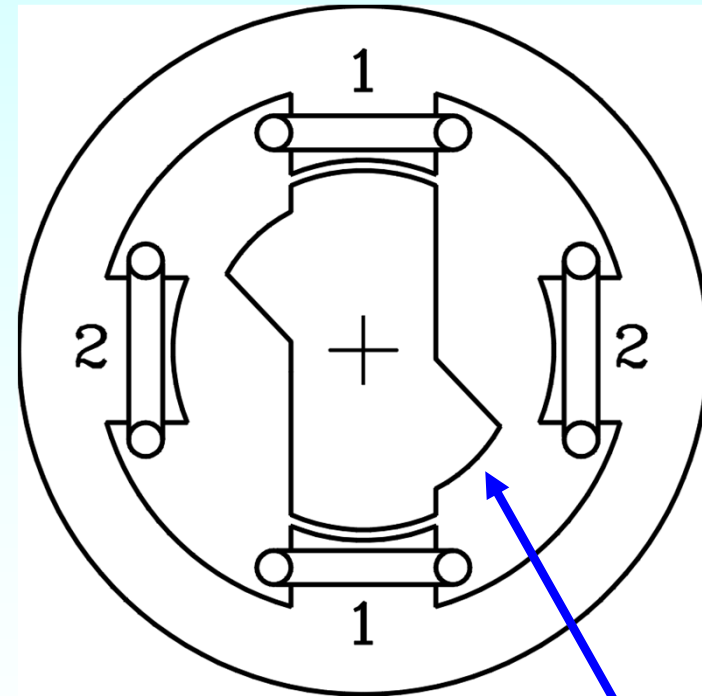
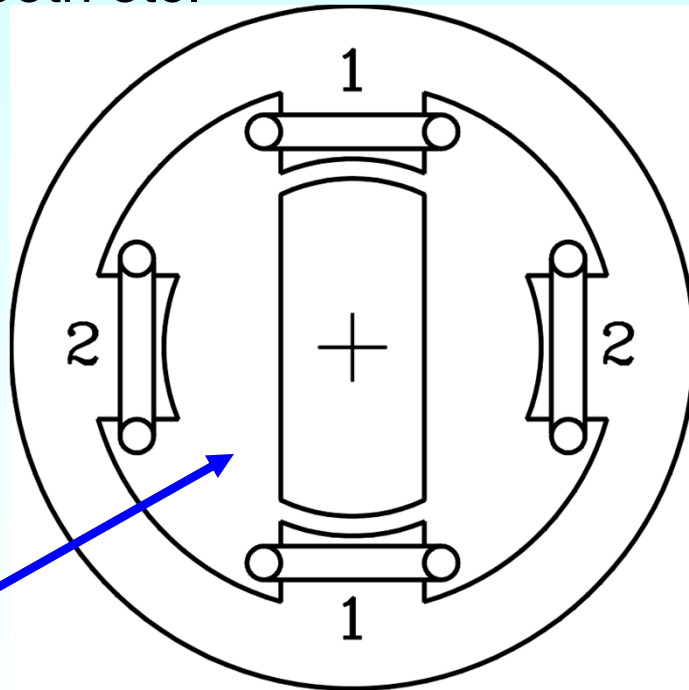
- Very small air gap for big difference of inductance of  $d$ - and  $q$ -axis
- Number of stator and rotor teeth NOT equal
- Usually number of rotor slots smaller
- Stator tooth width slightly smaller than rotor tooth width

**3 phases: 6/4 teeth per pole pair    4 phases: 8/6 teeth per pole pair**

# One - & Two-phase SR motors are not self starting

Stator and rotor teeth numbers, two phase machine: per pole pair ( $2p = 2$ ):  
 $m = 2$ :  $Q_s = 2p \cdot m = 2 \cdot 2 = 4$      $Q_r = Q_s - 2p = 4 - 2 = 2$

Self starting is only assured, if some special asymmetry is put into the machine e.g. **asymmetric rotor teeth**, additional permanent magnet in on stator tooth etc.

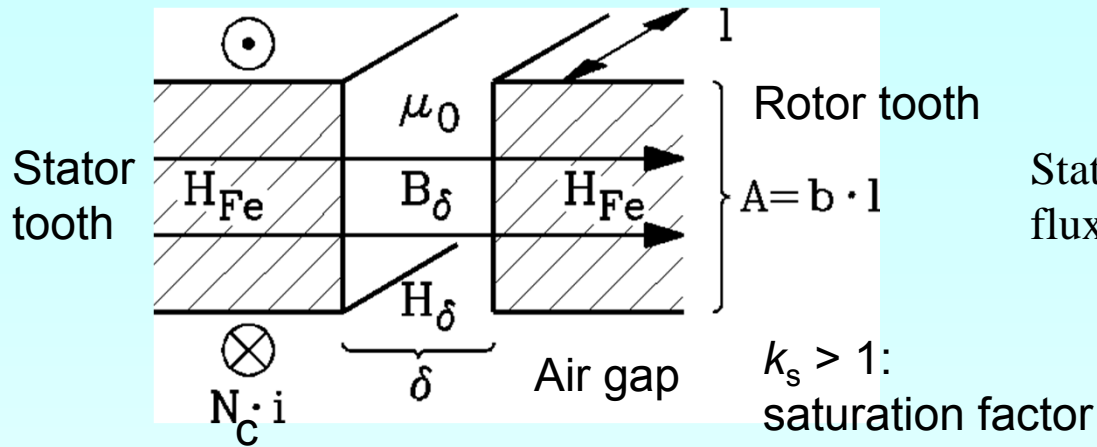


Symmetric rotor cannot start from aligned position

Phase 2 exerts magnetic pull on **asymmetric rotor** to self-start in ccw direction

# Flux linkage per phase in SR machines

Stator coil

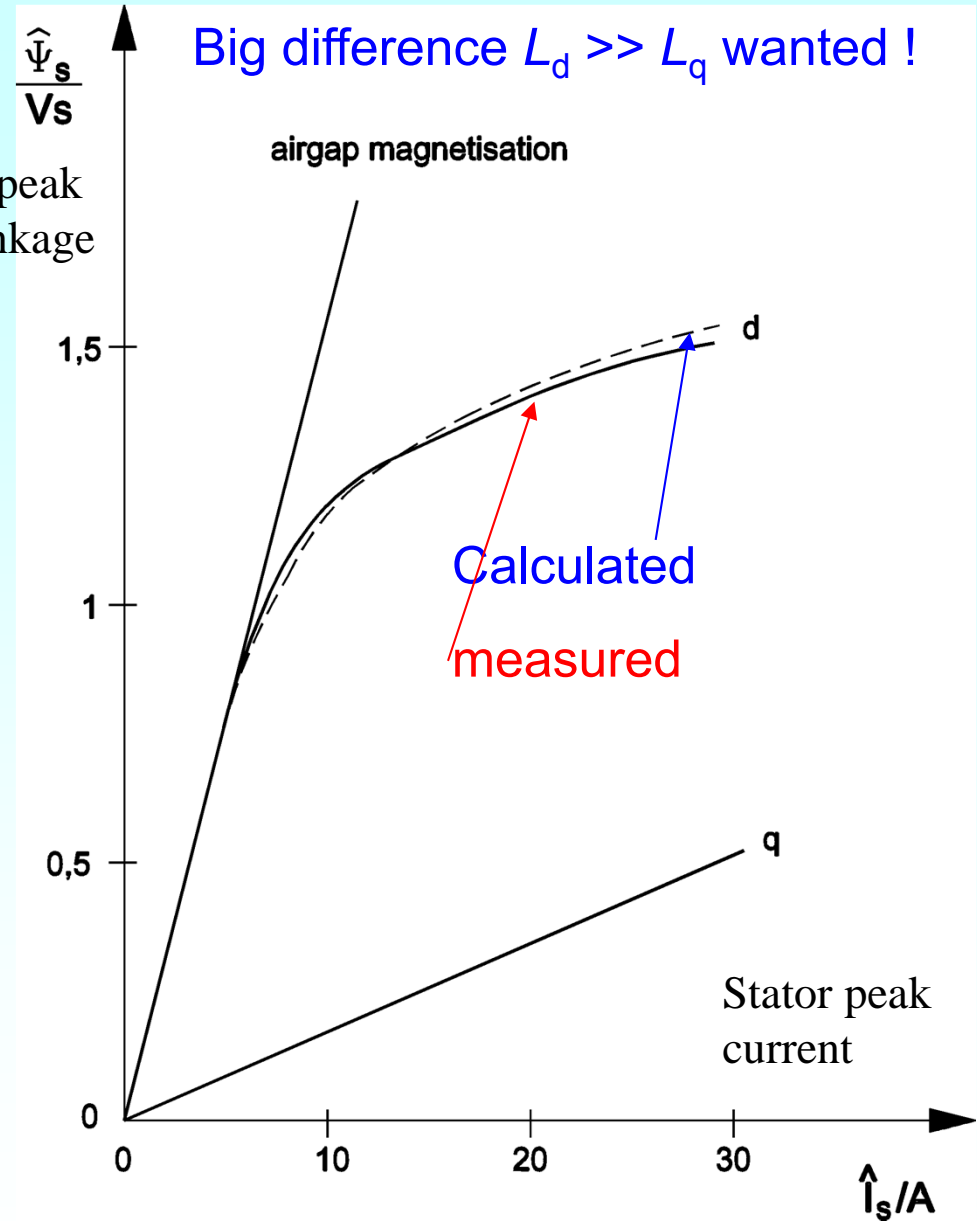


$$L_c = \frac{\Psi}{i} = \frac{N_c \cdot A \cdot B_\delta}{i} = \mu_0 \cdot N_c^2 \cdot \frac{b}{\delta \cdot k_s} \cdot l$$

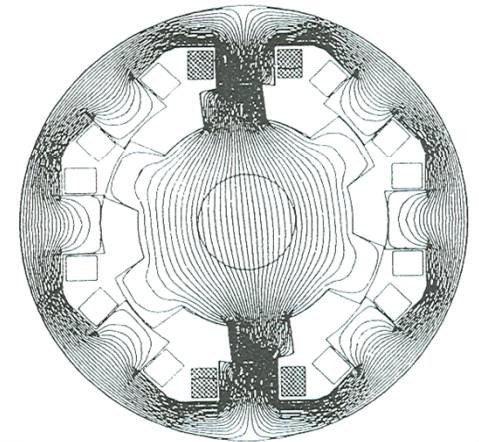
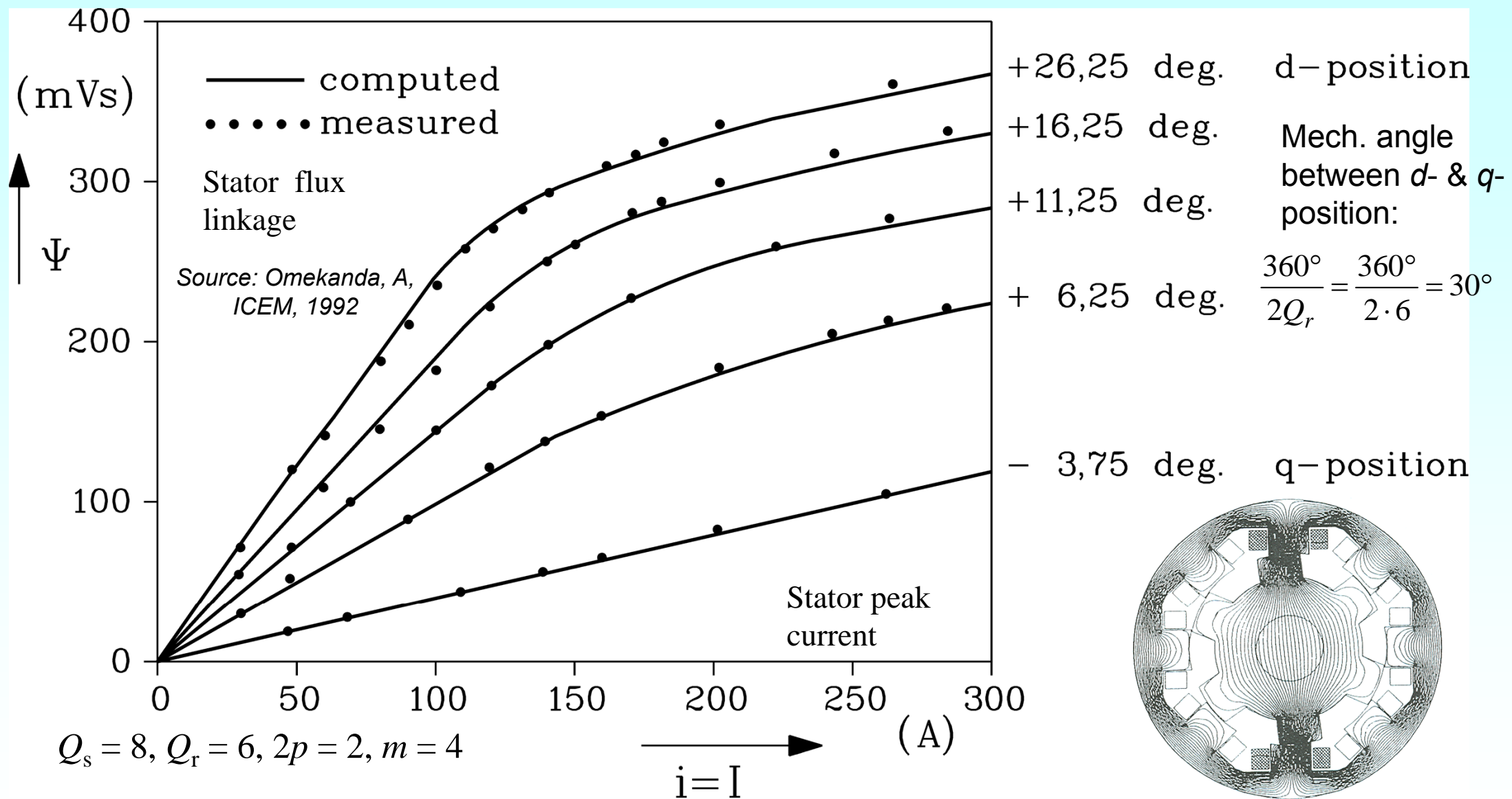
- Inductance is biggest in aligned position (**d-position:  $L_d = 2pL_{c,d}/a$** ) = small air gap  $\delta$ .
- Unaligned position (**q-position:  $L_q = 2pL_{c,q}/a$** ): Rotor slot opposes stator tooth = big air gap = small inductance.

**Facit:**

Inductance depends on stator current (= iron saturation) and rotor position .

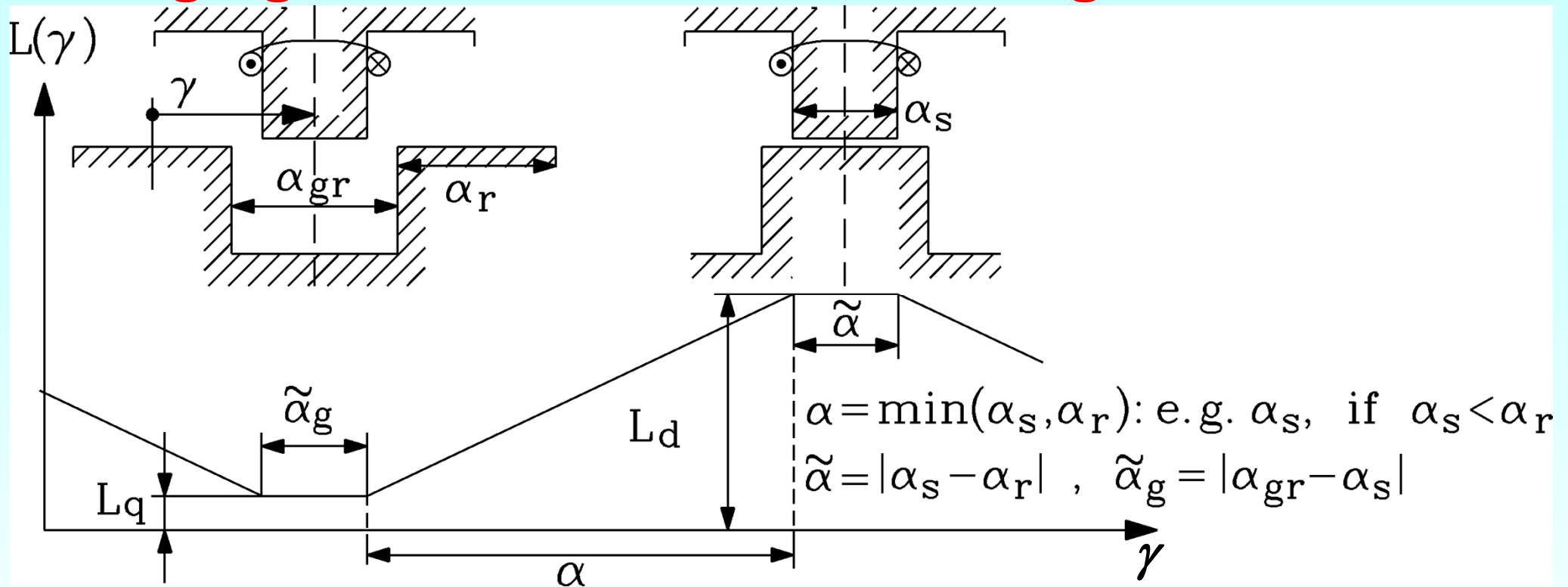


# Example: Numerically calculated flux linkage per phase in intermediate positions between $d$ - and $q$ -position





# Changing of stator inductance during rotor movement



- In order to get big torque the difference between d-axis and q-axis flux linkage (inductance) must be very big, which holds true for all kinds of reluctance machines.

- Sign of current polarity does not influence sign of torque, so uni-polar current feeding is sufficient.

# Voltage equation per phase of a SR machine

Rotor position angle  $\gamma$  (mech. degrees):  
Determines speed and inductance !  $\Omega_m = \frac{d\gamma}{dt}$

Flux linkage depends on rotor position angle  $\gamma$  and current  $i$  (saturation):

$$\psi(\gamma, i) = L(\gamma, i) \cdot i$$

Voltage equation per phase:  $u = R \cdot i + \frac{d\psi}{dt} = R \cdot i + \left. \frac{d\psi}{d\gamma} \right|_{i=c.} \cdot \frac{d\gamma}{dt} + \left. \frac{d\psi}{di} \right|_{\gamma=c.} \cdot \frac{di}{dt}$

Induced voltage due to rotor motion (“Back EMF”):  $u_i = \left. \frac{d\psi}{d\gamma} \right|_{i=c.} \cdot \Omega_m = i \cdot \frac{dL(\gamma, i)}{d\gamma} \cdot \Omega_m$

Inductive voltage drop:  $\left. \frac{d\psi}{di} \right|_{\gamma=c.} \cdot \frac{di}{dt}$

Special case: Saturation neglected:  $\psi(\gamma, i) = L(\gamma) \cdot i$

“Back EMF”:  $u_i = i \cdot \frac{dL(\gamma)}{d\gamma} \cdot \Omega_m$  Inductive voltage drop:  $\left. \frac{d\psi}{di} \right|_{\gamma=c.} \cdot \frac{di}{dt} = L \cdot \frac{di}{dt}$

# Power balance per phase of a SR machine

Magnetic energy per phase:  $W_{mag} = \int_0^{\psi} i \cdot d\psi$

Special case: No iron saturation:  $\psi(\gamma, i) = L(\gamma) \cdot i$

$$W_{mag} = \int_0^{\psi} i \cdot d\psi = \int_0^i i \cdot L(\gamma) \cdot di = \frac{L(\gamma) \cdot i^2}{2}$$

Change of magnetic energy per phase:  $\frac{dW_{mag}}{dt} = \frac{d}{dt} \frac{L(\gamma) \cdot i^2}{2} = \frac{i^2}{2} \cdot \frac{dL(\gamma)}{d\gamma} \cdot \frac{d\gamma}{dt} + \frac{L(\gamma)}{2} \cdot 2 \cdot i \cdot \frac{di}{dt}$

Voltage equation per phase:  $u = R \cdot i + \frac{d\psi}{dt} = R \cdot i + L \cdot \frac{di}{dt} + i \cdot \frac{dL}{d\gamma} \cdot \Omega_m$

Power equation per phase:  $p_e = u \cdot i = R \cdot i^2 + i \cdot L \cdot \frac{di}{dt} + i^2 \cdot \frac{dL}{d\gamma} \cdot \Omega_m$

General power balance per phase:  $p_e = p_{Cu} + \frac{dW_{mag}}{dt} + p_{\delta}$

Mechanical air gap power (“internal power”):  $p_{\delta} = \frac{1}{2} i^2 \cdot \frac{dL}{d\gamma} \cdot \Omega_m$

Electromagnetic torque per phase:  $M_e = p_{\delta} / \Omega_m = \frac{1}{2} i^2 \cdot \frac{dL}{d\gamma}$

# Torque equation of SR machine

Special case: No iron saturation:  $\psi(\gamma, i) = L(\gamma) \cdot i$

**Electromagnetic torque** ( $\gamma$ : mech. degrees):

$$M_e = p_\delta / \Omega_m = \frac{1}{2} \cdot i^2 \cdot \frac{dL(\gamma)}{d\gamma}$$

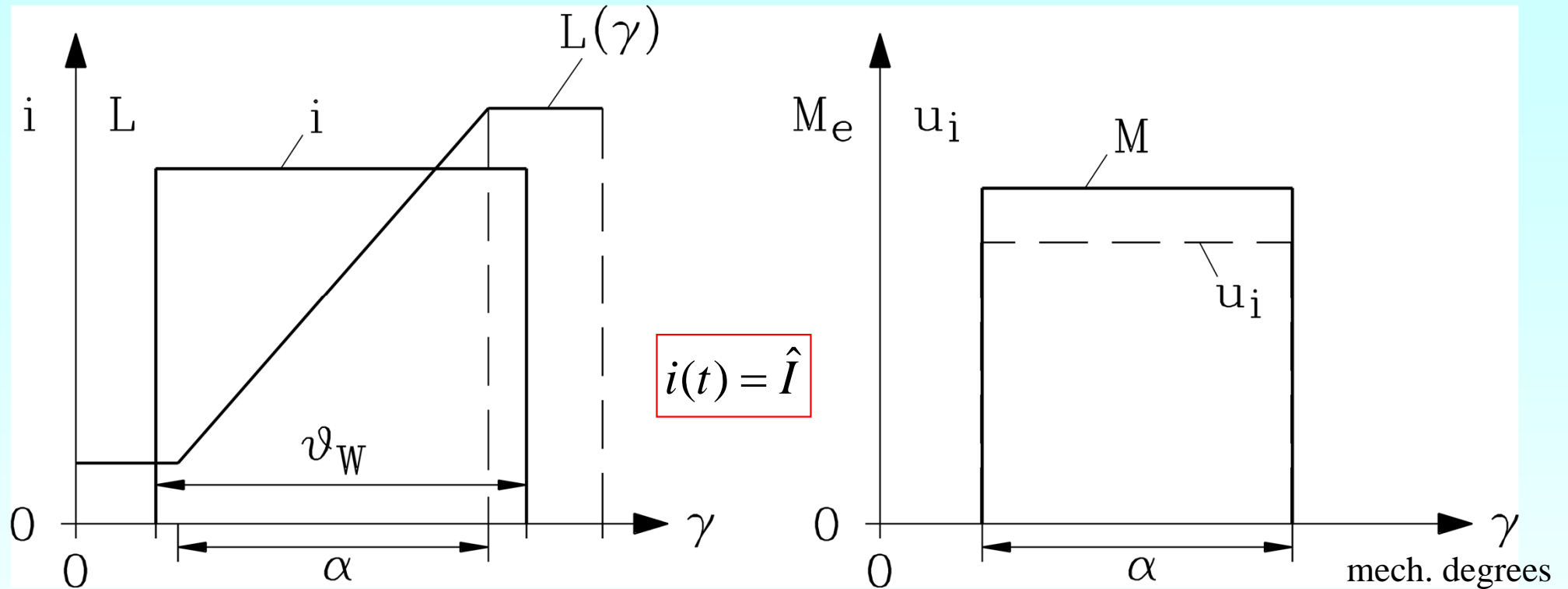
**Electromagnetic torque** ( $\gamma$ : el. degrees):

$$M_e = \frac{Q_r}{2} \cdot i^2 \cdot \frac{dL}{d\gamma}$$

One electrical period of the stator current corresponds to a rotation of the rotor by one rotor slot pitch. Hence:

$$\gamma(\text{mech.}) = \gamma(\text{ele.}) / Q_r$$

# SR machine operation at ideal conditions (1)



- Ideally constant current per phase (=ideal inverter)
- Ideally linear rising inductance per phase (= a) no 2D fringing flux, b) no saturation)
- Ideally constant torque, ideally constant back EMF

$$M_e = \frac{1}{2} i^2 \cdot \frac{dL}{d\gamma} = \frac{1}{2} \hat{I}^2 \cdot \frac{L_d - L_q}{\alpha}$$

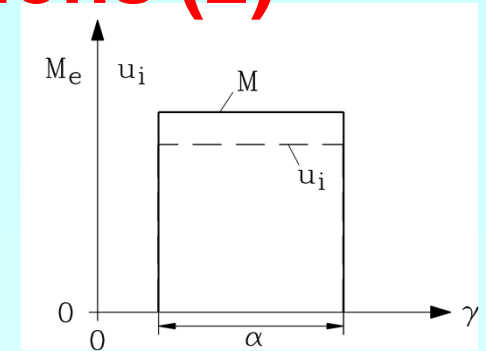
$$\hat{U}_i = \hat{I} \cdot \frac{L_d - L_q}{\alpha} \cdot \Omega_m$$

# SR machine operation at ideal conditions (2)

- Linear variation of phase inductance with rotor position assumed !

$L = L_s$ : stator phase inductance

$$M_e = \frac{1}{2} i^2 \cdot \frac{dL_s}{d\gamma} = \frac{1}{2} \hat{I}^2 \cdot \frac{L_d - L_q}{\alpha}$$



*If no saturation occurs, torque rises with the square of current.*

$\gamma$  in mech. degrees

## Note: Generator mode:

Current flow, when rotor moves from aligned to unaligned position:

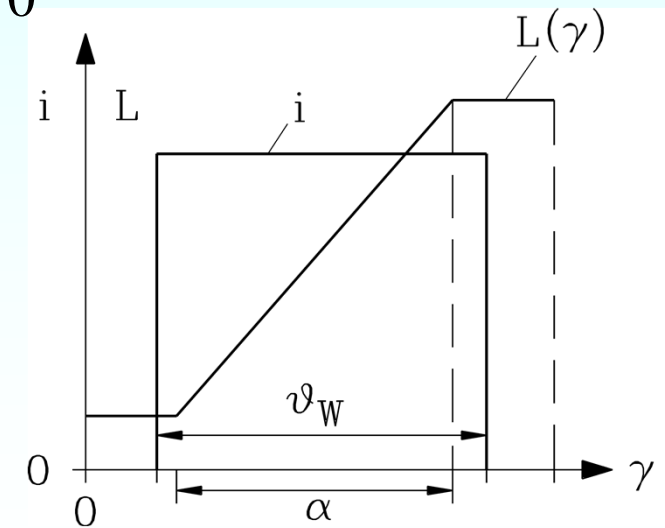
negative (braking) torque

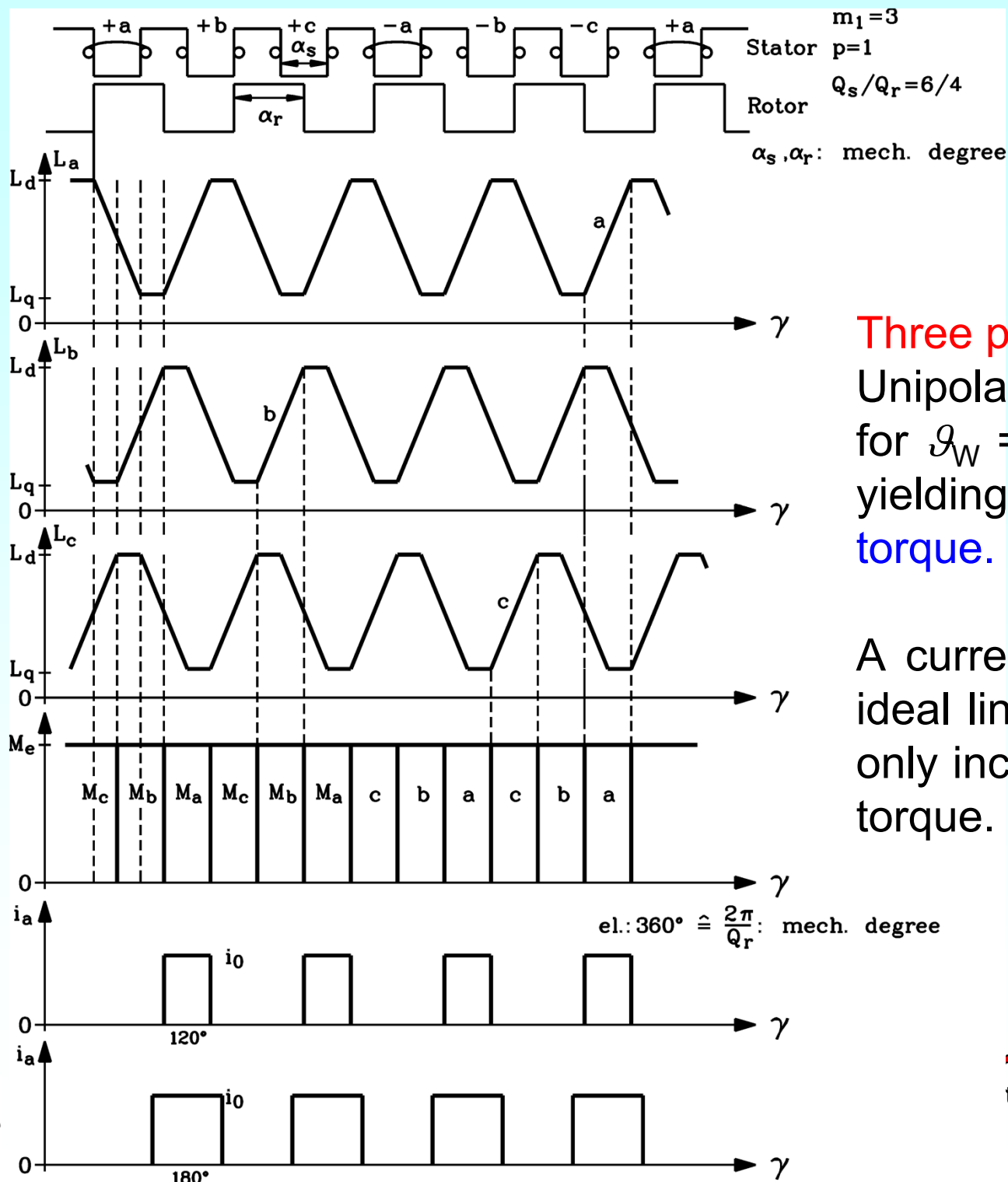
$$M_e = \frac{1}{2} i^2 \cdot \frac{dL}{d\gamma} = \frac{1}{2} \hat{I}^2 \cdot \frac{L_q - L_d}{\alpha} < 0$$

## Back EMF:

$$\hat{U}_i = \hat{I} \cdot \frac{L_d - L_q}{\alpha} \cdot \Omega_m > 0, \quad P_\delta = \hat{U}_i \hat{I} / 2 > 0 \quad \text{motor}$$

$$\hat{U}_i = \hat{I} \cdot \frac{L_q - L_d}{\alpha} \cdot \Omega_m < 0, \quad P_\delta = \hat{U}_i \hat{I} / 2 < 0 \quad \text{generator}$$





## Current angle in SR machines

### Three phase 6/4-SR machine:

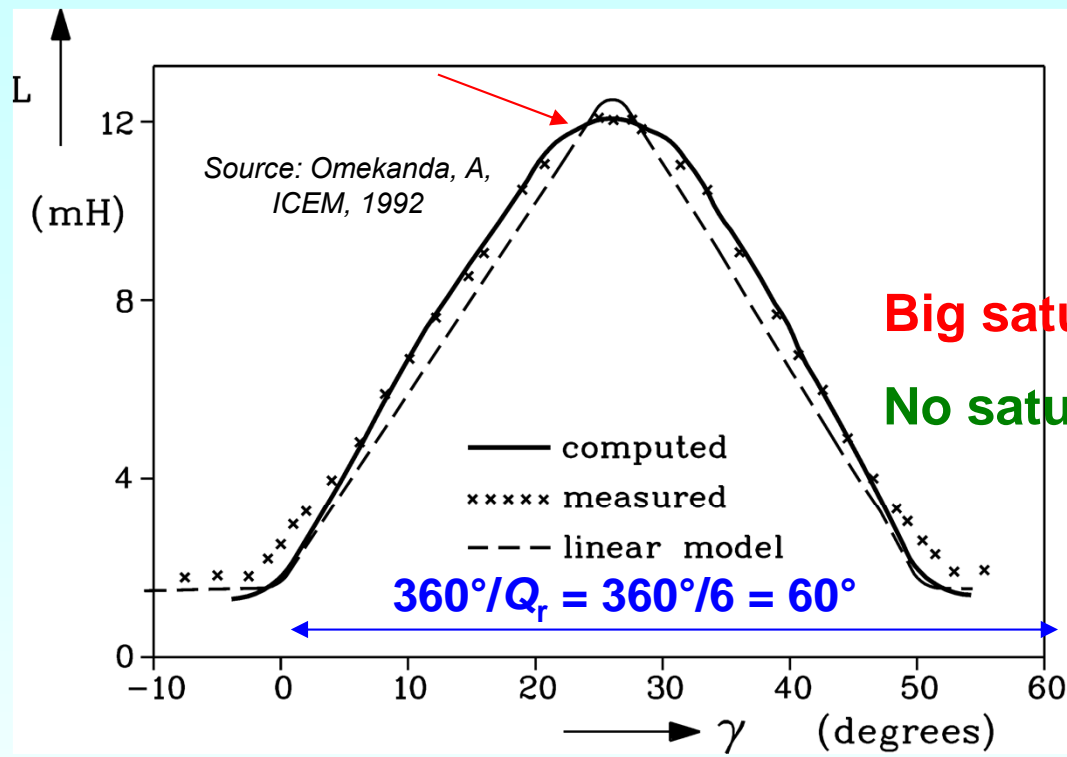
Unipolar current impression is done for  $\vartheta_W = \alpha = 120^\circ$  el. for each phase, yielding a theoretically smooth torque.

A current impression of  $180^\circ$  at this ideal linear change of inductance will only increase resistive losses, but not torque.





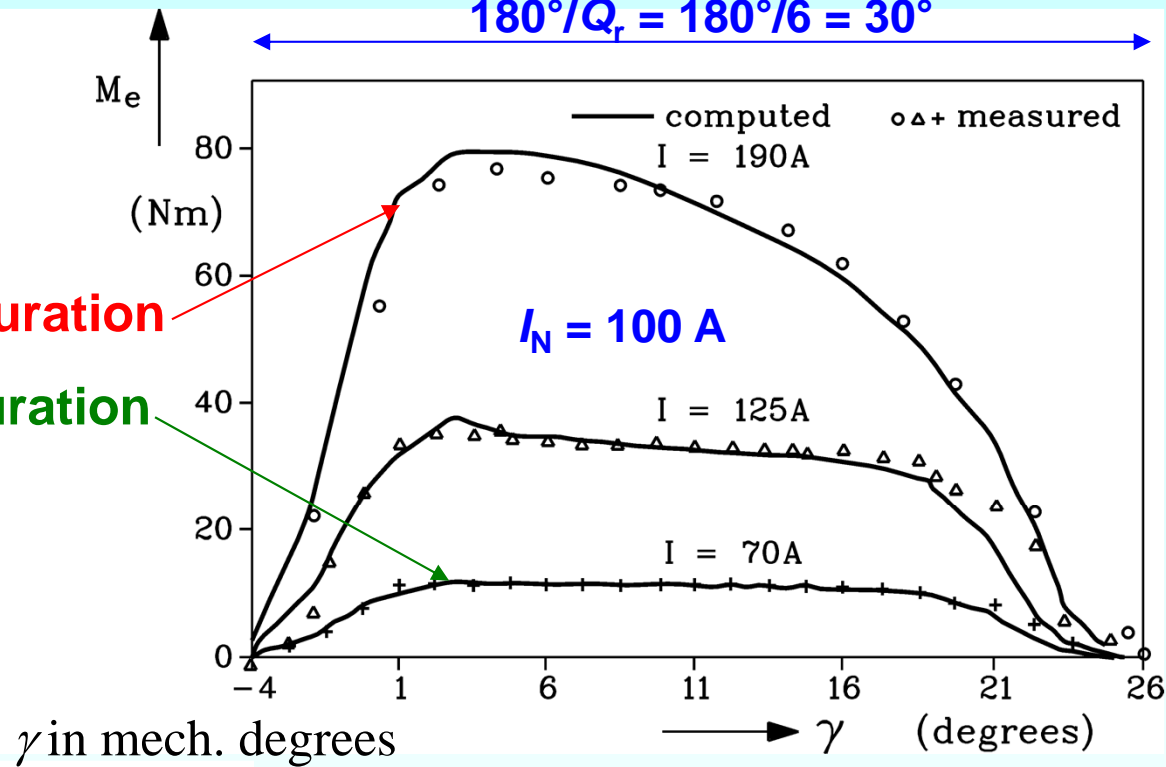
# Example: Numerically calculated inductance and torque per phase



**Inductance per phase**

- Real inductance does not rise exactly linear with rotor position

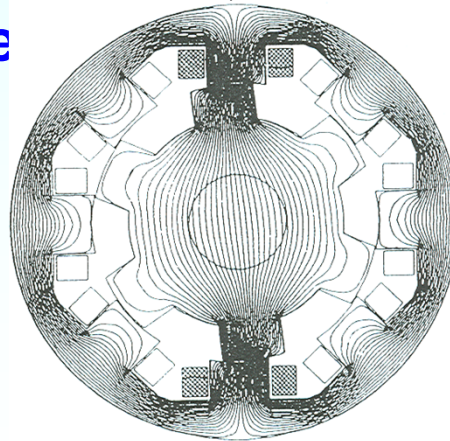
$$Q_s = 8, Q_r = 6, 2p = 2, m = 4$$



**Torque per phase**

- Real torque is not ideally constant, although current is ideally constant.

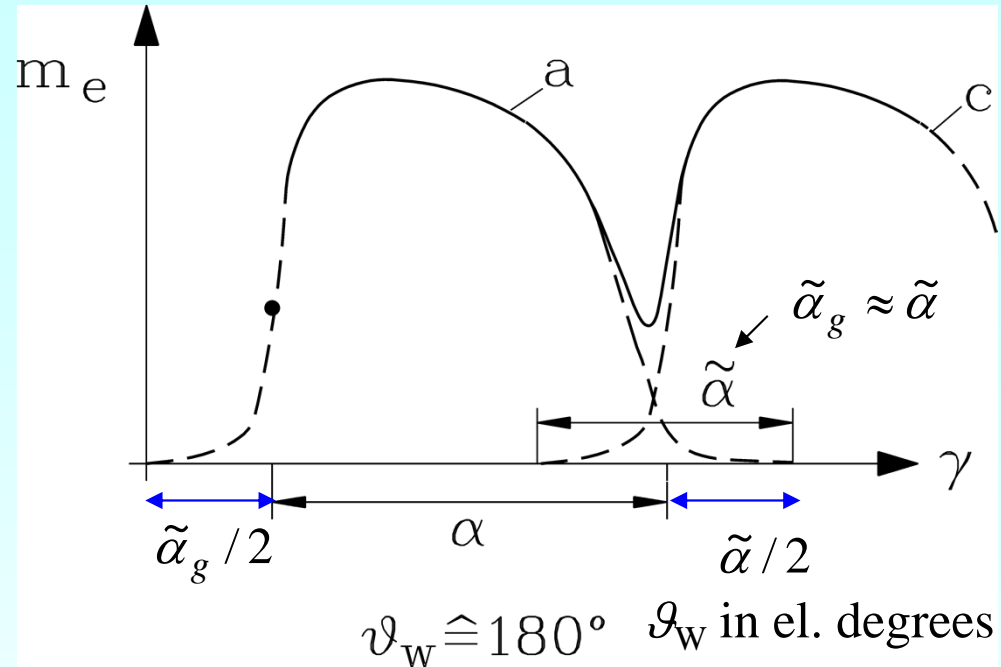
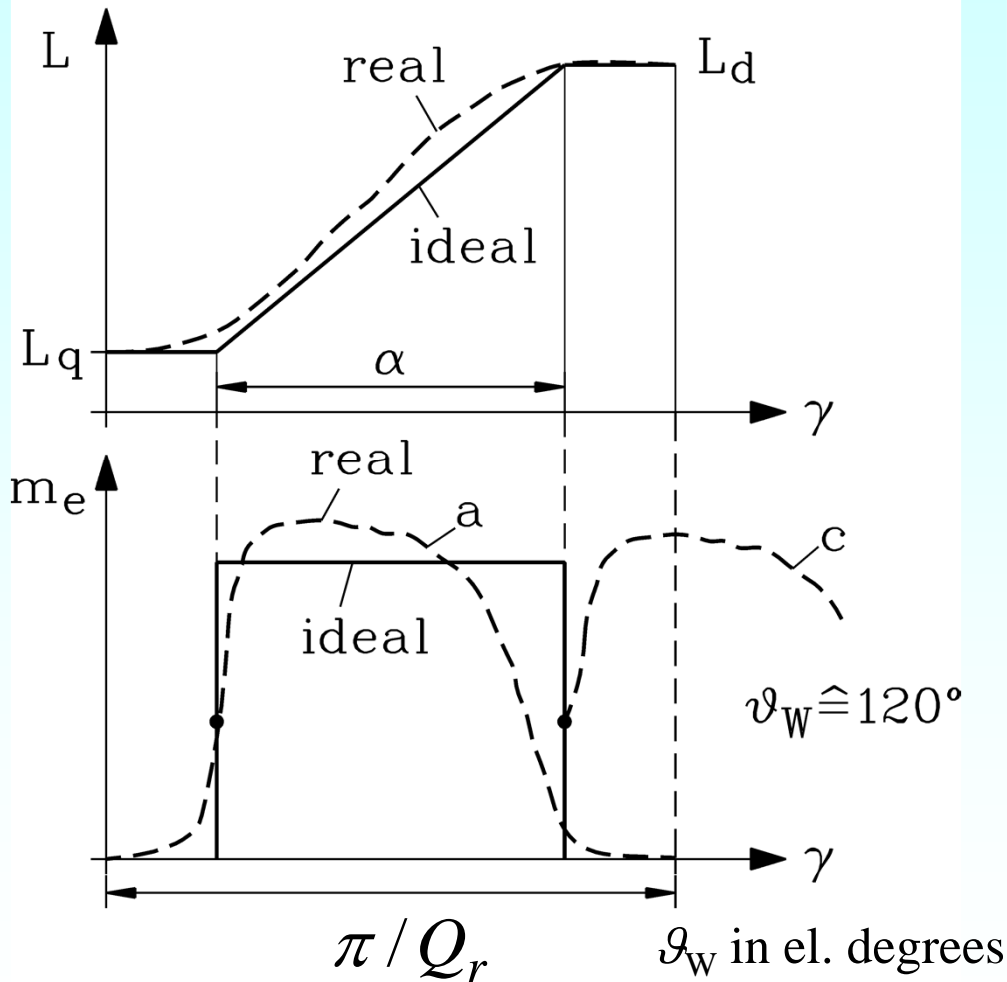
- Saturation deviates torque further.



# Real change of inductance with moving rotor

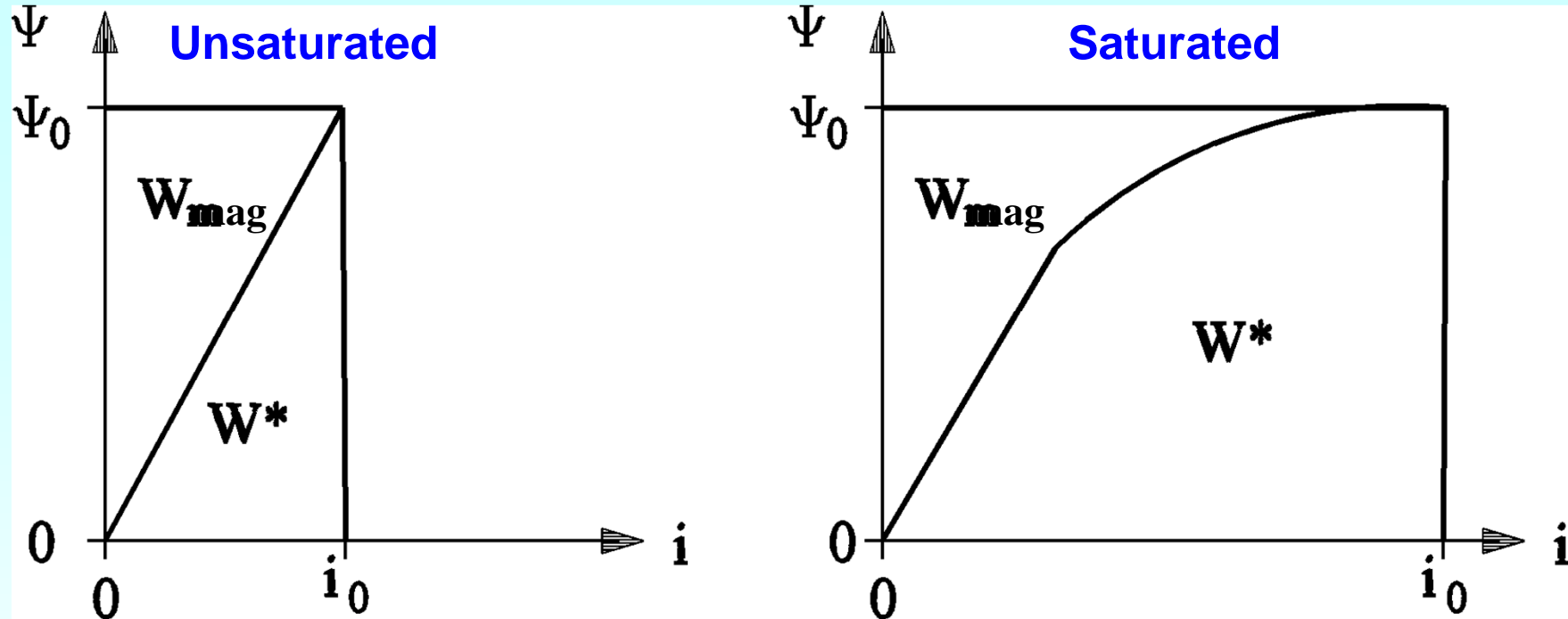
$$M_e(\gamma) = (1/2) \cdot i^2 \cdot dL/d\gamma$$

$i = \text{const.}$



- **Real:** Non-linear change of inductance: Torque ripple occurs !
- If current angle is **increased** from  $120^\circ$  el. to  $180^\circ$  el., the torque ripple is reduced and average torque is raised.

# Saturation in SR machines

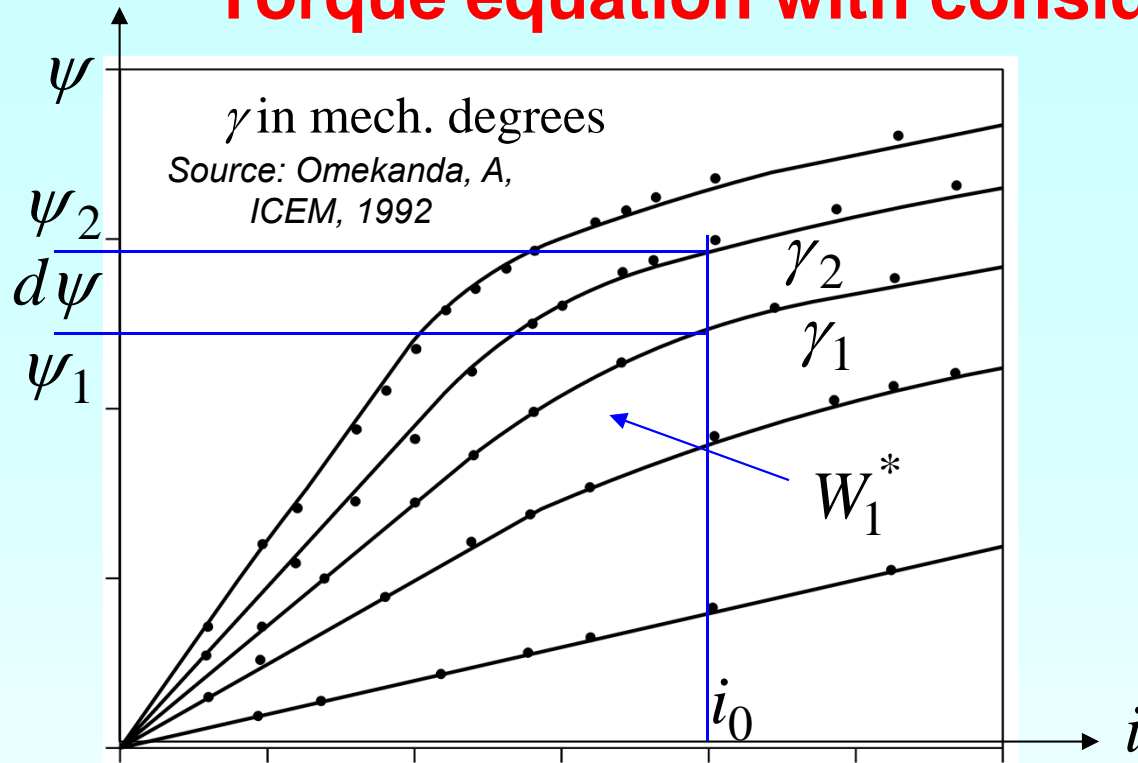


Magnetic energy: unsaturated  $W_{mag} = \int_0^{\psi} i \cdot d\psi = L \int_0^i i \cdot di = L \frac{i^2}{2}$

Magnetic co-energy:  $W^* = \psi \cdot i - W_{mag}$

In saturated machine magnetic co-energy is bigger than magnetic energy !  
 Electromagnetic torque is proportional to co-energy, so high saturation is aimed !

# Torque equation with consideration of iron saturation



If rotor moves by increment angle  $d\gamma$  (at constant current) from  $q$  to  $d$  axis, flux linkage increases by  $d\psi$ .

$$W_1^* = \psi_1 \cdot i_0 - W_{mag,1}$$

$$W_2^* = \psi_2 \cdot i_0 - W_{mag,2}$$

$$dW^* = W_2^* - W_1^* =$$

$$= (\psi_2 - \psi_1) \cdot i_0 - (W_{mag,2} - W_{mag,1})$$

Increase of magnetic energy and co-energy leads to energy balance per phase:

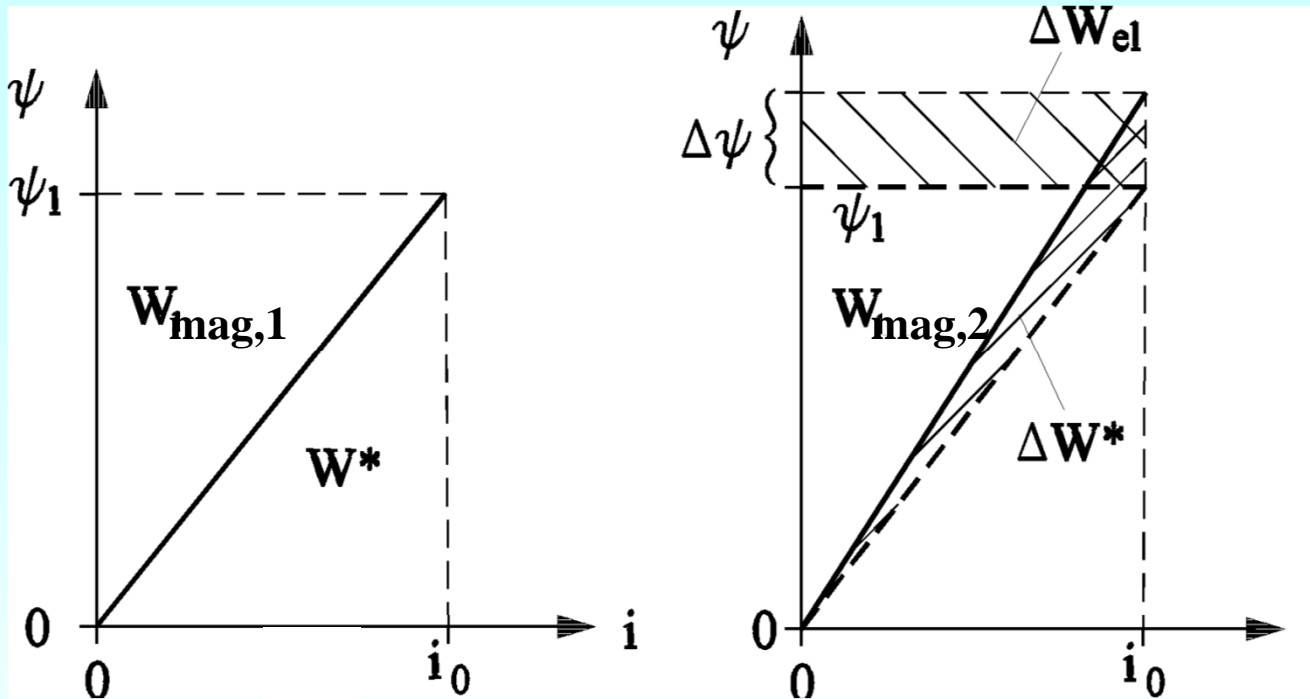
$$dW^* = d\psi \cdot i_0 - dW_{mag}$$

$$u = R \cdot i_0 + \frac{d\psi}{dt} \Rightarrow dW_e = u \cdot i_0 \cdot dt = R \cdot i_0^2 \cdot dt + i_0 \cdot d\psi = R \cdot i_0^2 \cdot dt + dW_{mag} + dA_m$$

$$dA_m = M_e \cdot d\gamma = M_e \cdot \Omega_m \cdot dt \Rightarrow dW^* = dA_m$$

$$M_e(\gamma, i) = \frac{dW^*}{d\gamma}$$

# Magnetic energy and co-energy in linear material



If rotor moves by increment angle  $\Delta\gamma$  (at constant current) from  $q$  to  $d$  axis, flux linkage increases by  $\Delta\psi$ .

$\gamma$  in mech. degrees

Increase of magnetic energy and co-energy leads to energy balance per phase:

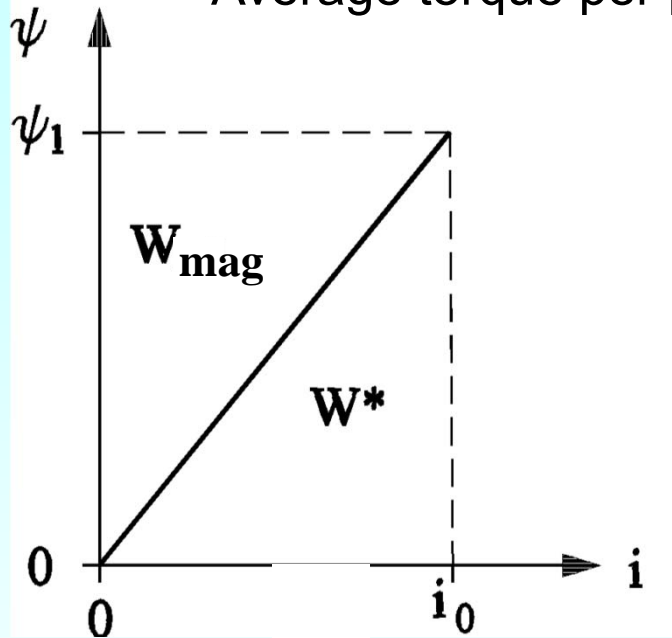
$$W_{mag,2} = W_{mag,1} + dW_{mag} = W_{mag,1} + i_0 \cdot d\psi - dW^*$$

$$u = R \cdot i_0 + \frac{d\psi}{dt} \Rightarrow dW_e = u \cdot i_0 \cdot dt = R \cdot i_0^2 \cdot dt + i_0 \cdot d\psi = R \cdot i_0^2 \cdot dt + dW_{mag} + dA_m$$

$$dA_m = M_e \cdot d\gamma = M_e \cdot \Omega_m \cdot dt \Rightarrow dW^* = dA_m \Rightarrow M_e(\gamma, i) = \frac{dW^*}{d\gamma}$$

# Example: Torque calculation for linear iron

Average torque per phase for rotor movement from  $q$ - to  $d$ -axis at phase current  $i$ :



a) Torque calculation from co-energy:

$$M_e(\gamma, i) = \frac{dW^*}{d\gamma} \quad \Delta W_{q \rightarrow d}^* = \frac{L_d}{2} i^2 - \frac{L_q}{2} i^2$$

$$\Delta \gamma_{q \rightarrow d} = \pi / Q_r$$

$\gamma$ : mech. degrees

$$M_e(\gamma, i) = \frac{\Delta W^*}{\Delta \gamma} = \left( \frac{L_d}{2} - \frac{L_q}{2} \right) \cdot i^2 \cdot \frac{Q_r}{\pi}$$

b) Torque calculation change of inductance:

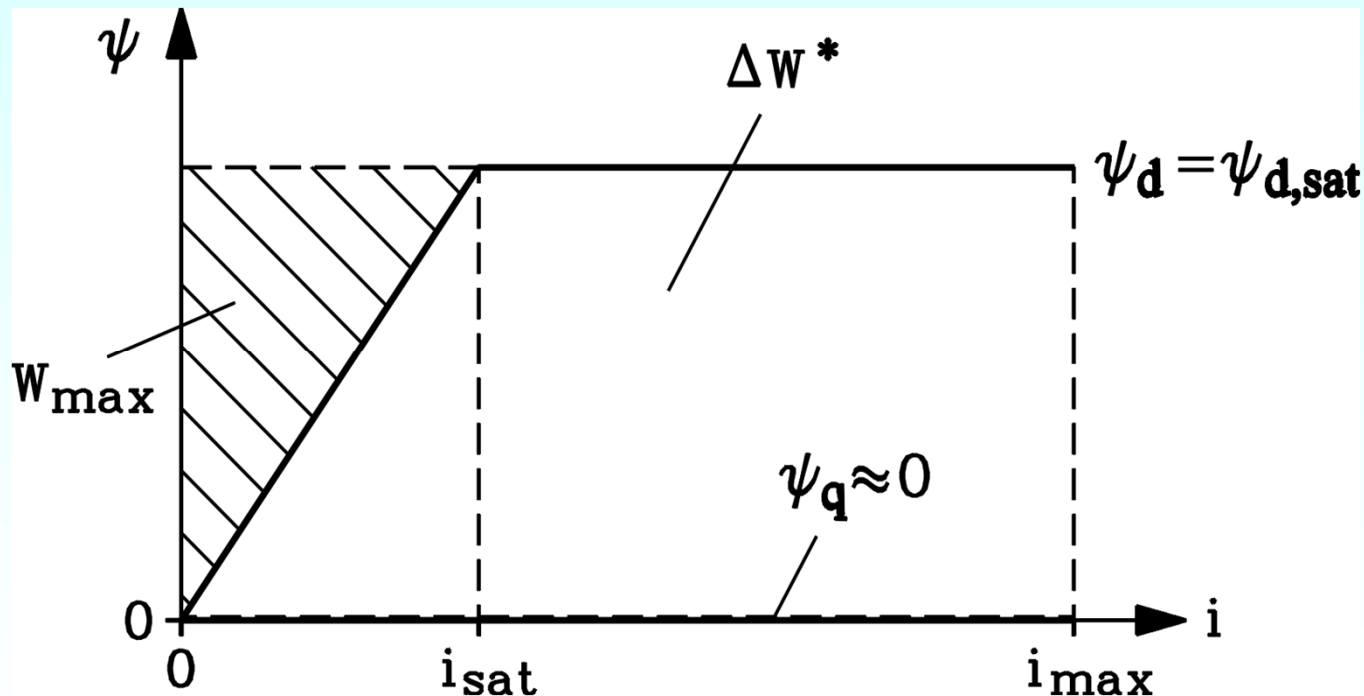
$$M_e = \frac{1}{2} i^2 \cdot \frac{dL}{d\gamma} = \frac{1}{2} i^2 \cdot \frac{L_d - L_q}{\pi / Q_r}$$

Facit: For linear iron methods a) and b) deliver identical results. For saturated iron method a) must be used.

# High utilization of SR machine needs high saturation

Torque calculation is done from map of  $\psi(i, \gamma)$ -curves, evaluating for given current the change of co-energy with change of rotor angle  $\gamma$ .

SR machines shall be operated highly saturated in order to limit inverter rating by limiting switched magnetic energy.



Torque is proportional to change of co-energy between  $d$ - and  $q$ -position  $\Delta W^*$ :

a) Unsaturated case  $i < i_{sat}$

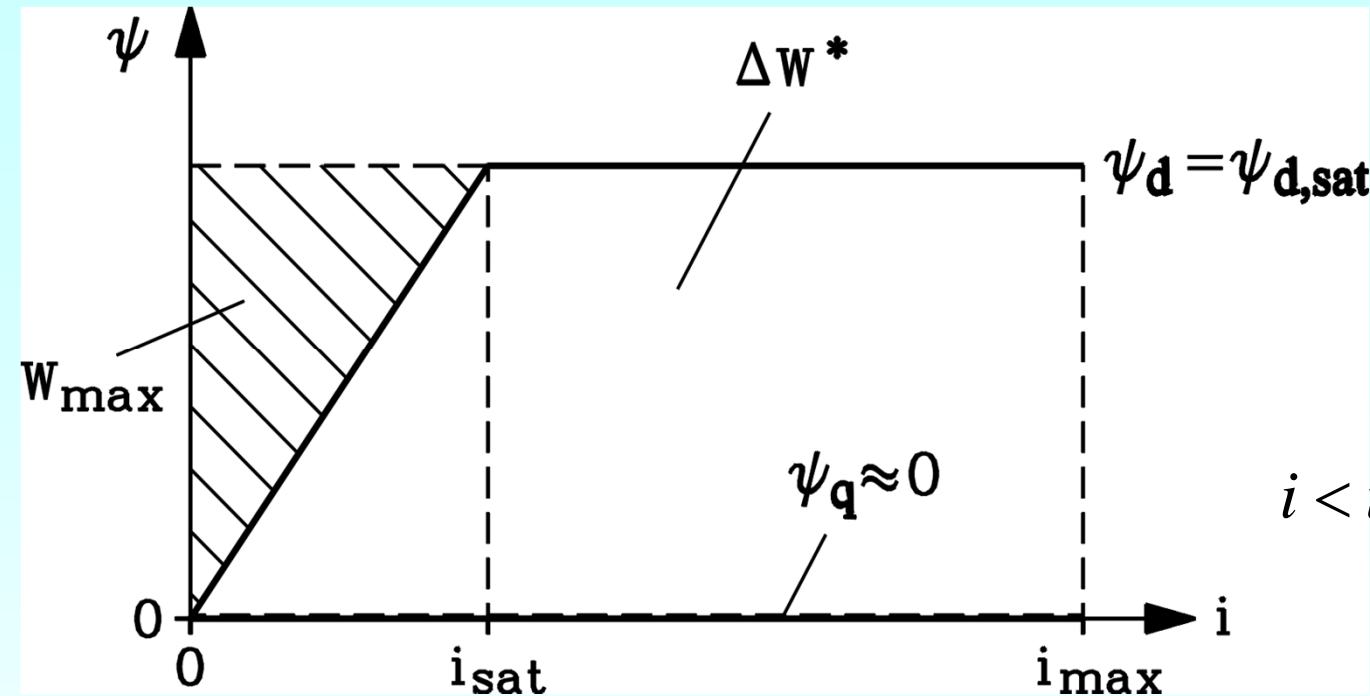
Torque is proportional  $i^2$

b) Saturated case  $i > i_{sat}$

Torque tends to be proportional nearly  $i$



# Torque-current characteristic



$$W_{max} = \psi_{d,sat} \cdot i_{sat} / 2$$

$$\Delta\gamma_{q \rightarrow d} = \pi / Q_r$$

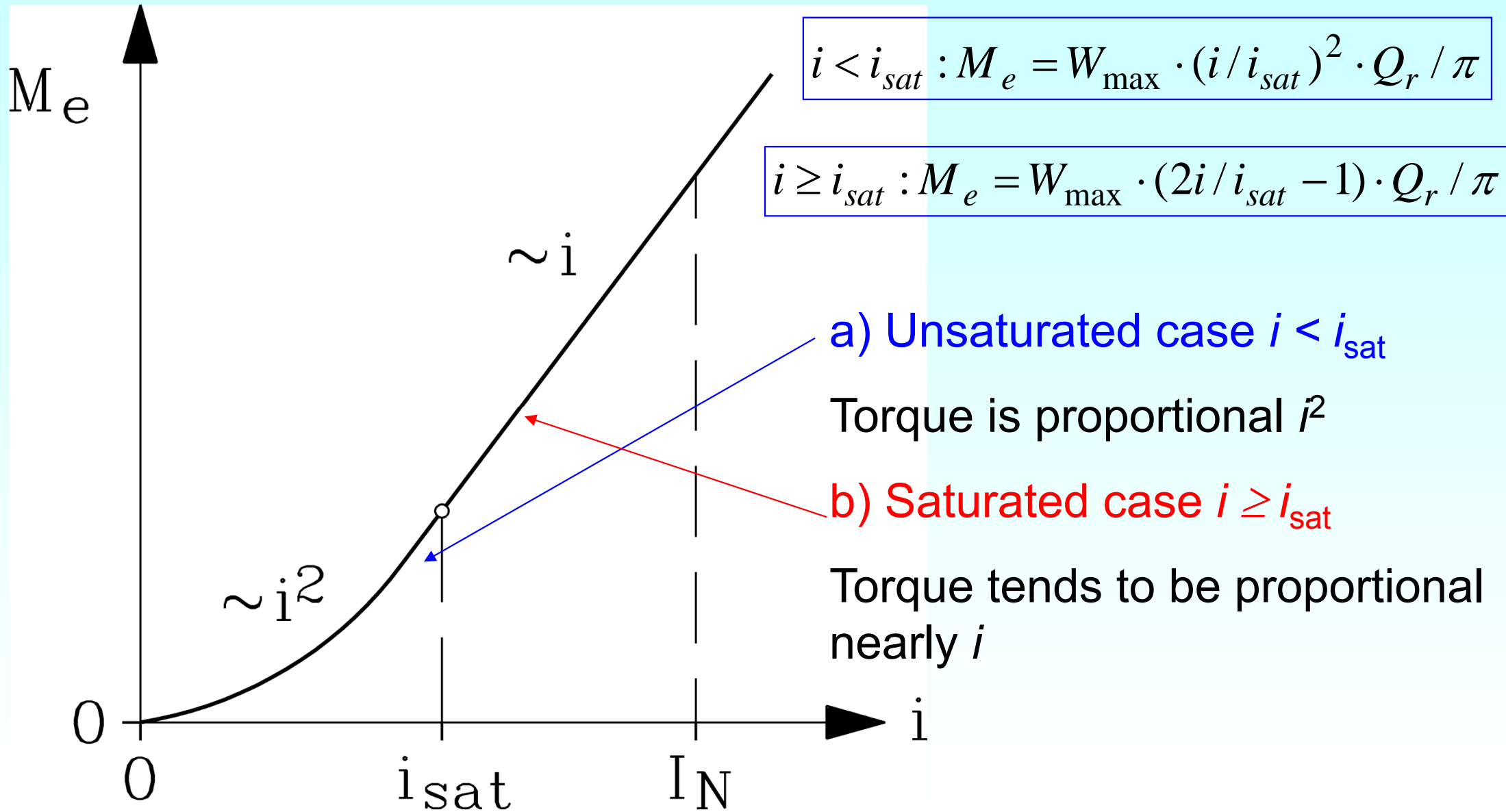
$$i < i_{sat} : \Delta W_{q \rightarrow d}^* = W_{max} \cdot (i / i_{sat})^2$$

$$i < i_{sat} : M_e = \Delta W_{q \rightarrow d}^* / \Delta\gamma_{q \rightarrow d} = W_{max} \cdot (i / i_{sat})^2 \cdot Q_r / \pi$$

$$i \geq i_{sat} : \Delta W_{q \rightarrow d}^* = W_{max} + \psi_{d,sat} \cdot (i - i_{sat}) = W_{max} + 2W_{max} \cdot (i / i_{sat} - 1)$$

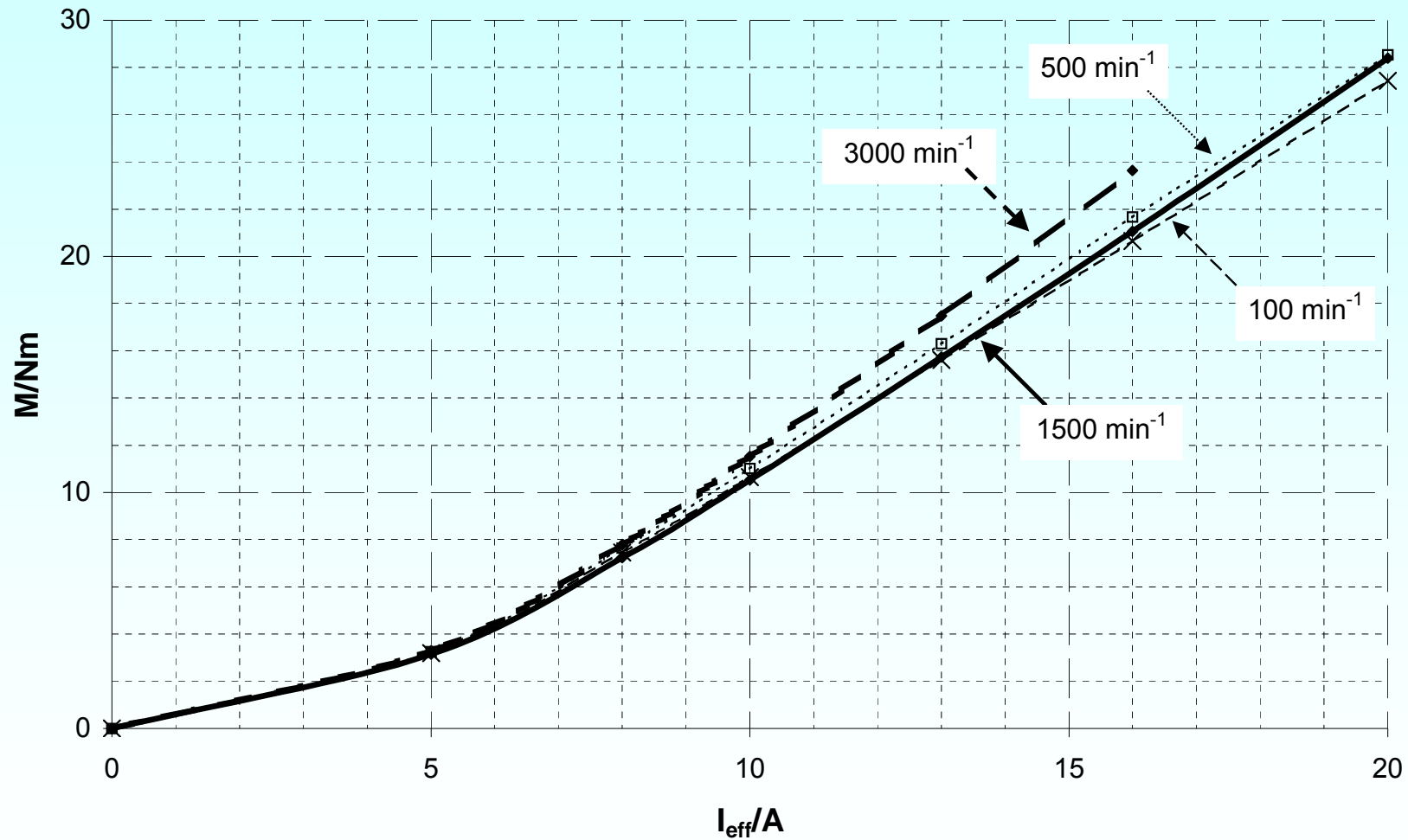
$$i \geq i_{sat} : M_e = \Delta W_{q \rightarrow d}^* / \Delta\gamma_{q \rightarrow d} = W_{max} \cdot (2i / i_{sat} - 1) \cdot Q_r / \pi$$

# Torque-current curve of switched reluctance machine

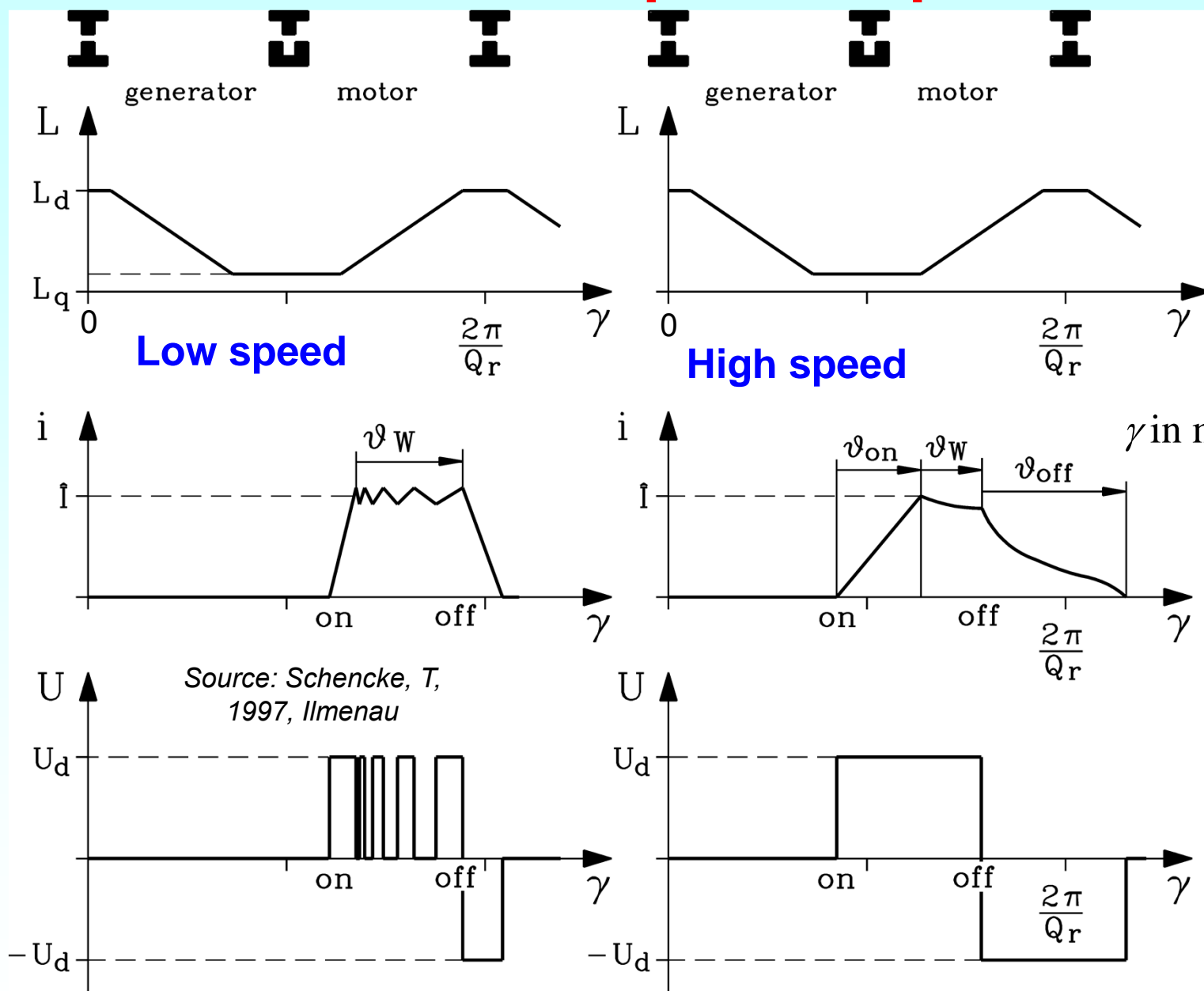


# Measured torque-current curve of a 1.2 kW SRD

4-pole, 3-phase SRD: Rated data: 1.2 kW, 1500 ... 6000/min, total mass 32 kg, rotor inertia 3.9 g·m<sup>2</sup>, stator/rotor teeth: 12/8, Company SICME/Italy



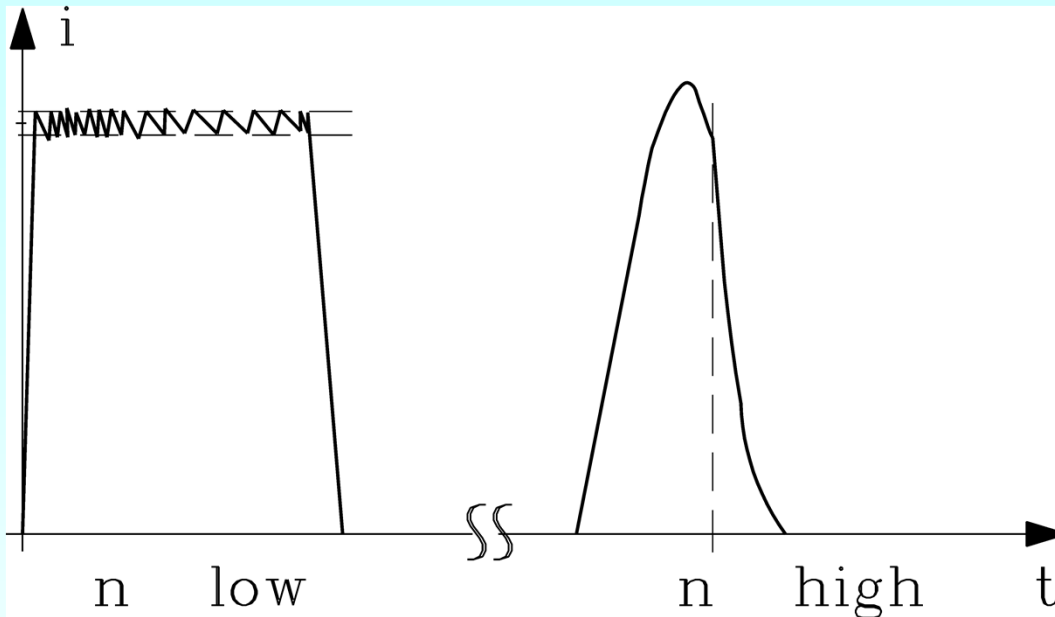
# Real shape of unipolar current



At low speed:  
Hysteresis control of current allows generation of block shaped unipolar current.

At high speed: Time is too short for hysteresis control. Only "voltage on/off" is possible. Thus distorted current generates **increased torque ripple**.

# Real shape of uni-polar current



**At low speed:** Hysteresis control of current allows generating rather block shaped unipolar current.

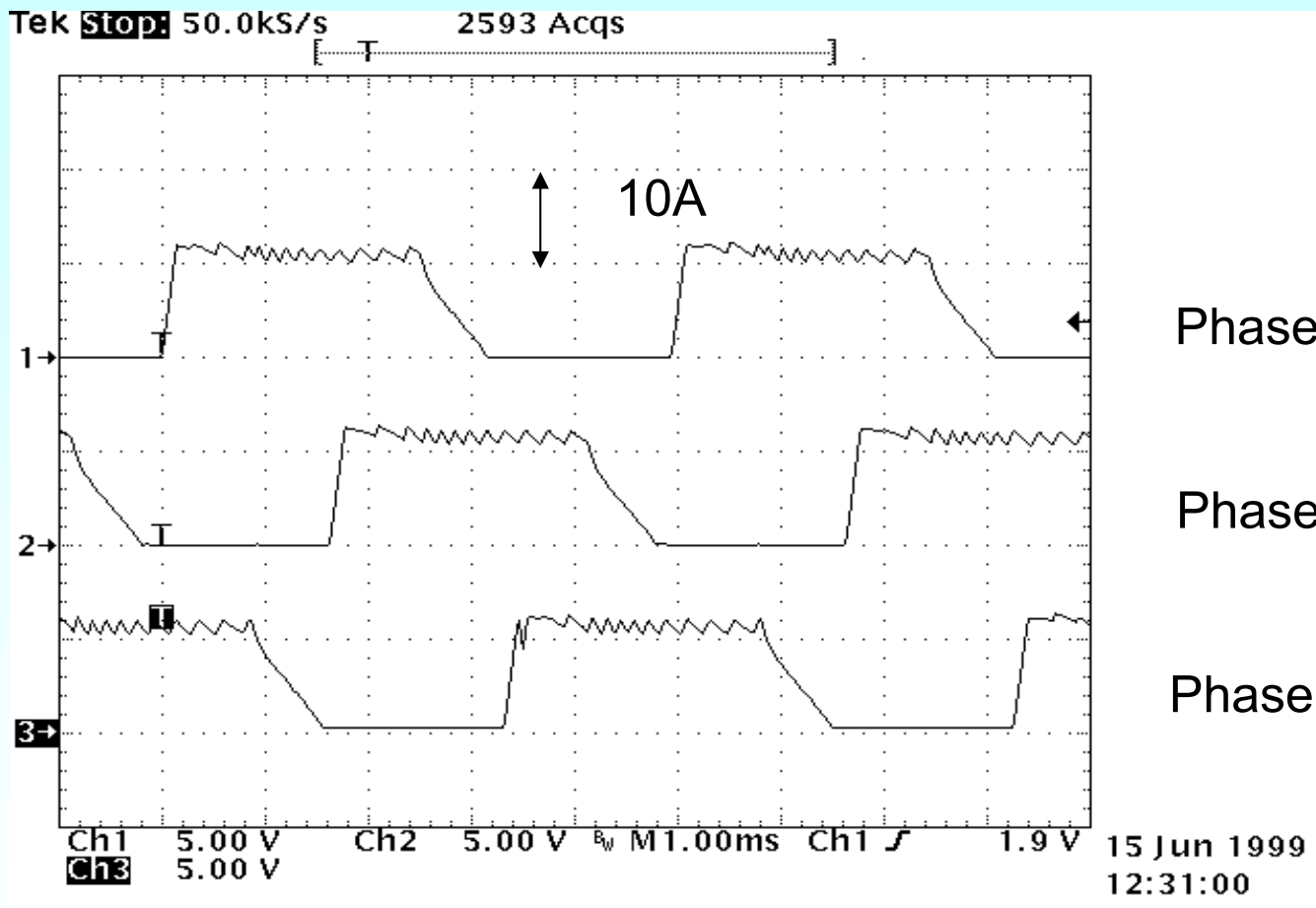
**At high speed:** Time is too short for hysteresis control. Only "voltage on/off" is possible. Thus distorted current generates **increased torque ripple**.

*Real SR machines show considerable torque ripple: at low speed due to non-linear variation of inductance, at high speed: increased ripple due to distorted current.*

*Frequency of torque ripple:*  $f_{puls} = n \cdot Q_r \cdot m$  e.g. 3000/min,  $Q_r = 8$ ,  $m = 3$ : [1.2 kHz](#)

# Measured uni-polar current signal at $n_N = 1500/\text{min}$

4-pole, 3-phase SRD: Rated data: 1.2 kW, 1500 ... 6000/min, total mass 32 kg, rotor inertia 3.9 g·m<sup>2</sup>, stator/rotor teeth: 12/8, Company SICME/Italy



**Currents are nearly block-shaped**

Current angle nearly 180°el

r.m.s. current at 180°el:

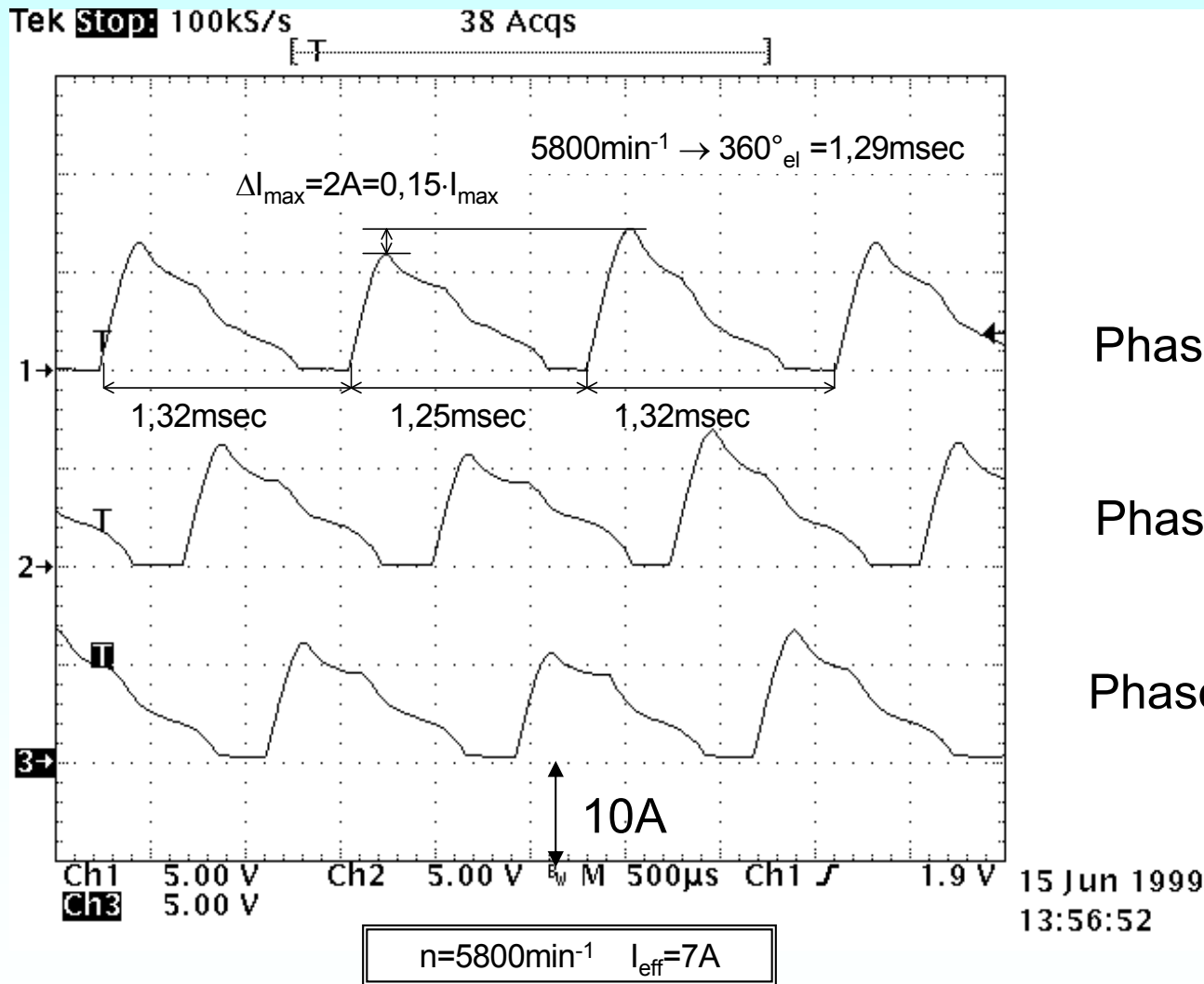
$$I_{rms} = \sqrt{\frac{1}{T} \int_0^T i(t)^2 dt} = \sqrt{\frac{1}{T} \hat{I}^2 \frac{T}{2}} = \frac{\hat{I}}{\sqrt{2}} = 0.71 \hat{I}$$

$$I_{rms} = 0.71 \cdot 12 = 8.5 \text{ A}$$

$n=1500\text{min}^{-1}$   $I_{\text{eff}}=8\text{A}$

# Measured uni-polar current signal at $n_{\max} = 5800/\text{min}$

4-pole, 3-phase SRD: Rated data: 1.2 kW, 1500 ... 6000/min, total mass 32 kg, rotor inertia 3.9 g·m<sup>2</sup>, stator/rotor teeth: 12/8, Company SICME/Italy



**Current wave-form deviates strongly from the ideal block shape**

Phase U

Phase V

Phase W



# SR Drive operation – torque-speed characteristic

a) *Current limit*: Inverter current limit usually 200% rated motor current to allow short time overload

b) *Voltage limit*: DC link block voltage is maximum inverter voltage:  $R_s \cong 0$ :

$$u = U_d = R \cdot \hat{I} + L \cdot \frac{d\hat{I}}{dt} + \hat{U}_i \Rightarrow U_d = \hat{U}_i = \hat{I} \cdot \frac{dL}{d\gamma} \cdot \Omega_m \quad \text{Block current: } \frac{d\hat{I}}{dt} = 0$$

$$\hat{I} = \frac{U_d}{dL_s / d\gamma} \cdot \frac{1}{\Omega_m} \cong \frac{U_d}{(L_d - L_q) / \alpha} \cdot \frac{1}{\Omega_m}$$

$$M_e \cong \frac{1}{2 \cdot (L_d - L_q) / \alpha} \cdot \left( \frac{U_d}{\Omega_m} \right)^2$$

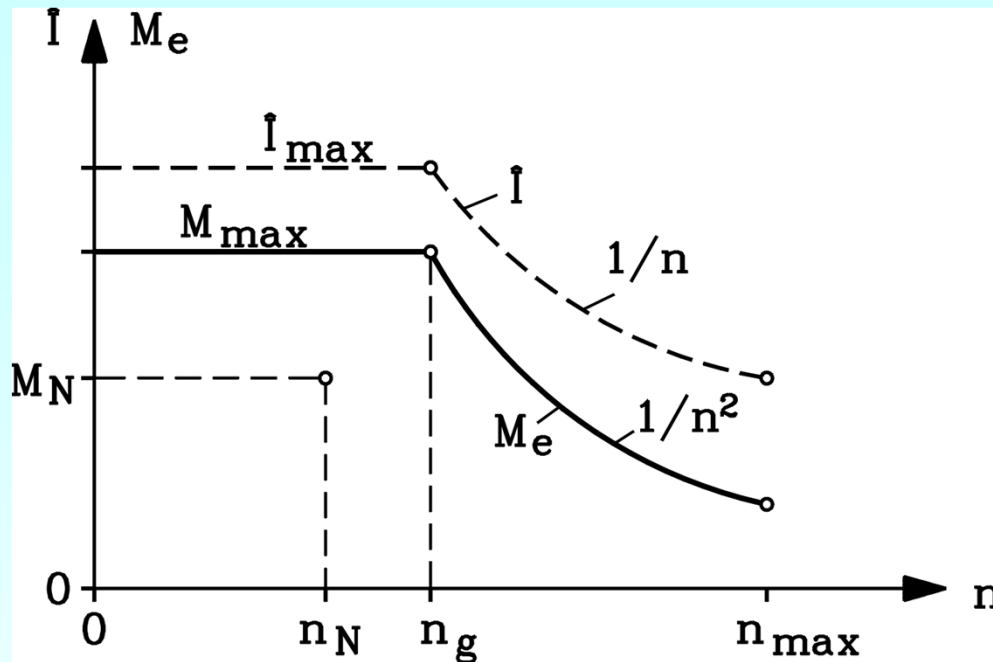
Possible current flow rises with inverse of decreasing speed, until it reaches the inverter current limit at speed:

$$n_g = \frac{1}{2\pi} \cdot \frac{U_d}{\hat{I}_{\max} \cdot ((L_d - L_q) / \alpha)}$$

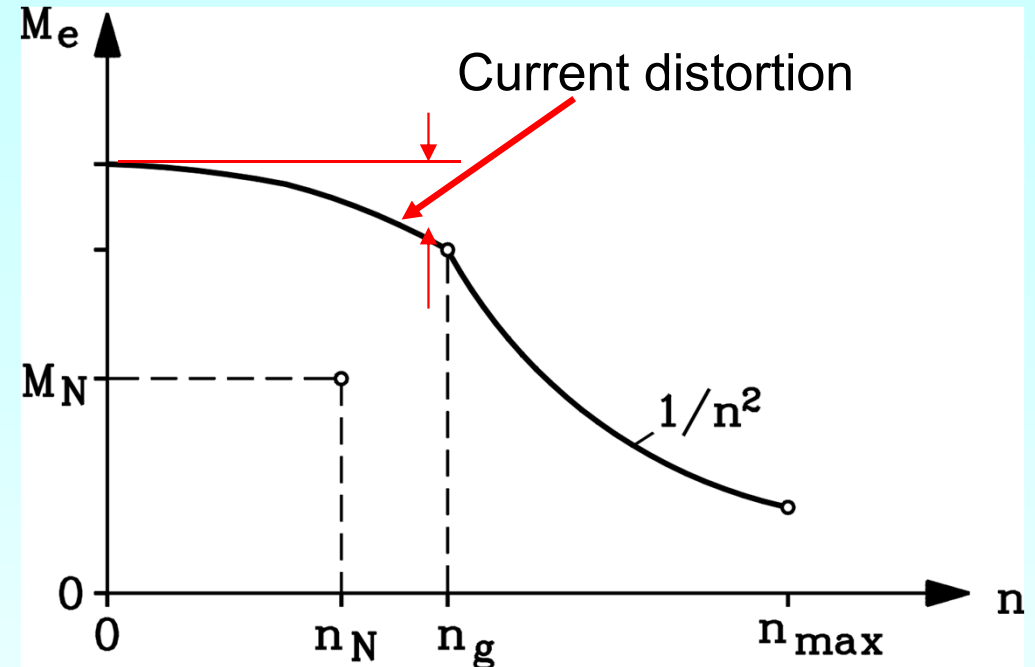
$\alpha$  in mech. degrees

*At the voltage limit the maximum possible torque of SR drives decreases with the square of rising speed.*

# Torque-speed characteristic of SR machine



a) for ideal block-shaped current,



b) considering real current shape  
which is distorted with rising speed

*Inverter current control:*

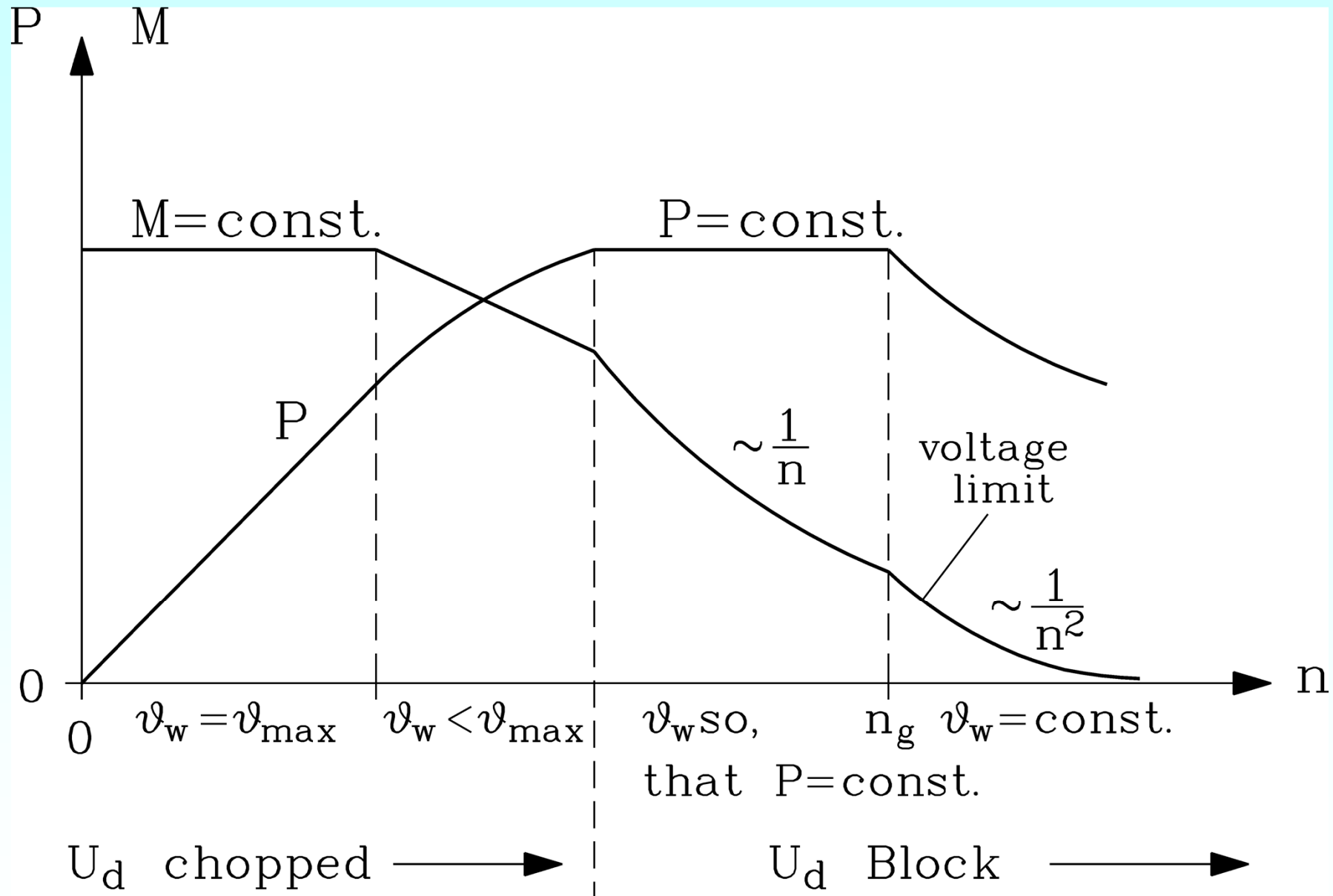
*At low speed:* **Block current** by hysteresis control with constant current angle

*Increased speed:* Current impulse duration  $T_W$  has to decrease

*At high speed:* Only voltage "switch on/off" possible so, that average torque decreases with  $1/n$  (**constant power operation**).

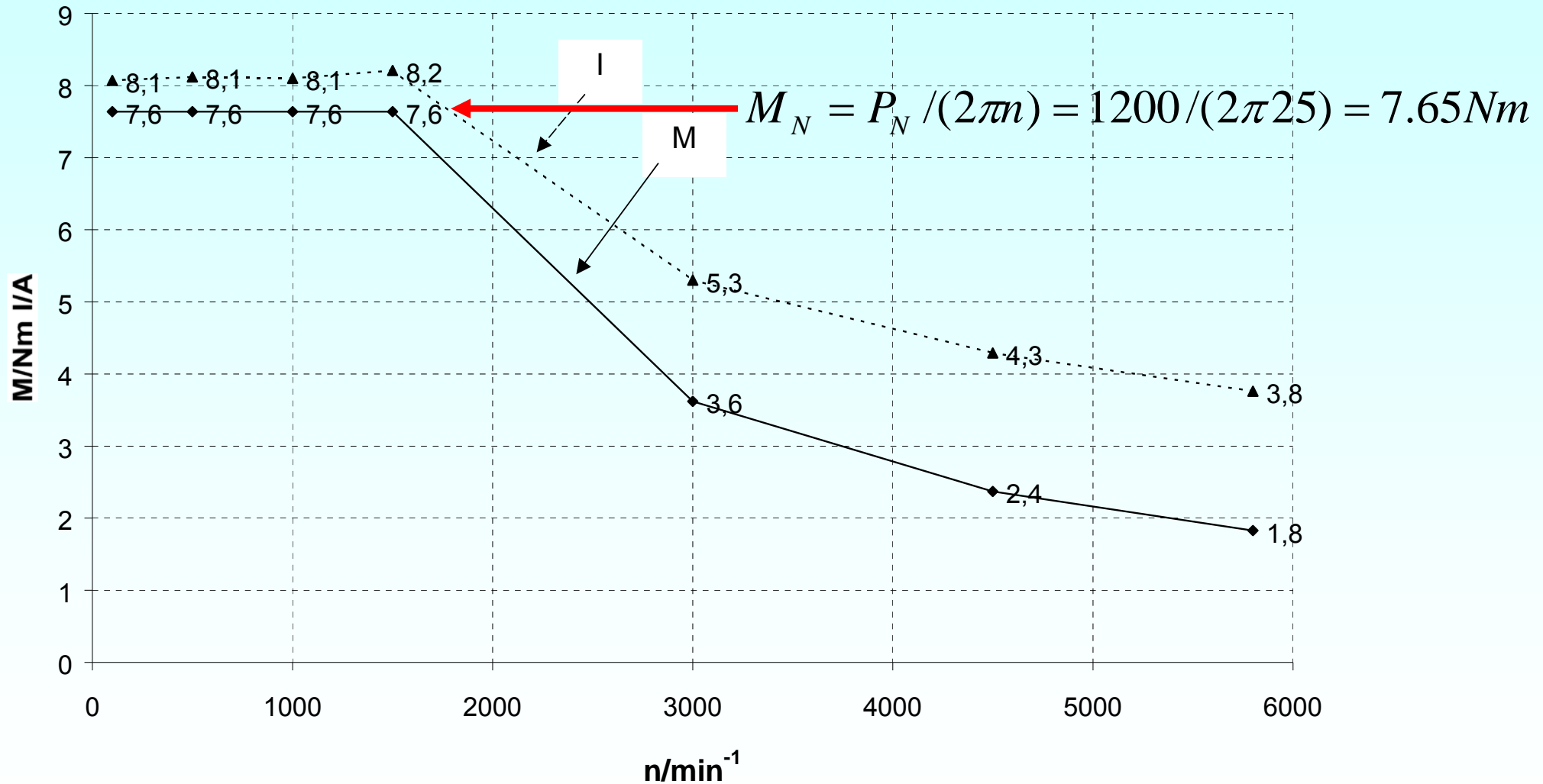
*Voltage limit:* No adjusting of current angle possible: torque decreases with  $1/n^2$ .

# Maximum SR torque & power, depending on speed



# Measured maximum SR torque & r.m.s. current over speed

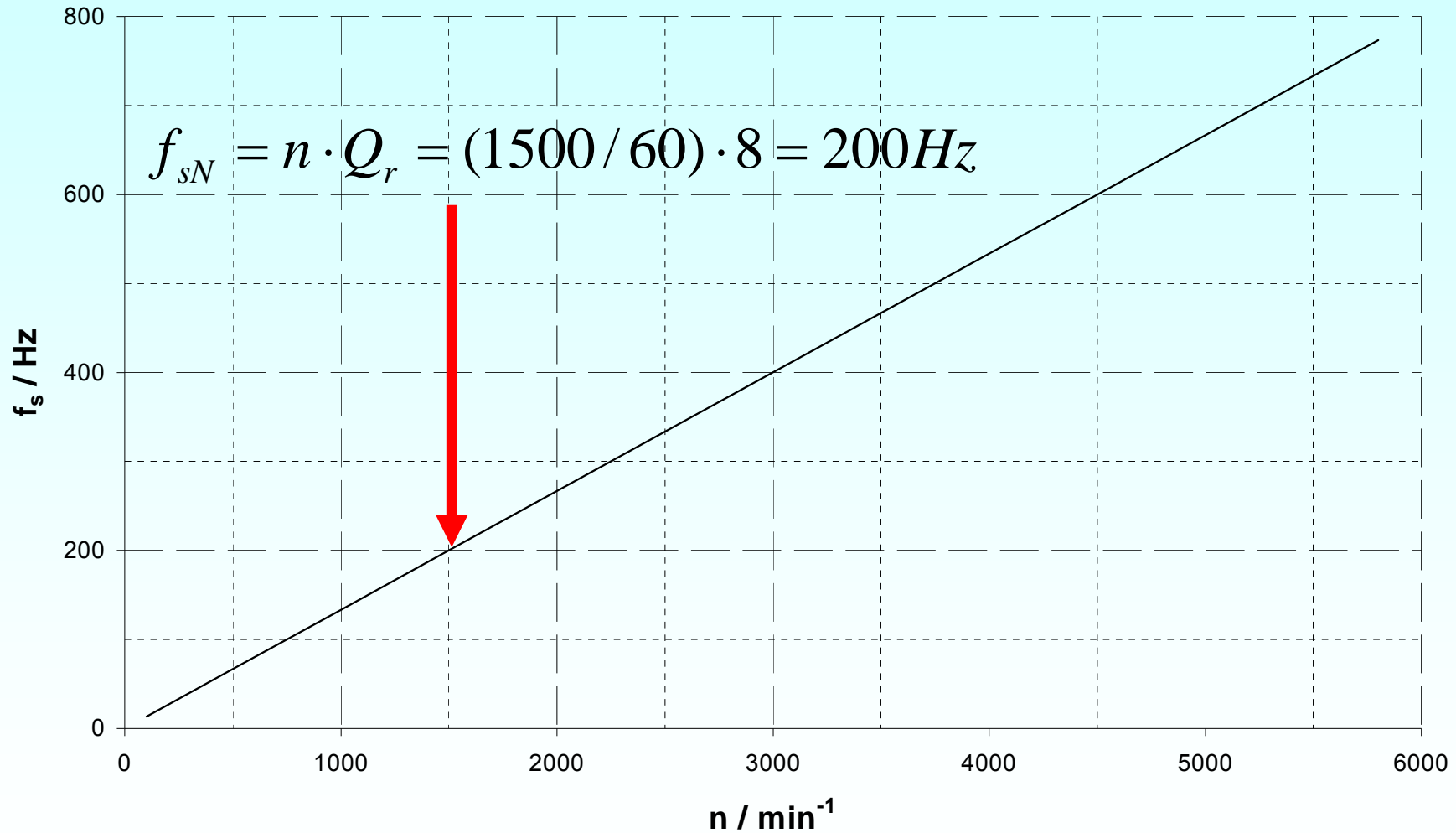
4-pole, 3-phase SRD: Rated data: 1.2 kW, 1500 ... 6000/min, total mass 32 kg, rotor inertia 3.9 g·m<sup>2</sup>, stator/rotor teeth: 12/8, Company SICME/Italy



# Stator frequency per phase over speed

4-pole, 3-phase SRD: Rated data: 1.2 kW, 1500 ... 6000/min, stator/rotor teeth: 12/8  
Company SICME/Italy

$$f_s = n \cdot Q_r$$

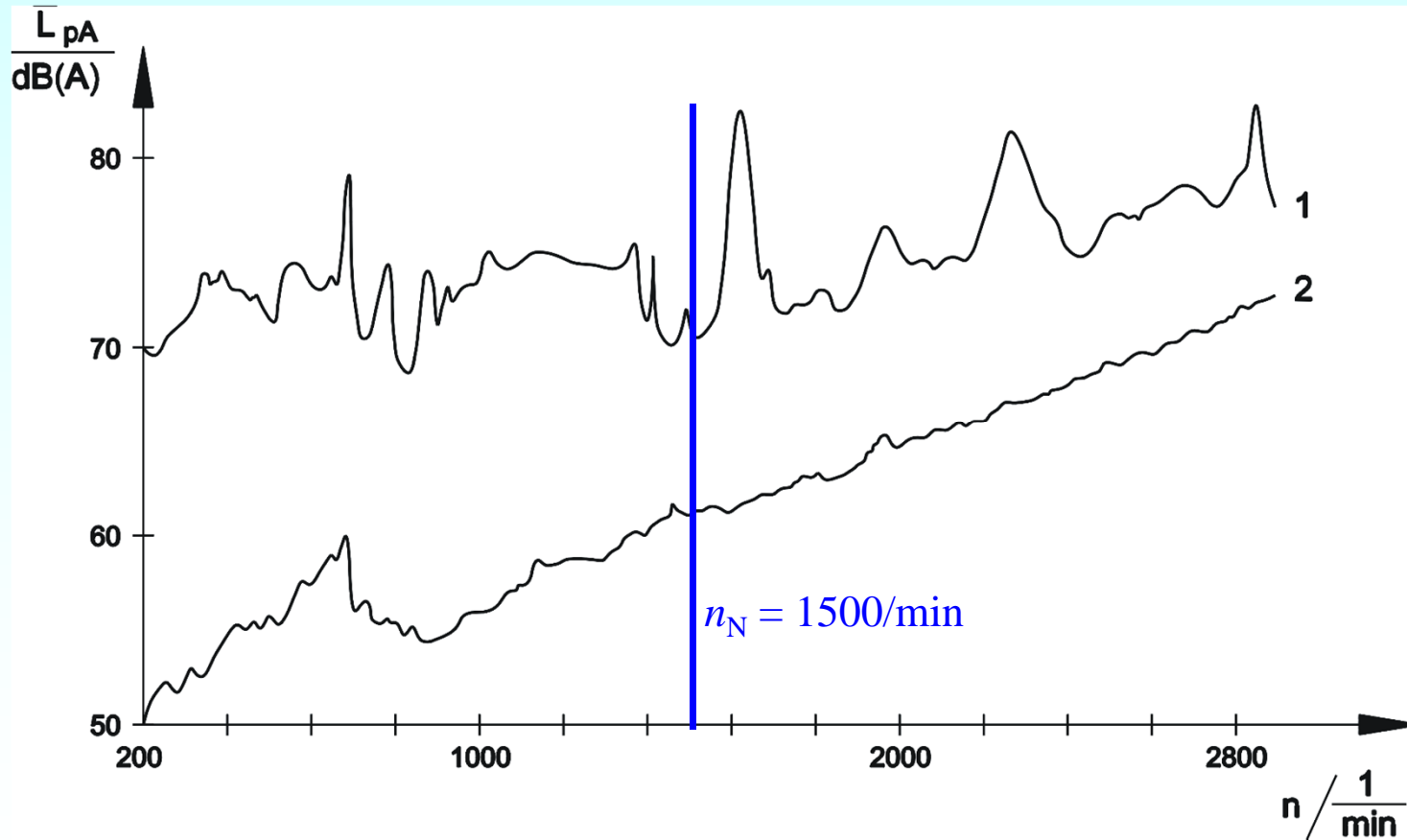


# Magnetically excited acoustic noise

Pulsating radial magnetic pull with frequency:  $f_{puls} = n \cdot Q_r \cdot m$

Pull causes radial vibrations of stator yoke and housing  $\Rightarrow$  acoustic sound.

If frequency coincides with eigen-frequency of stator yoke: **resonance** ! As stator yoke is very thin, motor "rings like a bell".



## Measured sound pressure level:

7.5 kW,  $2p = 4$ ,

$n_N = 1500$ /min

12/8 SR machine,

Operation at

1: rated current

2: no-load current.

Exciting frequency varies up to 1.2 kHz !

# Comparison of inverter fed induction and SR motor

Same rated power & speed, identical cooling = totally enclosed, fan on shaft

Data: 7.5 kW, base/top speed 1500/min / 3000/min, Th. Cl. F,  $m = 3$ ,  $2p = 4$

Thermal load run: 1500/min, 54 Nm and  $U_d = 540$  V: Result:

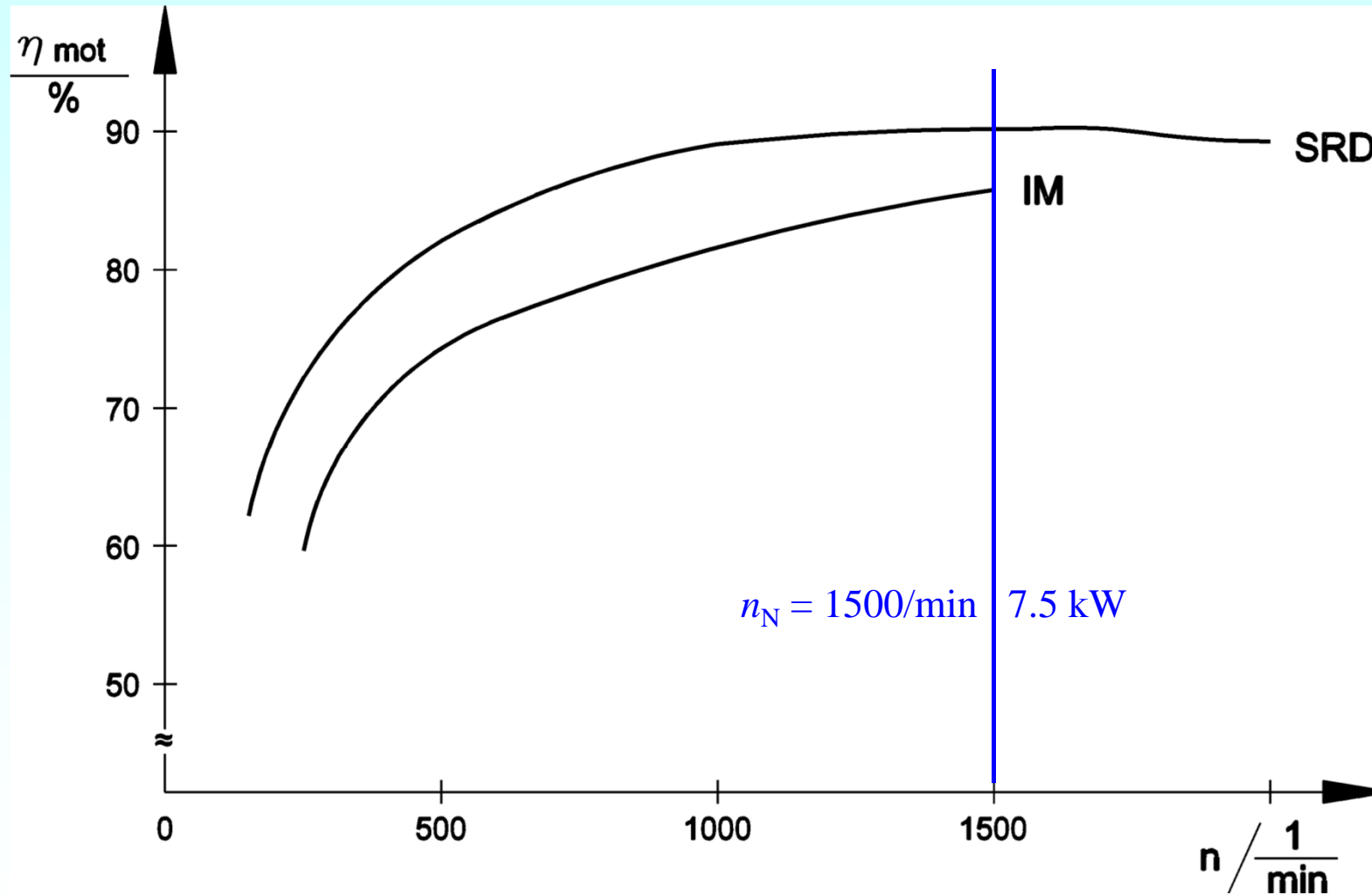
	<i>Switched Reluctance Machine</i>	<i>Induction Machine</i>
Input / Output power $P_{in} / P_{out}$	9440 W/ 8480 W	9950 W/ 8480 W
Phase current $I$ (rms)/ $\hat{I}$ (peak)	13.3 A/ 27.5 A	17.45 A/ 30 A
Stator frequency $f_s$	200 Hz	52 Hz ( $U_{s,k=1} = 225.5$ V)
Armature temperature rise	110 K	101 K
Iron losses / friction&windage losses	200 W/ 165 W	265 W/ 55 W
Stator copper losses/cage losses	595 W/ 0 W	650 W/ 350 W
Additional losses	0 W	150 W
Stator current density $J_s$	5.25 A/mm <sup>2</sup>	8.23 A/mm <sup>2</sup>
Current loading $A = 2mN_s I_s / (d_{si} \pi)$	513 A/cm	305 A/cm
Motor efficiency $\eta_{mot}$	<b>89.8 %</b>	<b>85.2 %</b>
Inverter efficiency $\eta_{inv}$	96.6 %	97.0%
Drive efficiency $\eta$	<b>86.7 %</b>	<b>82.6 %</b>



# Comparison of measured motor efficiency at 54 Nm

12/8 SR machine (SRD) / inverter-fed standard induction machine (IM)

Four-pole, 3-phase: at 54 Nm, 100 K armature temperature rise



# Applications of SR drives

## Example:

### Starter-generator for military aircraft jet (US Air Force, manufacturer GE)

- Rated power 250 kW, rated speed 13 500/min, rated torque 177 Nm, rated current 750 A, DC link voltage 270 V
- Maximum speed 22200/min, over-speed 26000/min, overall system efficiency: 90%
- Three phase four pole 12/8 SR machine !

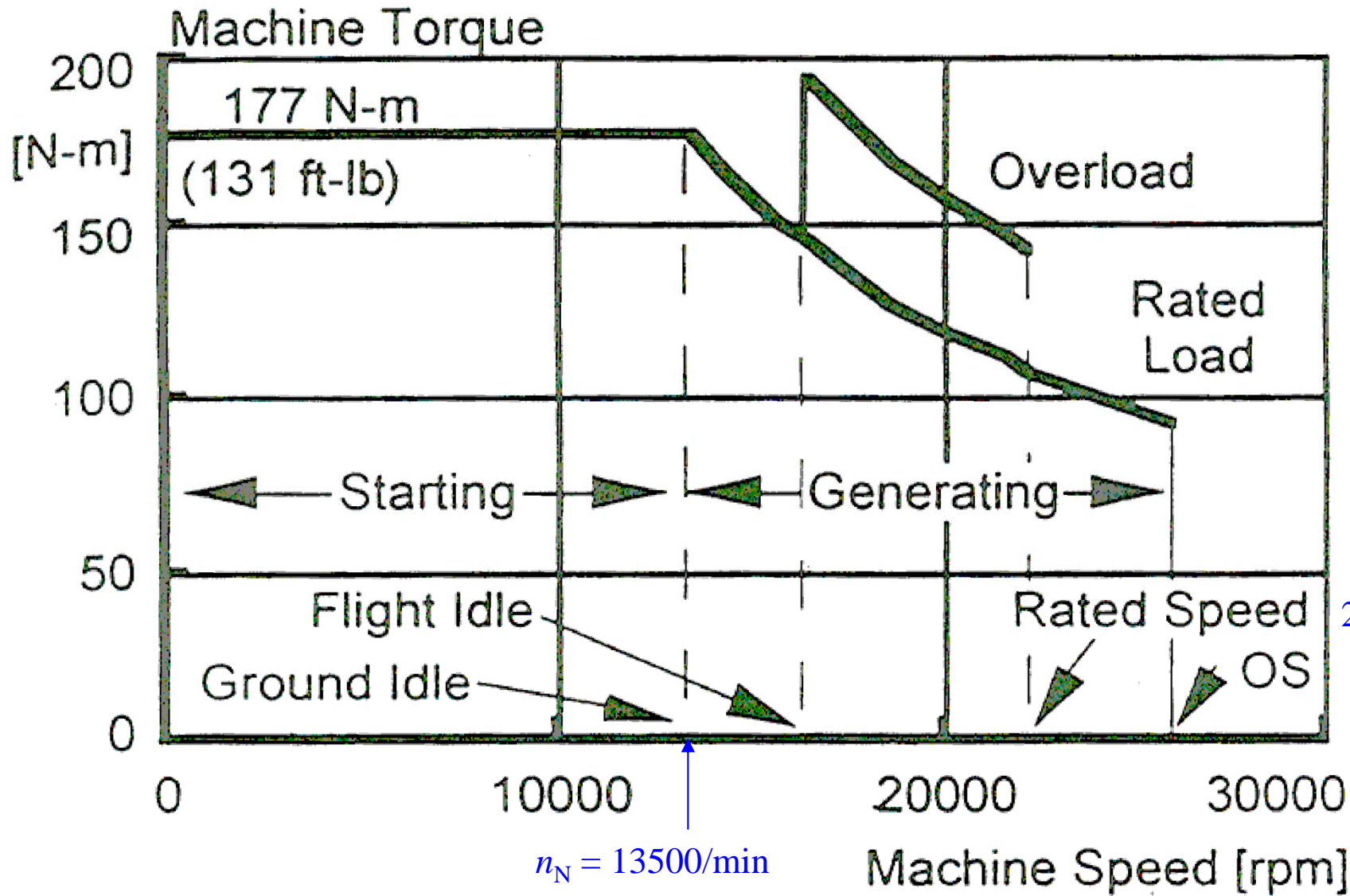
**Reliability:** Two independent three phase systems: each 125 kW power. In case of failure motor is "fail-silent" = no current = no force = no induced voltage, so risk of fire due to short circuit is minimized.

**Small motor size:** Motor is *intensively cooled by oil and high speed*. Motor mass is only 70 kg, yielding "power weight" of  $P/m = 3.6$  kW/kg.

**Low speed range 0 ... 13500/min:** SR machine starts compressor of air craft engine with constant torque 177 Nm.

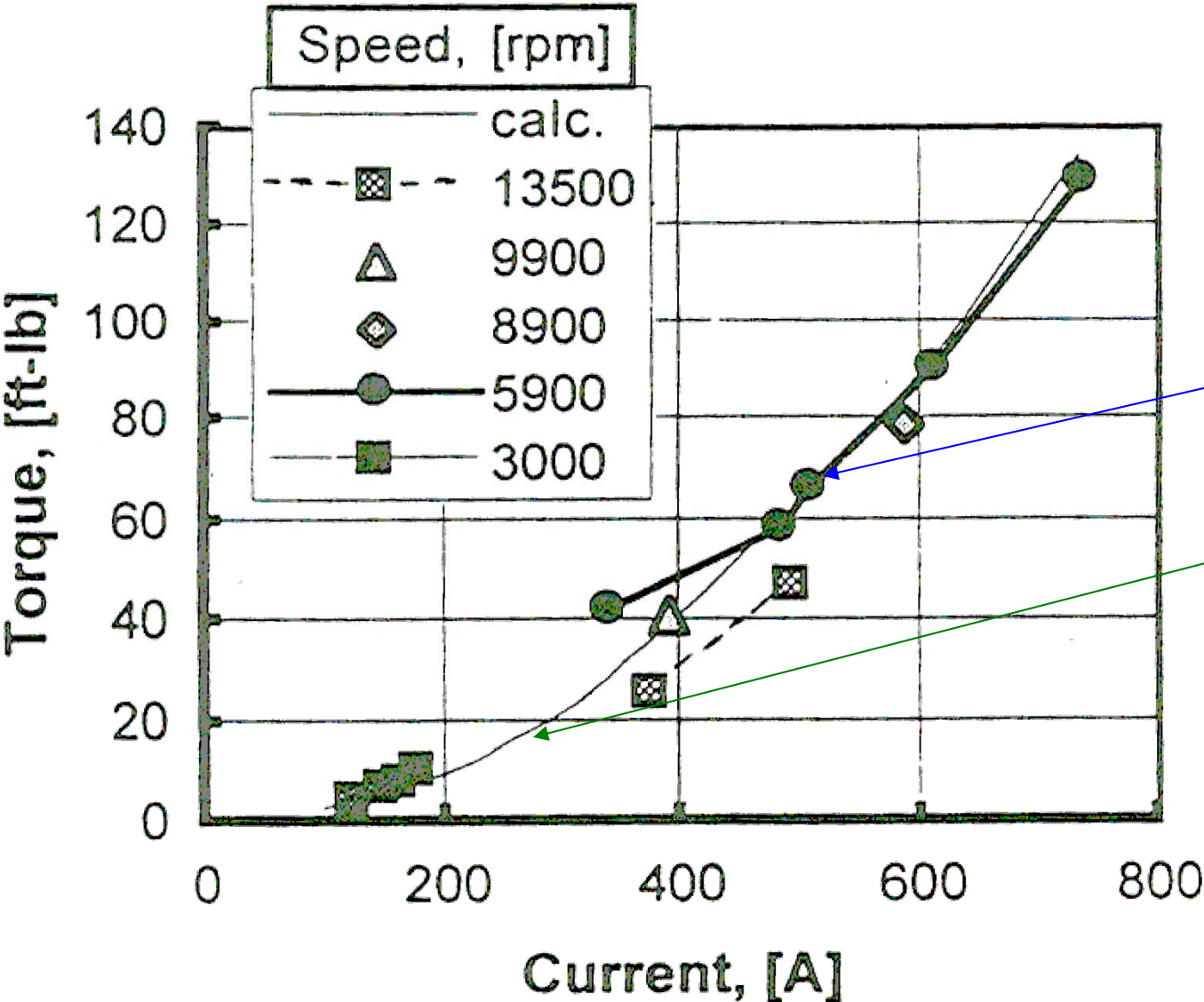
**High speed range 13500 ... 26000/min:** SR machine is generator at 250 kW.

# Torque-speed curve of aircraft starter generator



Source:  
General Electric,  
Cincinnati, USA

# Torque-current curve of aircraft starter generator



Source:  
General Electric,  
Cincinnati, USA



# Surface cooled switched reluctance machine

Three phases

Four poles

$Q_s = 12$ ,  $Q_r = 8$

Cooling fins on housing

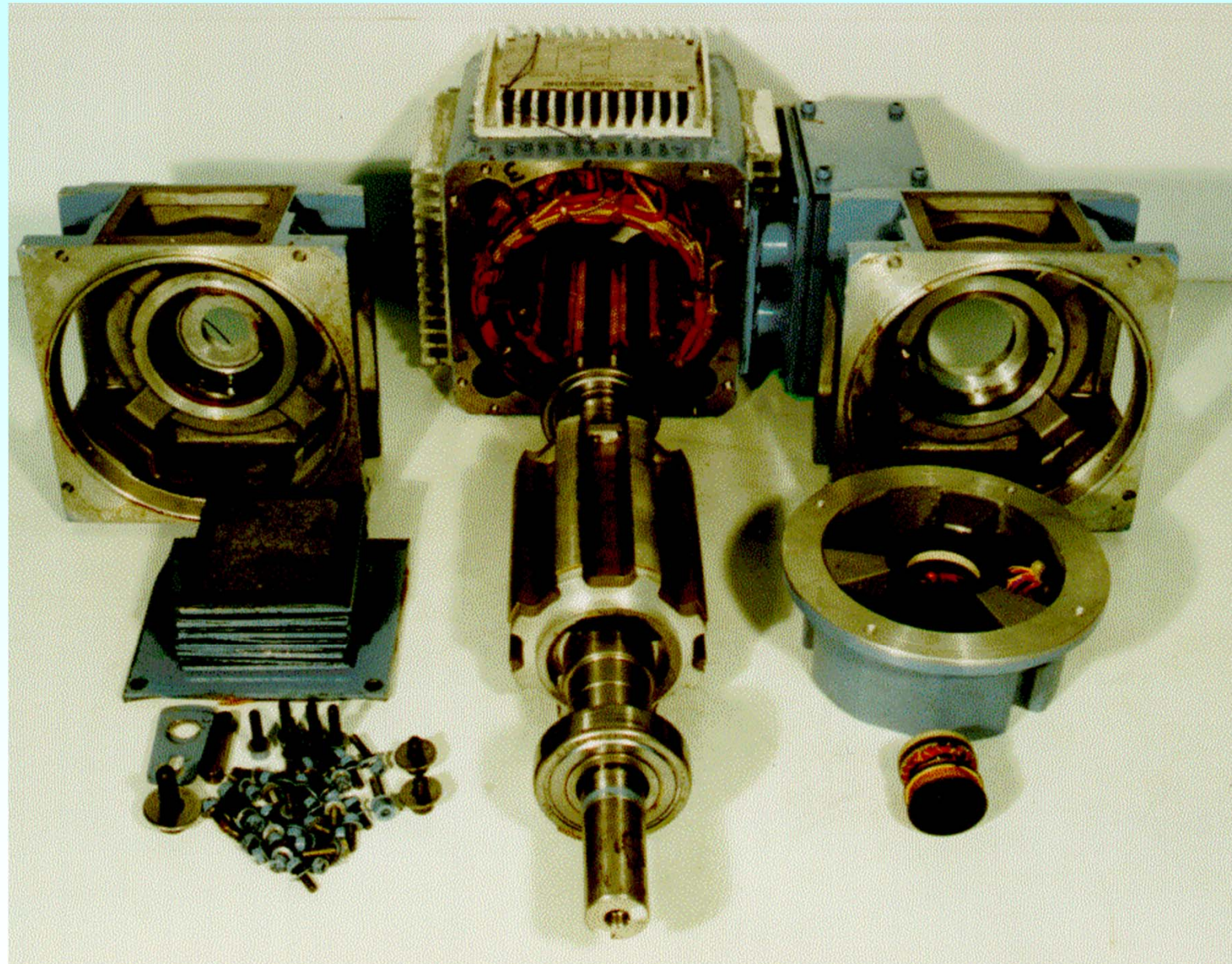
Resolver for position encoding

Rated speed:  
1500/min

Maximum speed:  
6000/min

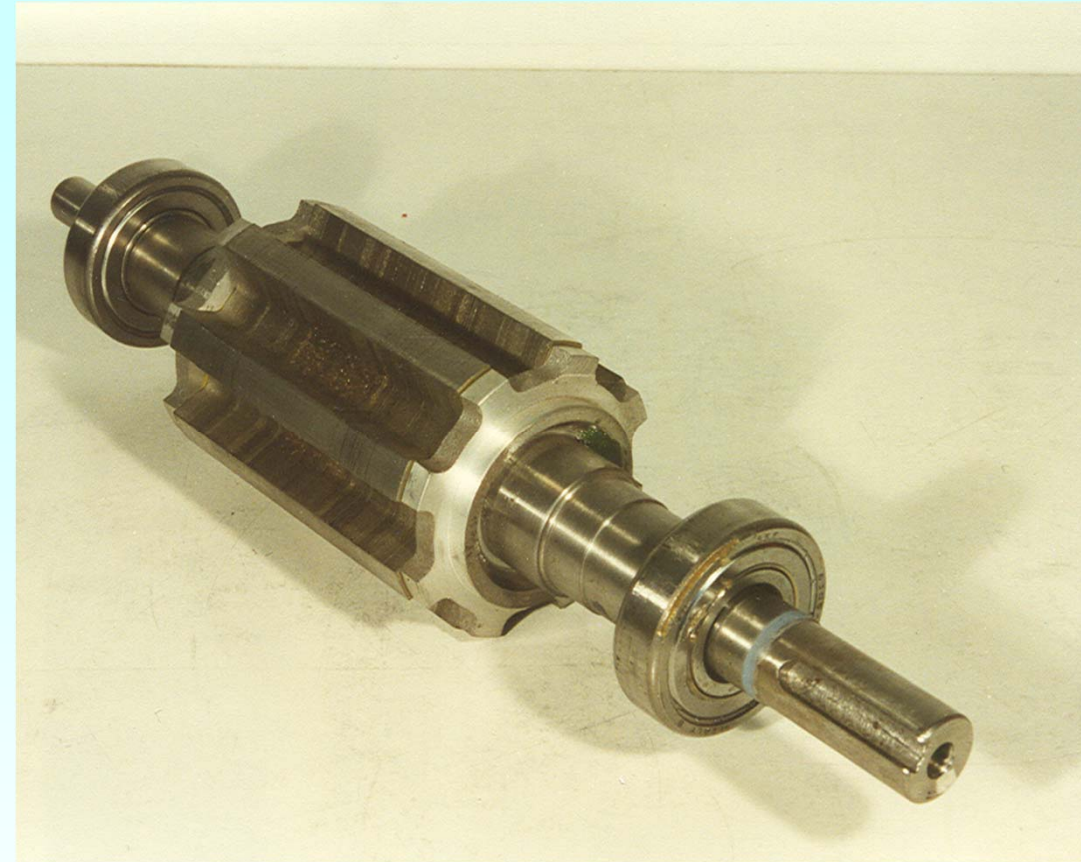
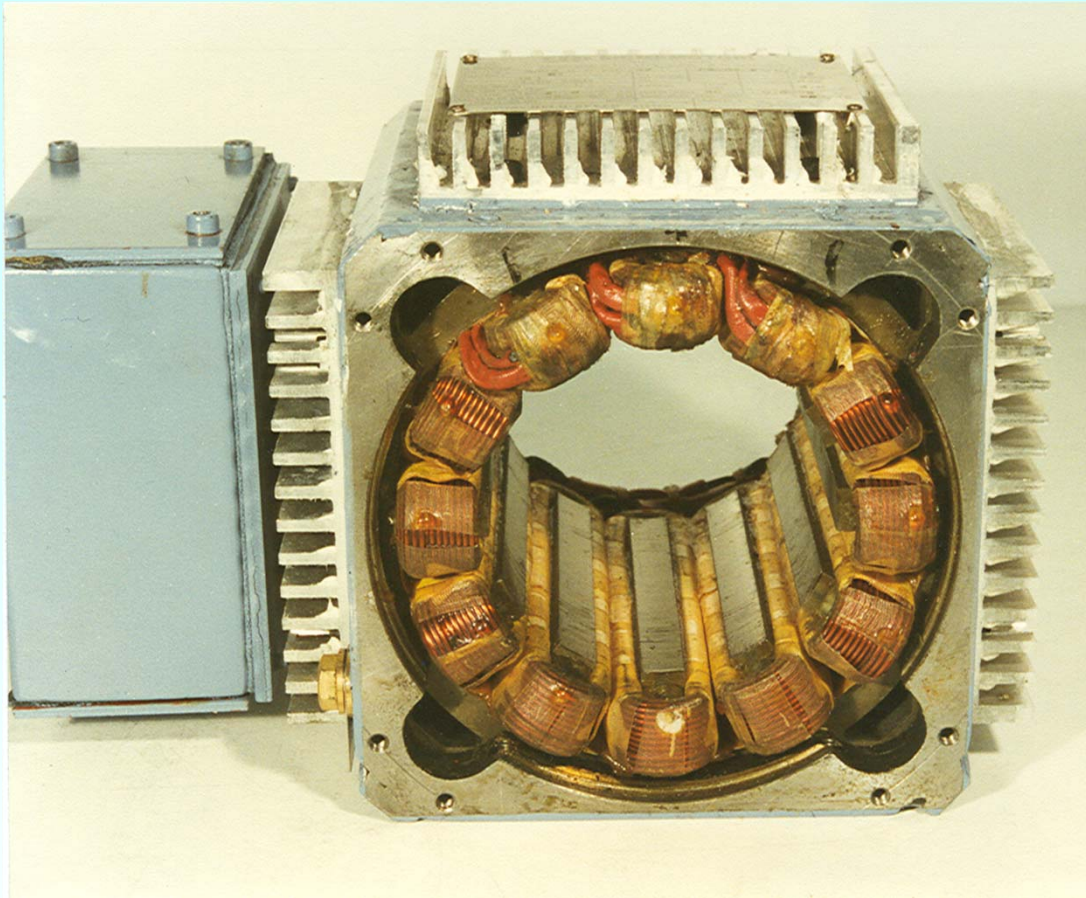
Source:

SICME, Italy





# Stator and rotor of switched reluctance machine



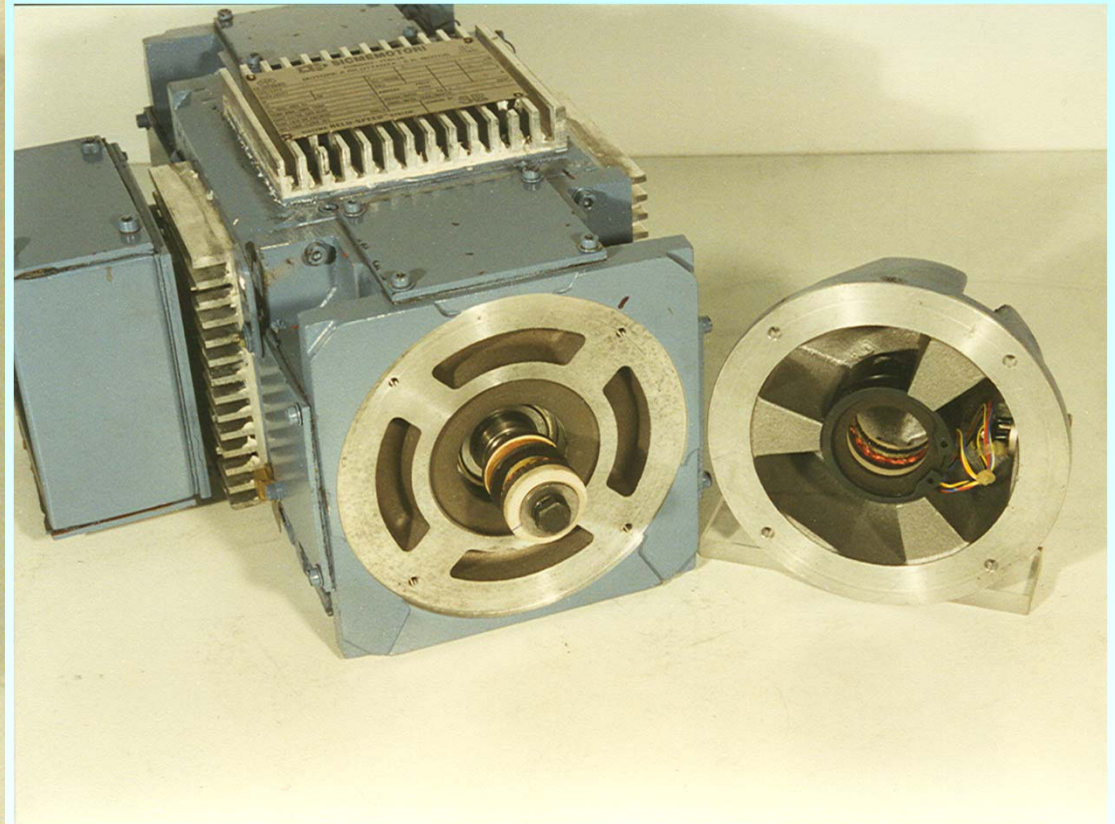
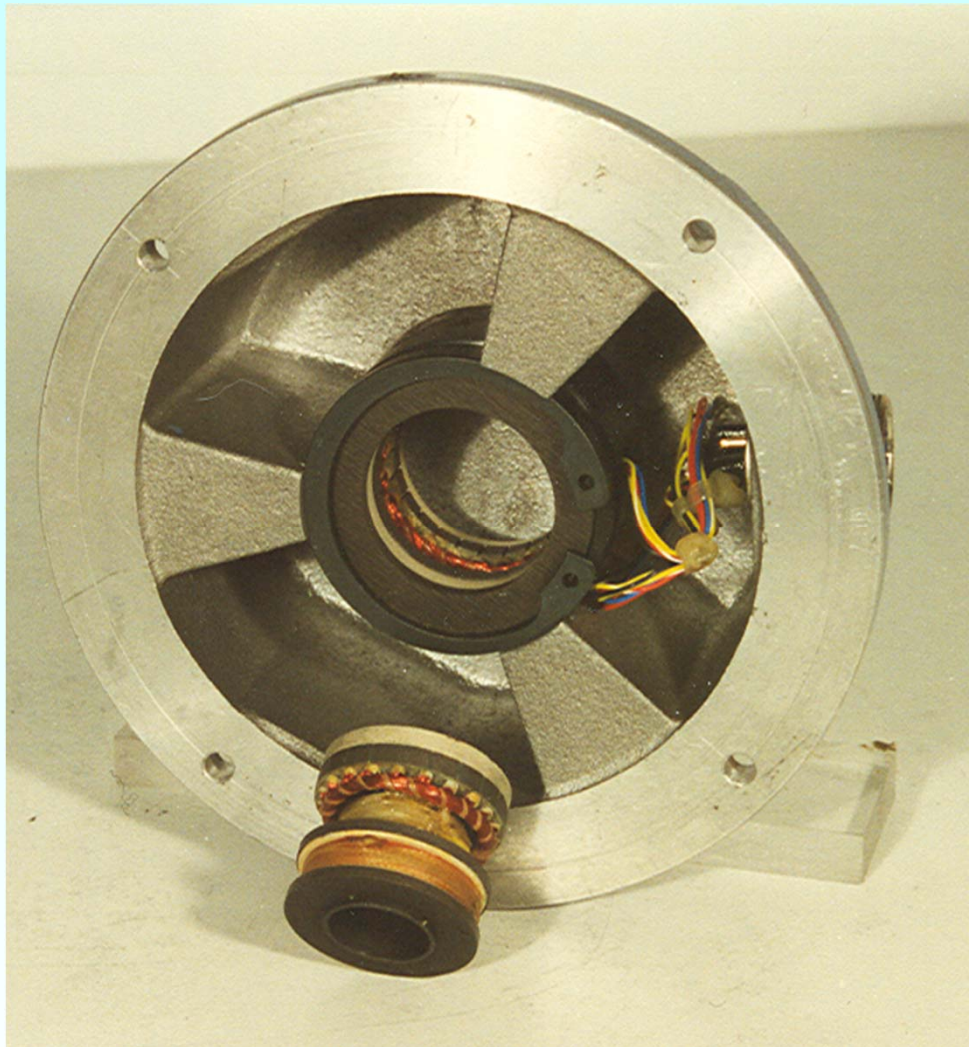
Three phases, four poles,  $Q_s = 12$ ,  $Q_r = 8$

Rated speed: 1500/min, maximum speed: 6000/min

Source:  
SICME, Italy



# Resolver for switched reluctance machine

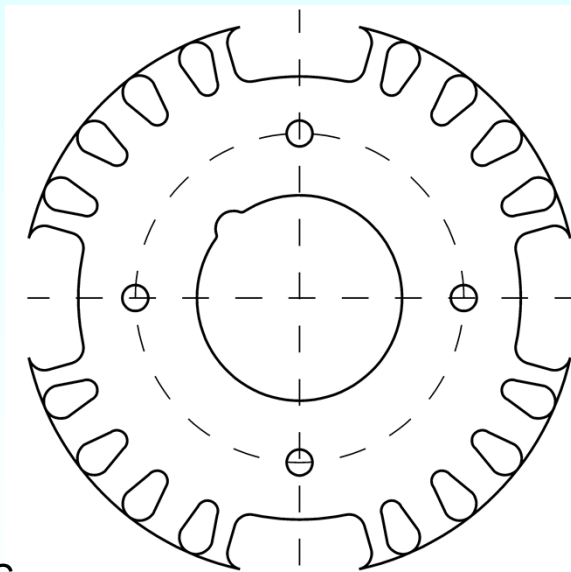


Source:  
SICME, Italy

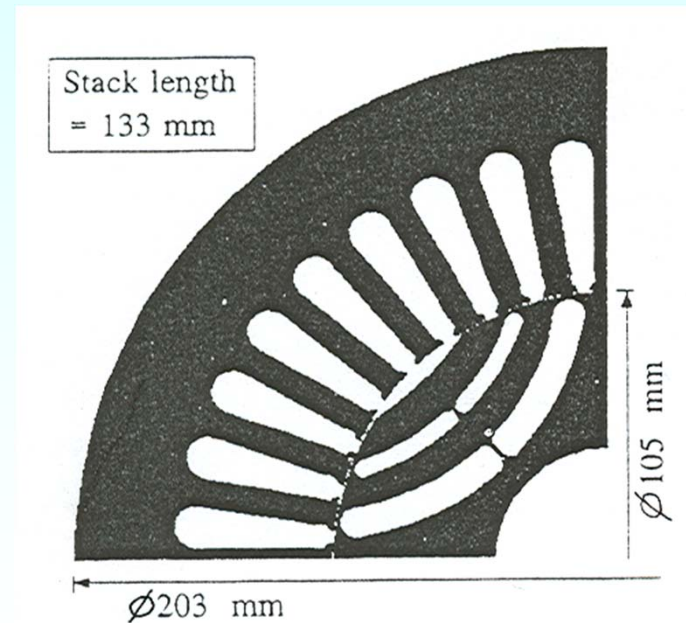


## 2. Reluctance machines

### 2.2 Synchronous reluctance machines



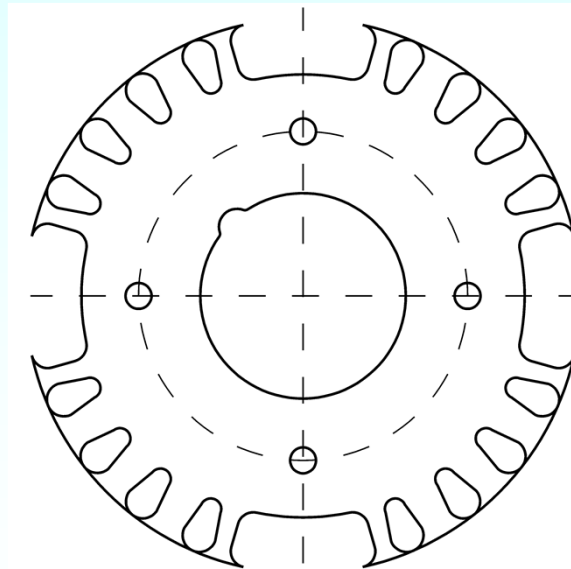
Source: Siemens AG.  
Germany



Source: M. Kamper,  
WCRR Conf, 1997

## 2. Reluctance machines

### 2.2.1 Line-starting synchronous reluctance machines

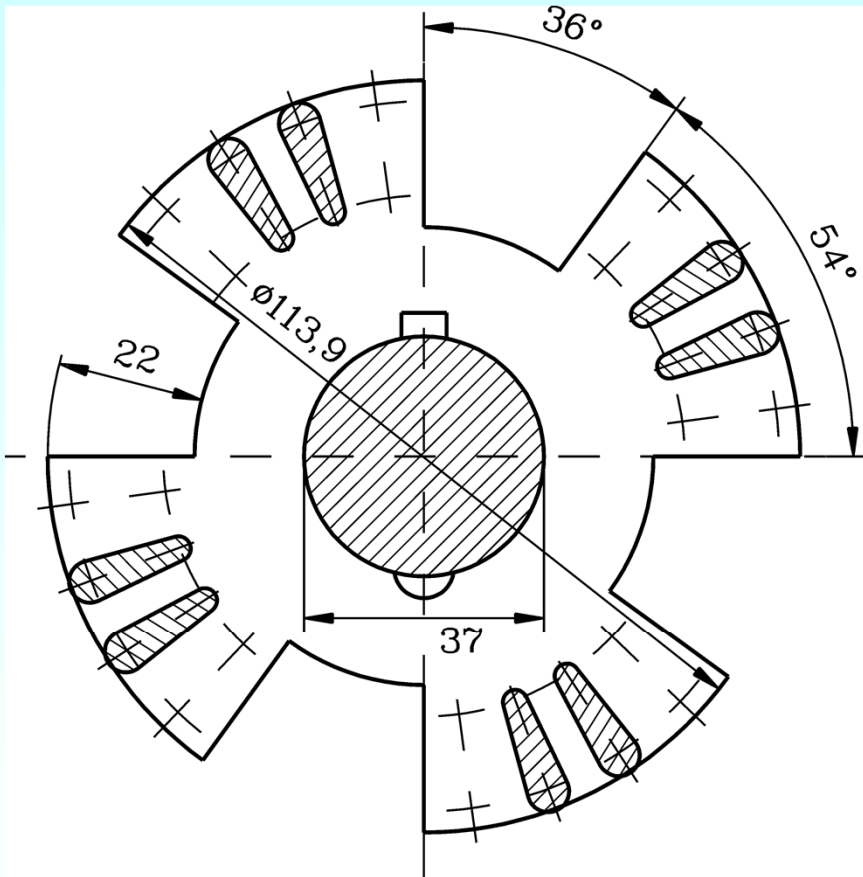


Source: Siemens AG.  
Germany

# 4-pole rotors of synchronous reluctance machines

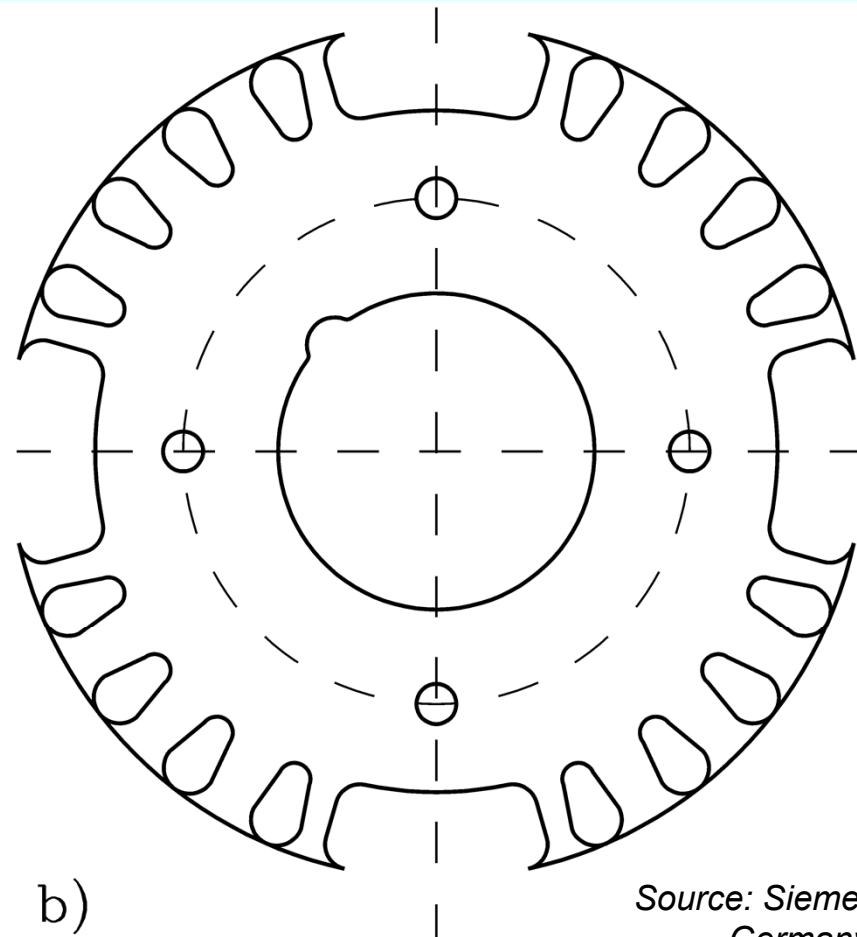
a) 2.2 kW, shaft height 112 mm

b) 550 W, shaft height 80 mm



a)

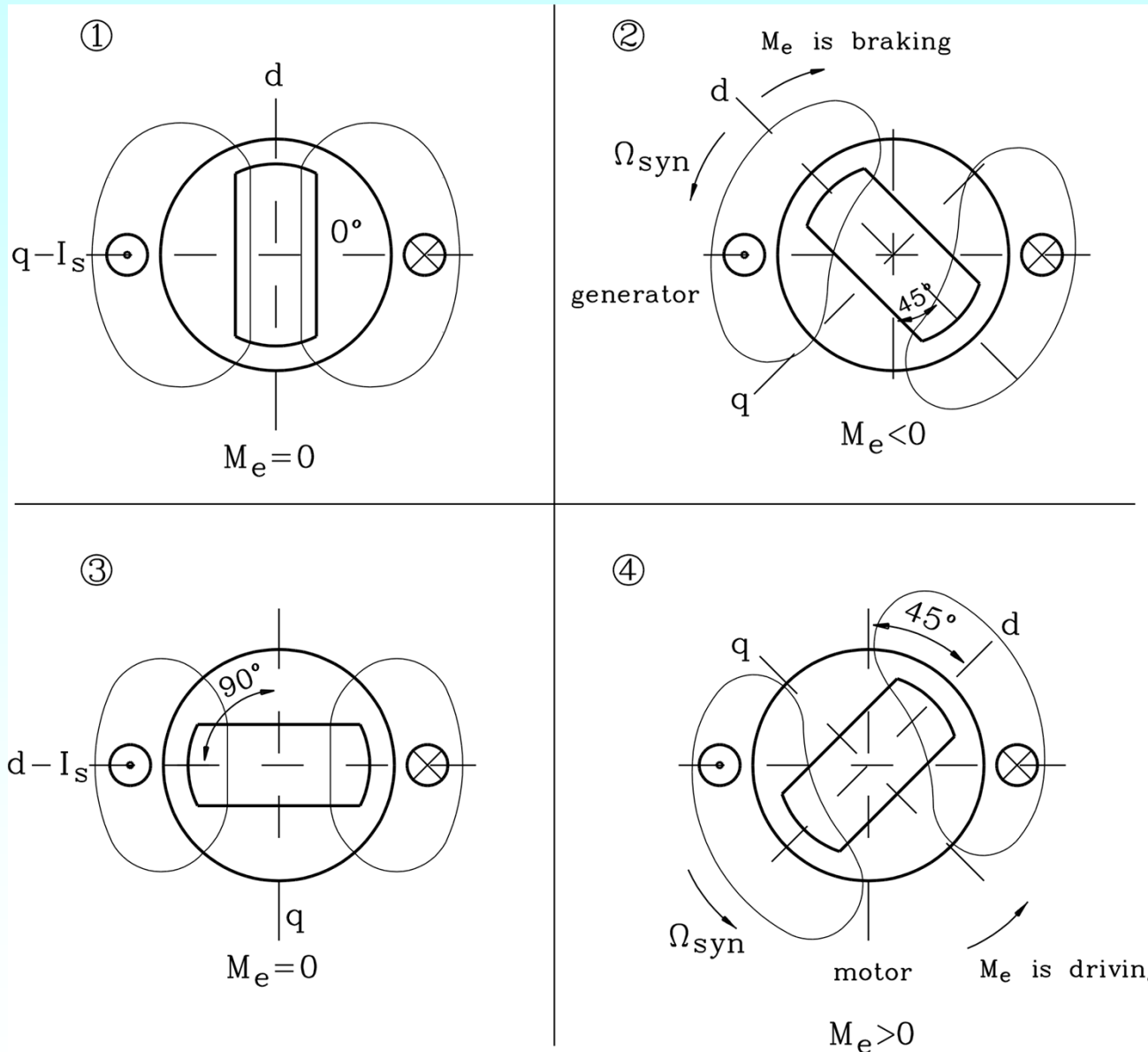
Source: A. Schmidt, TU  
Wien, 1988



b)

Source: Siemens AG.  
Germany

# Basic function of synchronous reluctance machine



Stator three phase winding operated at AC voltage system to generate **rotating stator field** with stator frequency  $f_s$ .

Rotor has **variable air-gap**:

small (**d-axis**): inductance  $L_d$

big (**q-axis**): inductance  $L_q$

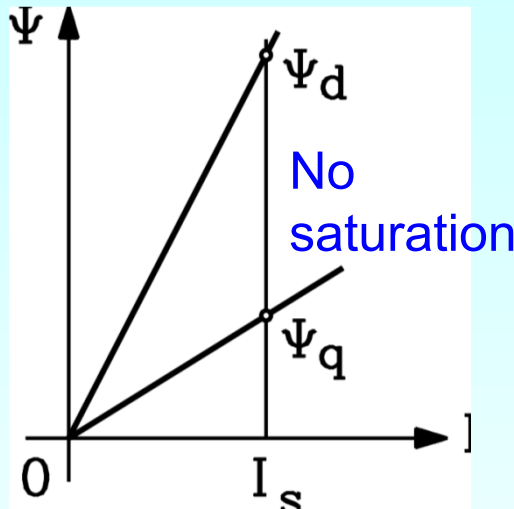
Air gap field tries to align rotor by tangential magnetic pull = reluctance torque.

Rotor rotates **synchronously** with stator field:  $n = f_s/p$ .

**Pull-out**: at load angle  $45^\circ$

# Air gap flux linkage in $d$ - and $q$ -axis

$$\underline{\Psi}_{hd} = L_{hd} \cdot \underline{I}_d \cdot \sqrt{2} \quad \underline{\Psi}_{hq} = L_{hq} \cdot \underline{I}_q \cdot \sqrt{2} \quad \Rightarrow \quad \underline{\Psi}_h = \underline{\Psi}_{hd} + \underline{\Psi}_{hq}$$



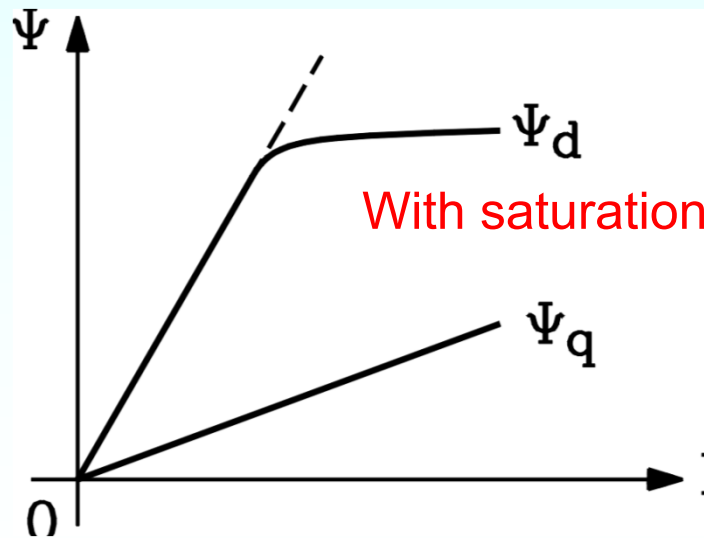
At  $R_s = 0$ :  $\underline{I}_s = I_d + jI_q = \underline{I}_d + \underline{I}_q$

$$\underline{U}_s = jX_d \underline{I}_d + jX_q \underline{I}_q = jX_d I_d - X_q I_q$$

Power balance:

$$P_e = m \cdot U_s \cdot I_s \cdot \cos \varphi = m \cdot (U_{s,Re} \cdot I_{s,Re} + U_{s,Im} \cdot I_{s,Im}) =$$

$$= m \cdot (-X_q I_d I_q + X_d I_d I_q) = \Omega_m M_e$$



Torque equation:

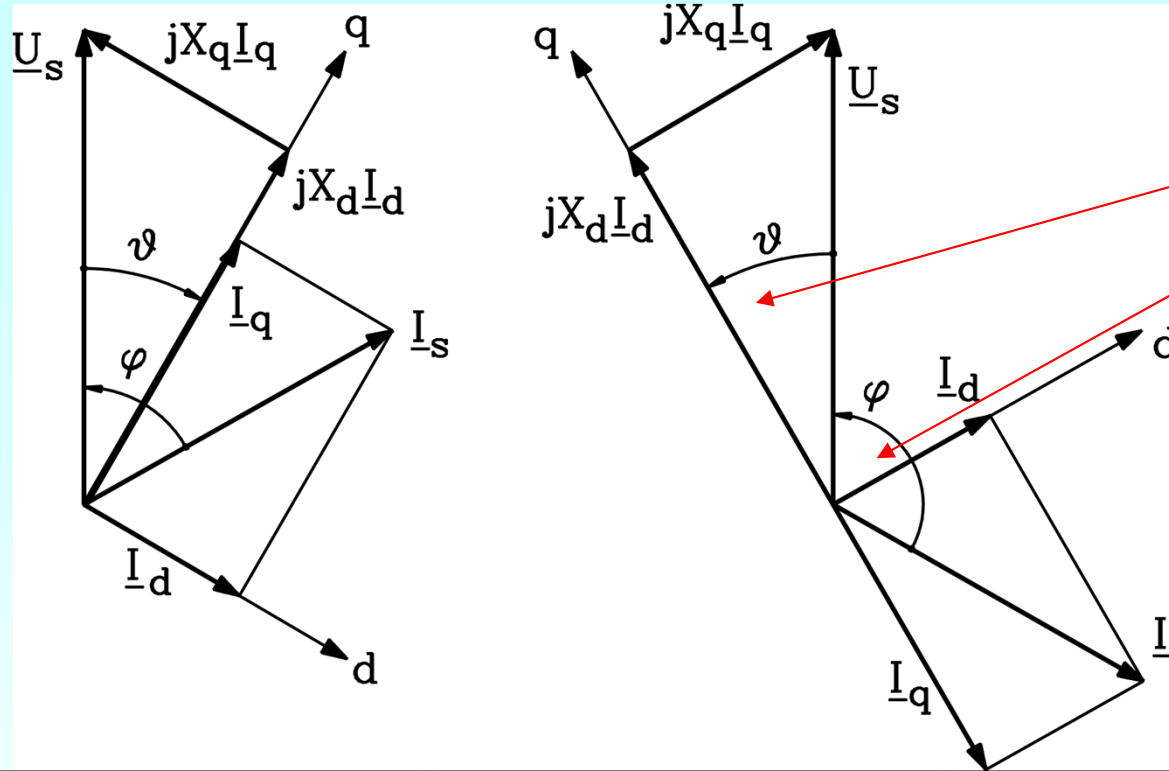
$$M_e = \frac{p \cdot m}{\omega_s} \cdot (X_d - X_q) \cdot I_d I_q$$

*Big difference between  $d$ - and  $q$ -axis inductance is needed : typically  $L_d/L_q \sim 5$ .*

*$I_d$  : "magnetizing" current: "main" flux  $d$ -axis*

*$I_q$  : torque-delivering current*

# Synchronous reluctance motor / generator ( $R_s = 0$ )



Load angle

Phase angle

Machine is always inductive consumer !

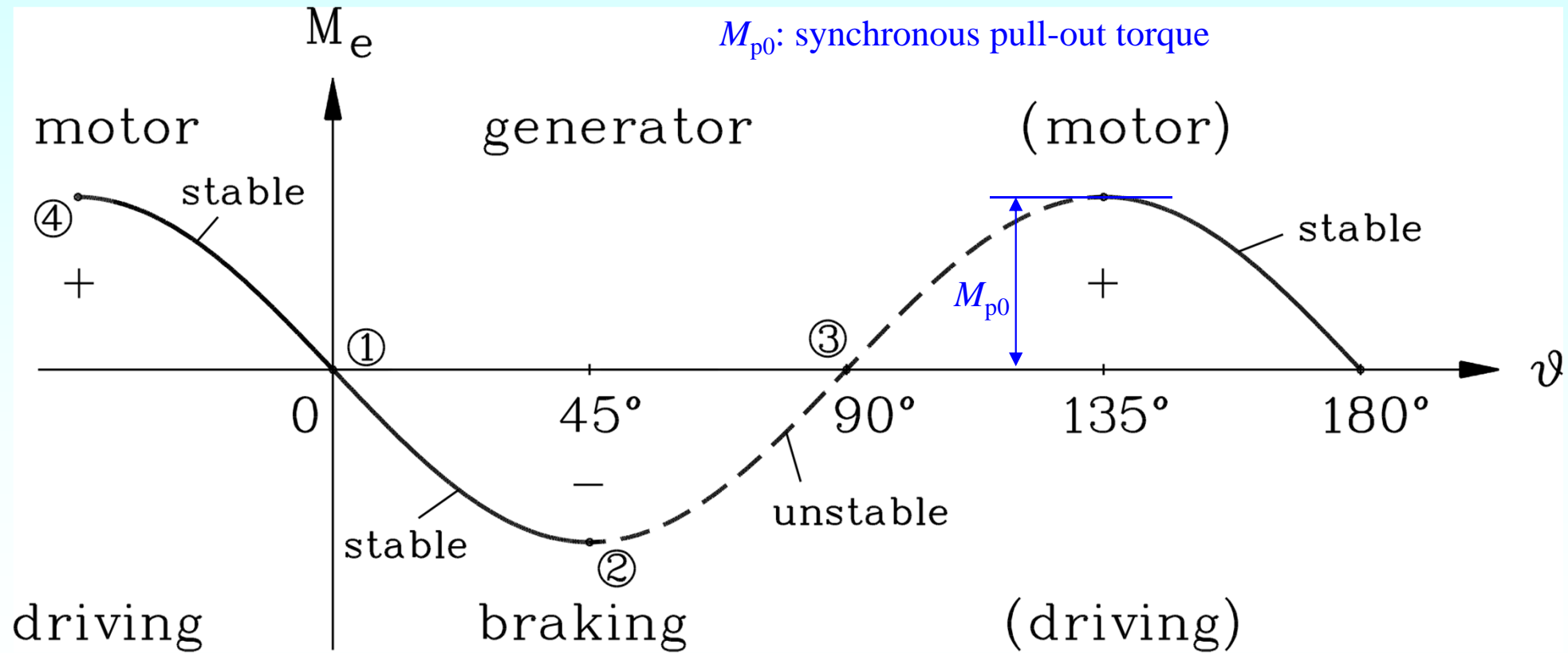
	Motor	Generator
Load angle $\vartheta$	$< 0$	$> 0$
Phase shift $\varphi$	$0 \dots 90^\circ$	$90^\circ \dots 180^\circ$
$d$ -current	$> 0$	$> 0$
$q$ -current	$> 0$	$< 0$
Electric power	$> 0$	$< 0$

# Operation at constant stator voltage amplitude

For  $R_s = 0$ : With  $U_s \cos \vartheta = I_d X_d$ ,  $-U_s \sin \vartheta = I_q X_q$  we get:

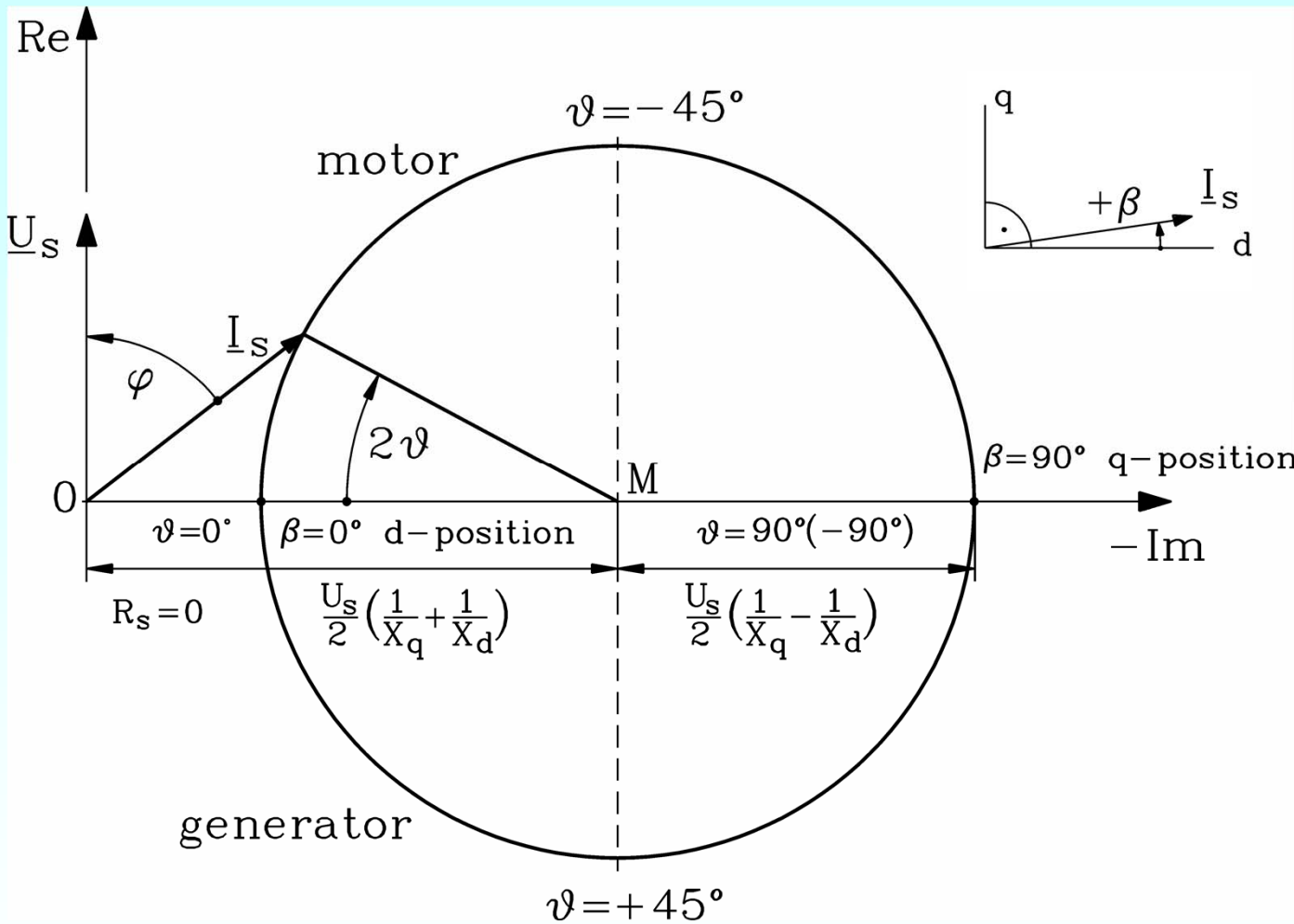
Torque, depending on voltage:

$$M_e = -\frac{p \cdot m}{\omega_s} \cdot \frac{U_s^2}{2} \cdot \left( \frac{1}{X_q} - \frac{1}{X_d} \right) \cdot \sin(2\vartheta)$$





# Current root locus at constant voltage ( $R_s = 0$ )



Circle diagram of reluctance machine („reluctance circle“)

Minimum current at no-load (d-current)  $I_{s0} = U_s/X_d$

At +/-45° load angle: Maximum torque

Increase of current beyond 45°, but UNSTABLE operation.

Maximum current at load angle 90°:  $I_{s,max} = U_s/X_q$ . Periodicity with 90°.

Current always lagging = machine is always inductive consumer !

$$M_e \sim U_s I_s \cos \varphi = -U_s \cdot \frac{U_s}{2} \cdot \left( \frac{1}{X_q} - \frac{1}{X_d} \right) \cdot \sin \vartheta$$



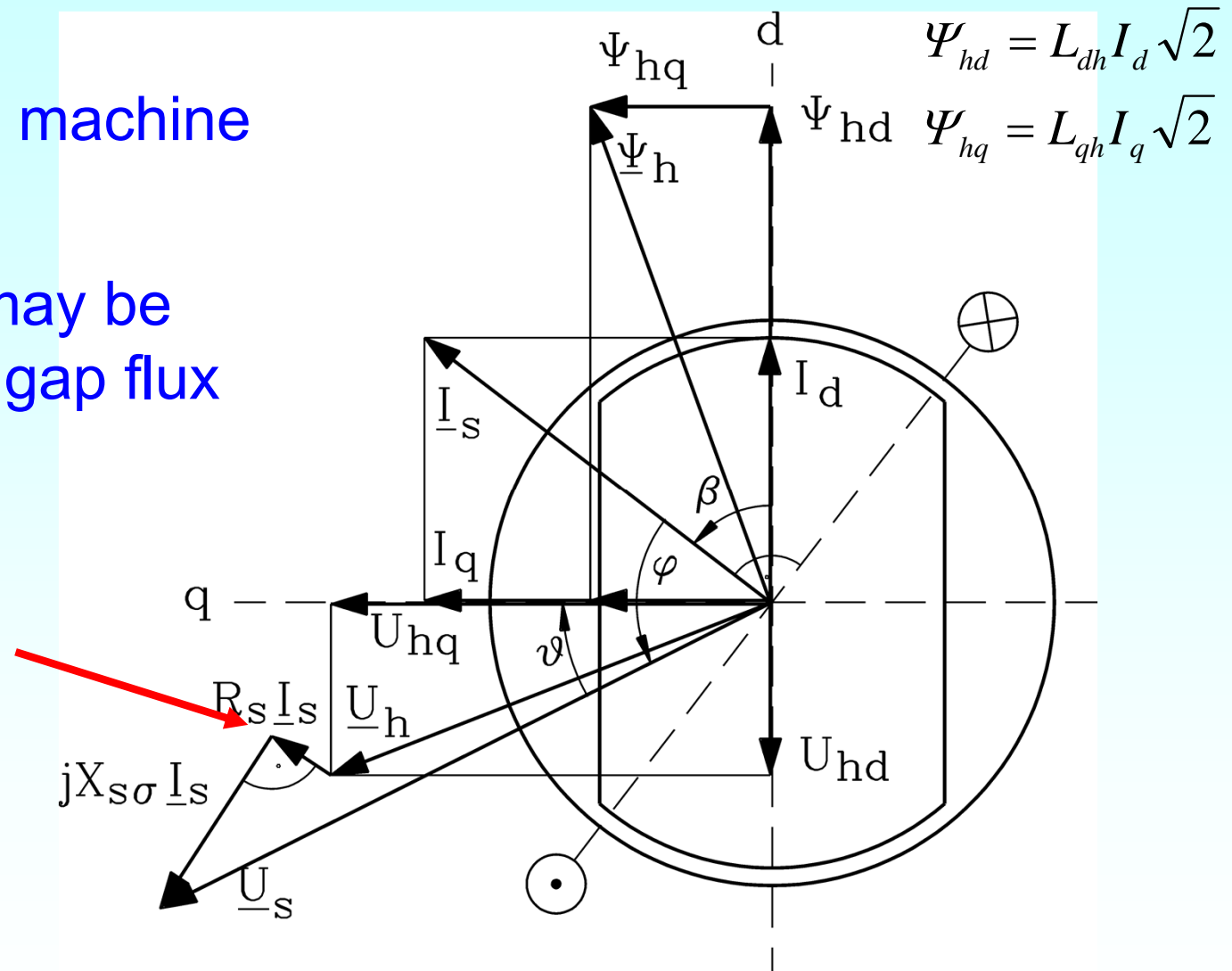
# Phasor diagram including stator resistive voltage drop

- Phasor diagram for synchronous reluctance machine for motor operation.

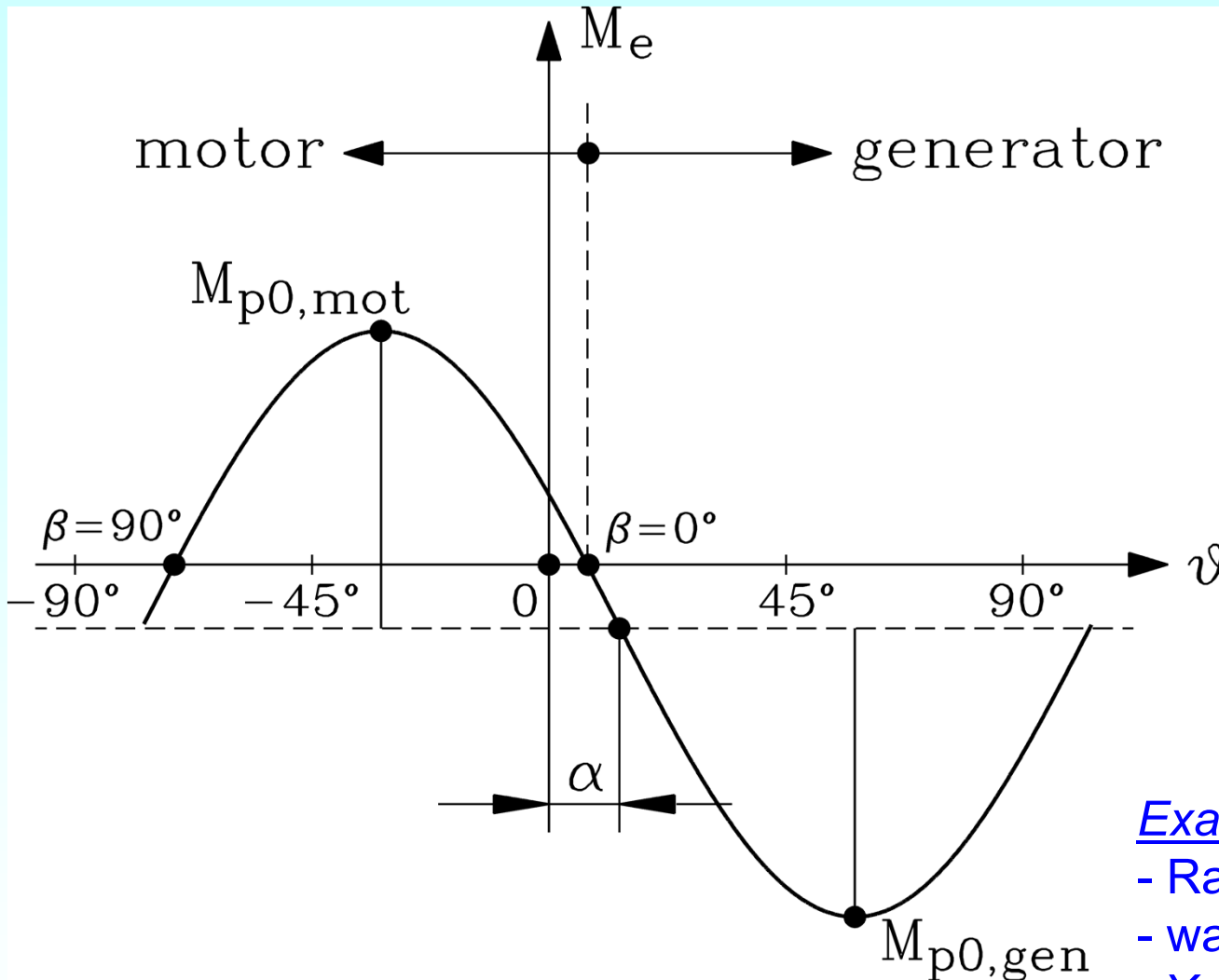
- Flux linkage phasors may be taken as direction of air gap flux components.

**Influence of stator resistance especially for these rather small machines considerable !**

$$X_d = X_{dh} + X_{s\sigma} \quad X_q = X_{qh} + X_{s\sigma}$$



# Torque over load angle for $R_s > 0$



- Torque curve shifted by angle  $\alpha$
- Motor pull out torque reduced
- Generator pull out torque increased

$$2\alpha = \arctan\left(\frac{R_s(X_d + X_q)}{X_d X_q - R_s^2}\right) > 0$$

Example: 2.2 kW, 380 V, 50 Hz,  $2p = 4$ :

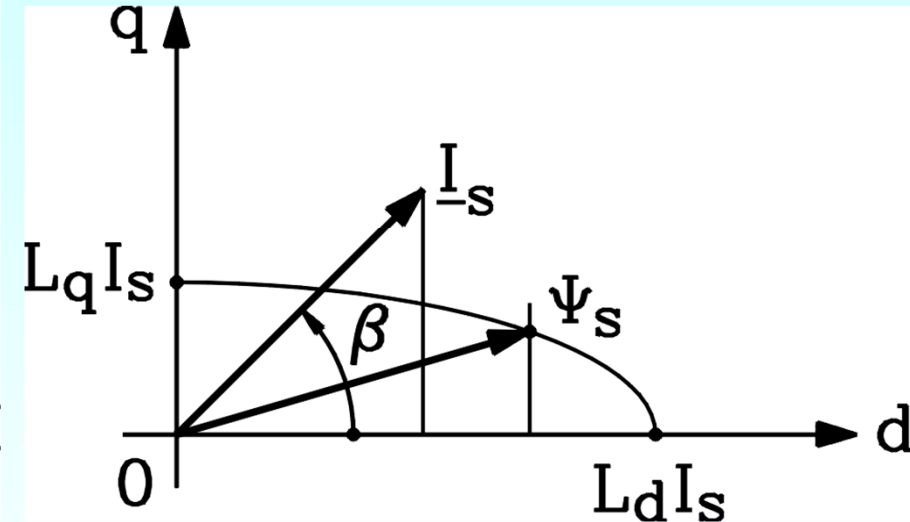
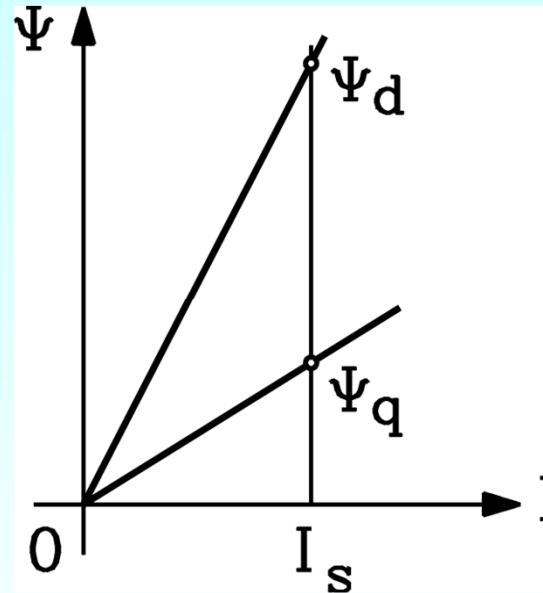
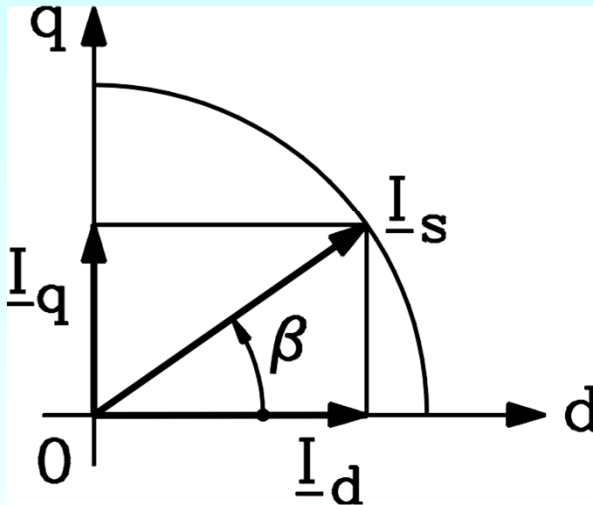
- Rated impedance:  $Z_N = U_N/I_N = 24.4 \Omega$
- warm stator phase resistance:  $R_s/Z_N = 5\%$
- $X_d/Z_N = 165\%$ ,  $X_q/Z_N = 33\%$
- Thus we get:  $2\alpha = 10.3^\circ$



# Influence of saliency at current control

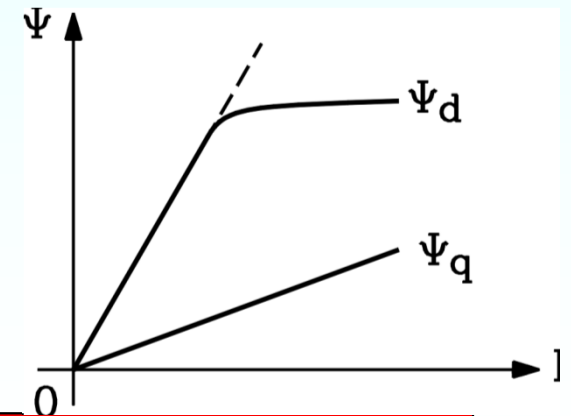
*No saturation:*

**Inverter current control:** If current phasor is shifted by angle  $\beta$  from  $d$ -axis with constant amplitude: current locus is circle, BUT flux linkage locus  $\Psi_s(\beta)$  is ELLIPSE.



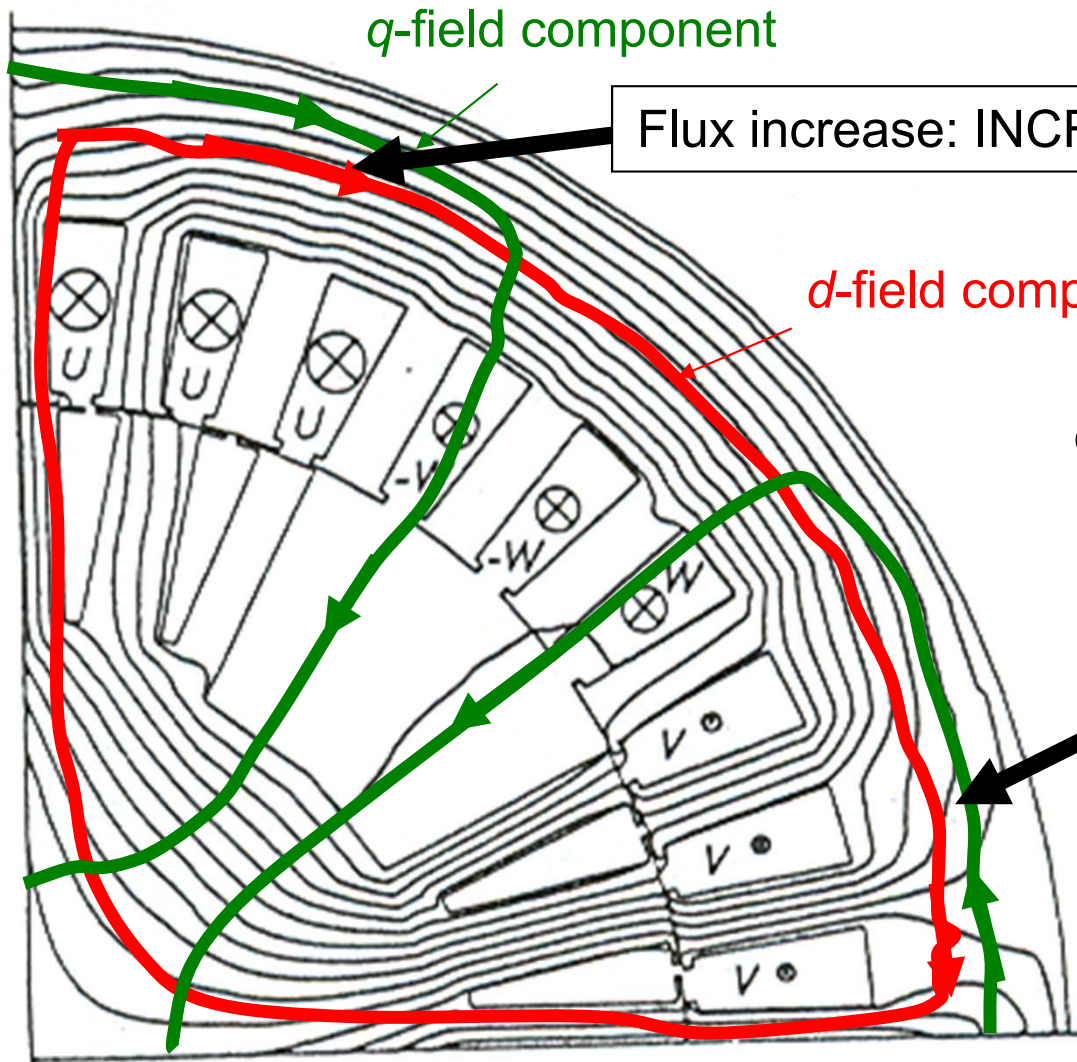
*With saturation (mainly in  $d$ -axis):*

Flux linkage locus  $\Psi_s(\beta)$  is no longer an ELLIPSE, but has to be calculated **step-by-step with numerical field analysis.**



# Increased saturation due to “cross-coupling” between $d$ - and $q$ -axis magnetic field

Example:  $\beta = 45^\circ: I_d = I_q$



Flux increase: INCREASED saturation

$d$ -field component

Increased saturation stronger than decreased saturation, which leads to a resultant flux reduction (FLUX LOSS). It must be calculated by intermediate rotor positions between  $d$ - and  $q$ -axis.

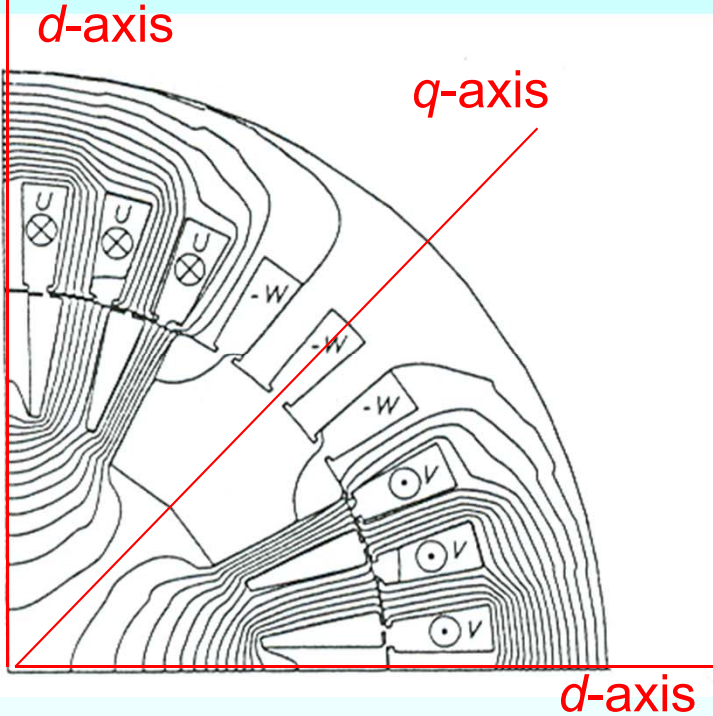
Flux decrease: DECREASED saturation

Influence of  $d$ -field on  $q$ -field and vice versa is called “magnetic coupling” of  $d$ - and  $q$ -axis!



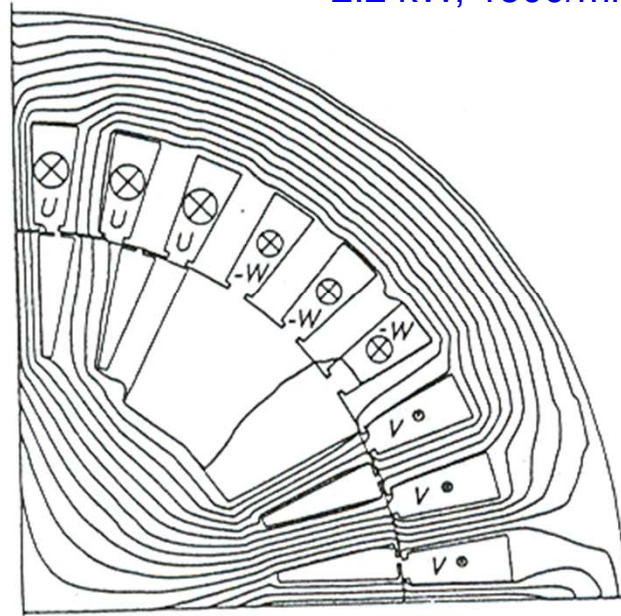
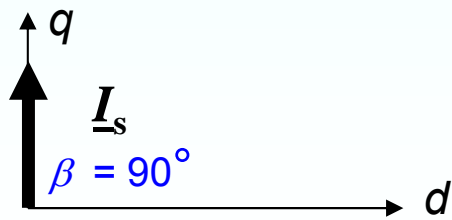
# 4-pole machine: Numerically calculated flux lines

Example: Rated voltage and current:  $U_N = 380 \text{ V}$ , Y,  $I_N = 9 \text{ A}$ , 50 Hz  
2.2 kW, 1500/min, frame size 112 mm, pole count  $2p = 4$



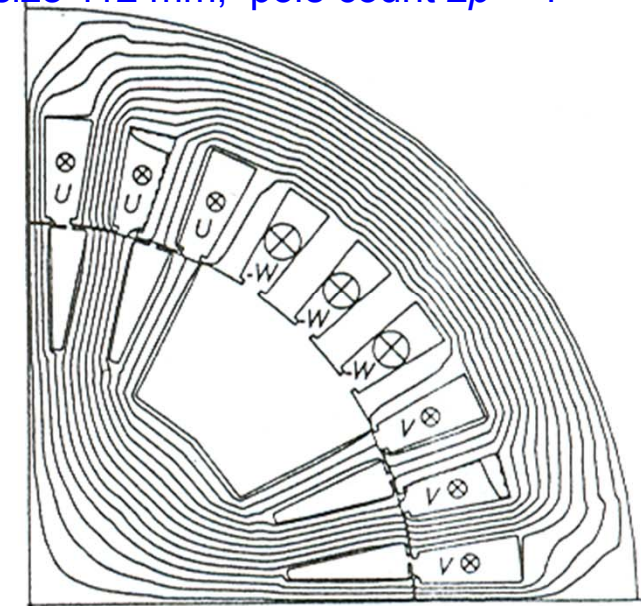
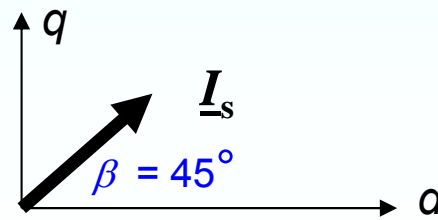
Rotor in  $q$ -position

Current angle:  $\beta = 90^\circ$



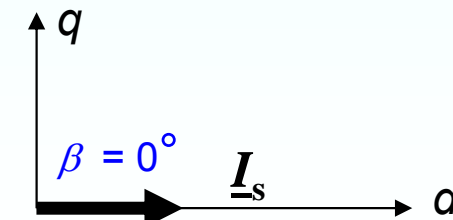
Rotor half between  $q$ - and  $d$ -position

$\beta = 45^\circ$



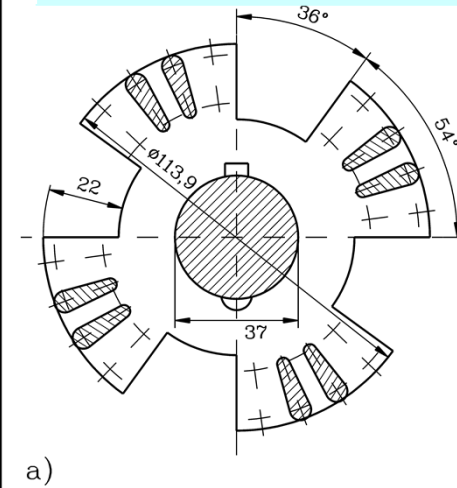
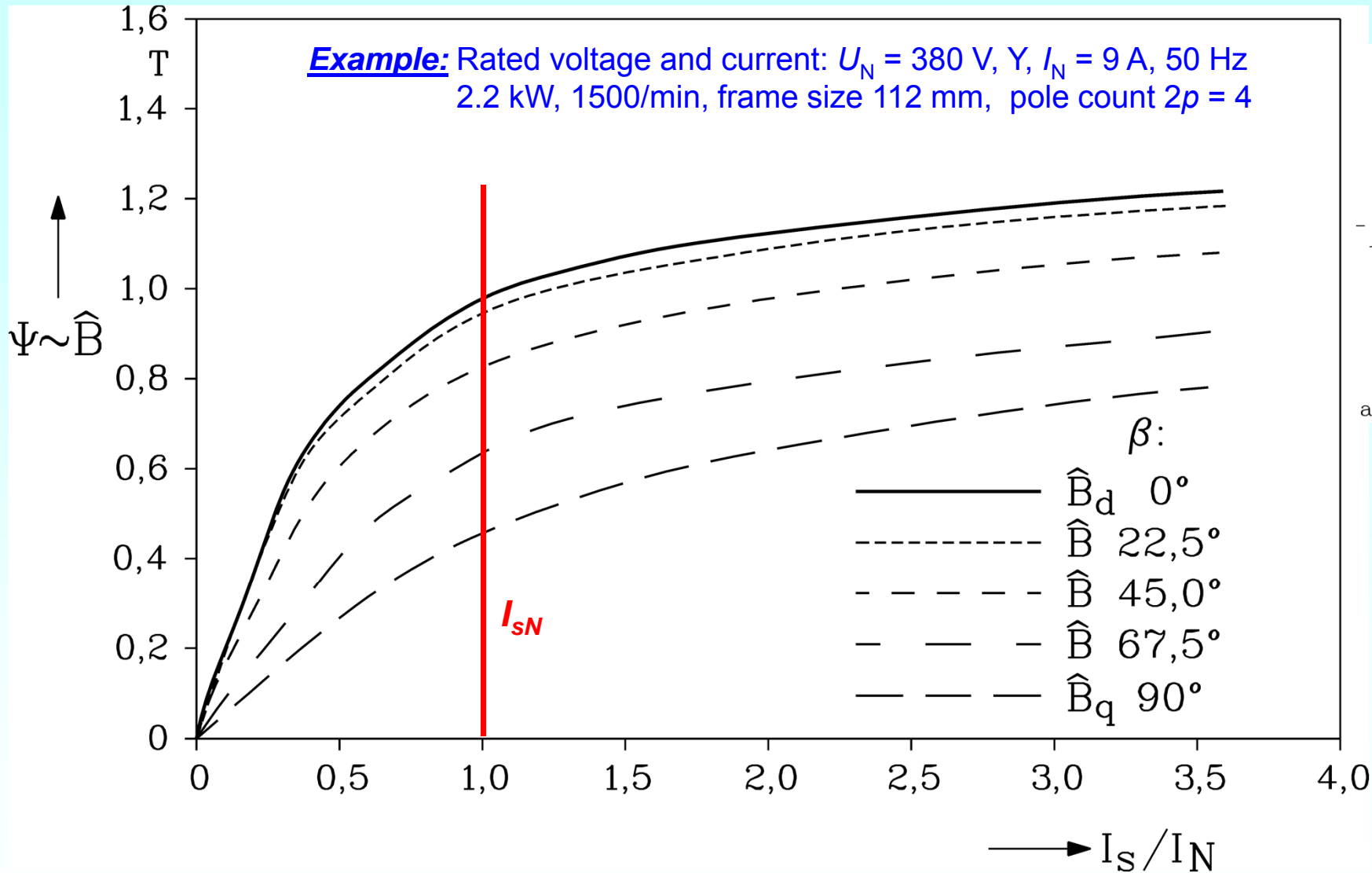
Rotor in  $d$ -position

$\beta = 0^\circ$





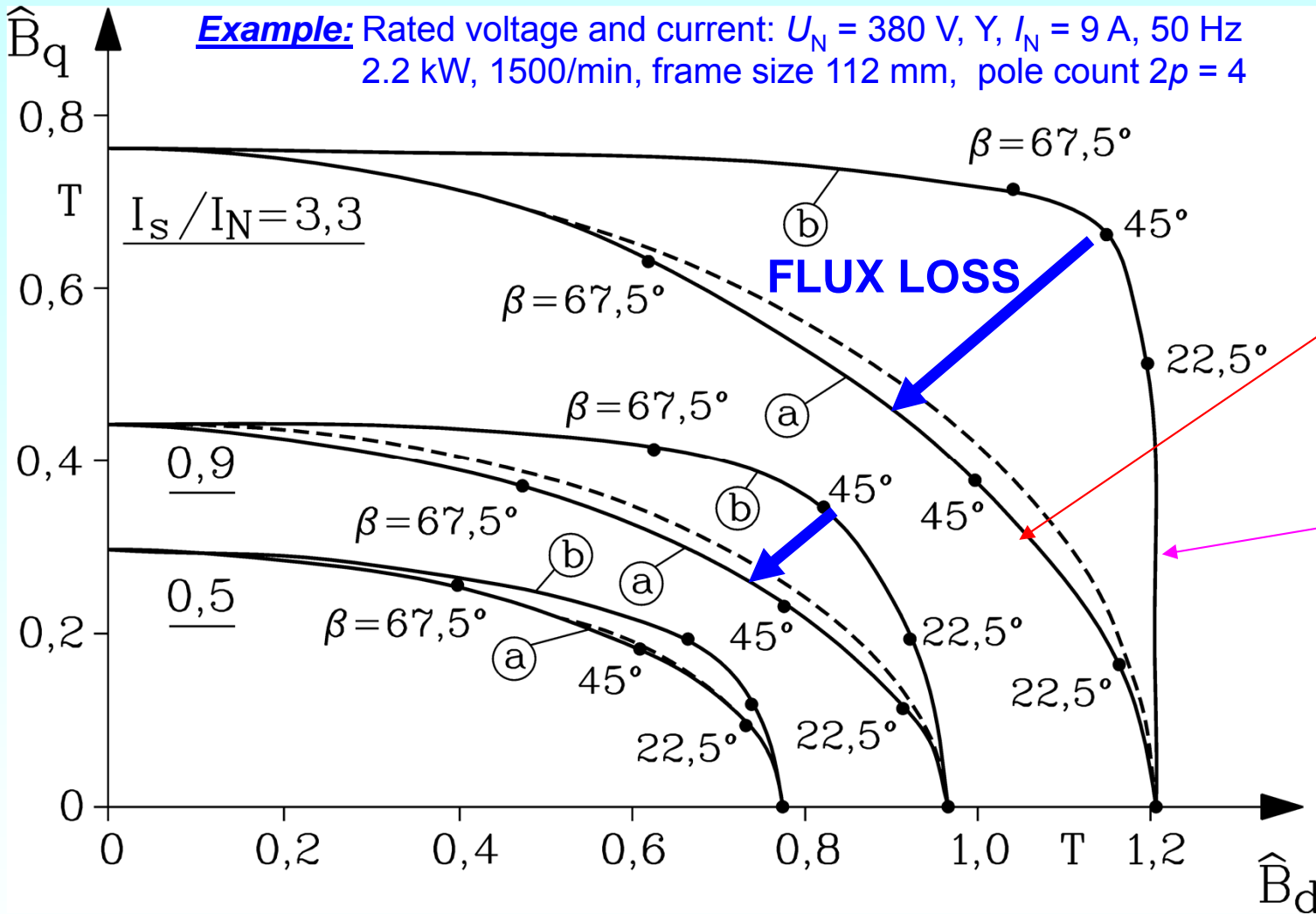
# Numerically calculated flux linkage characteristics



## Numerically calculated flux linkage characteristics at different current angle $\beta$

# Locus of air gap flux density amplitude

**Example:** Rated voltage and current:  $U_N = 380 \text{ V}$ ,  $Y$ ,  $I_N = 9 \text{ A}$ ,  $50 \text{ Hz}$   
 2.2 kW, 1500/min, frame size 112 mm, pole count  $2p = 4$

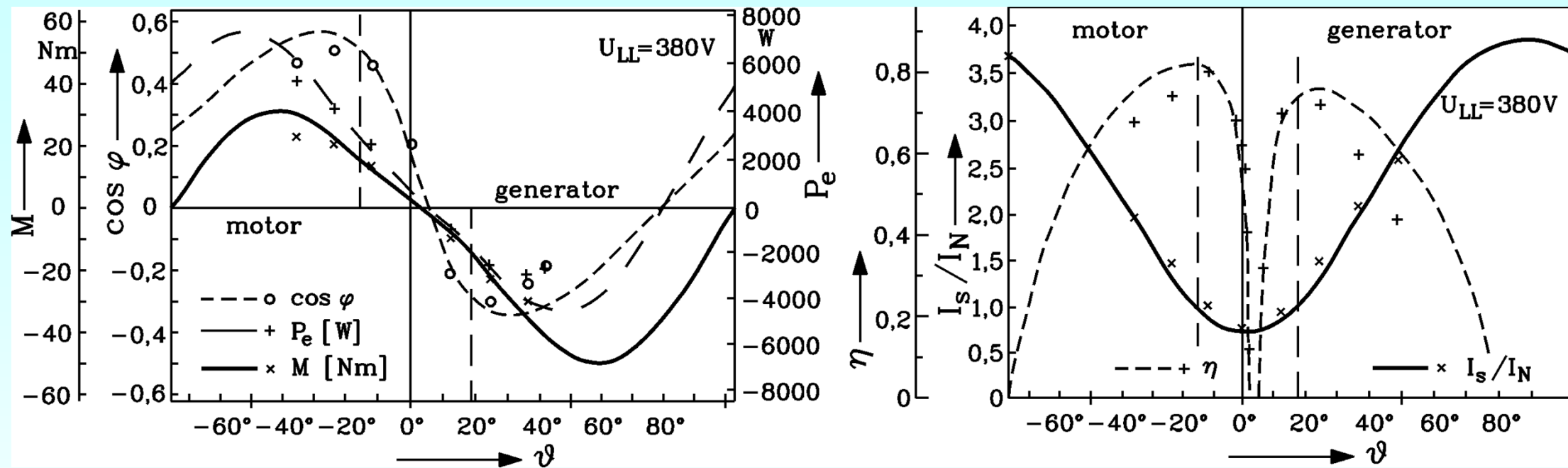


- Different stator current: 50%, 90%, 330% of rated current
  - Different current angles  $\beta$
  - Curves (a): flux linkage characteristic with "magnetic coupling"
  - Curves (b): No magnetic coupling between d- and q-axis considered
- Facit: Method b) yields wrong results except for d- and q-axis.**

(dotted line -----: approximation ellipses)



# Measured and calculated torque, power and current

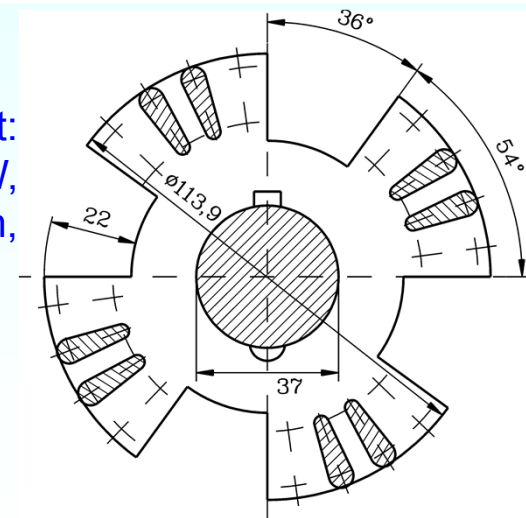


## Four pole synchronous reluctance machine:

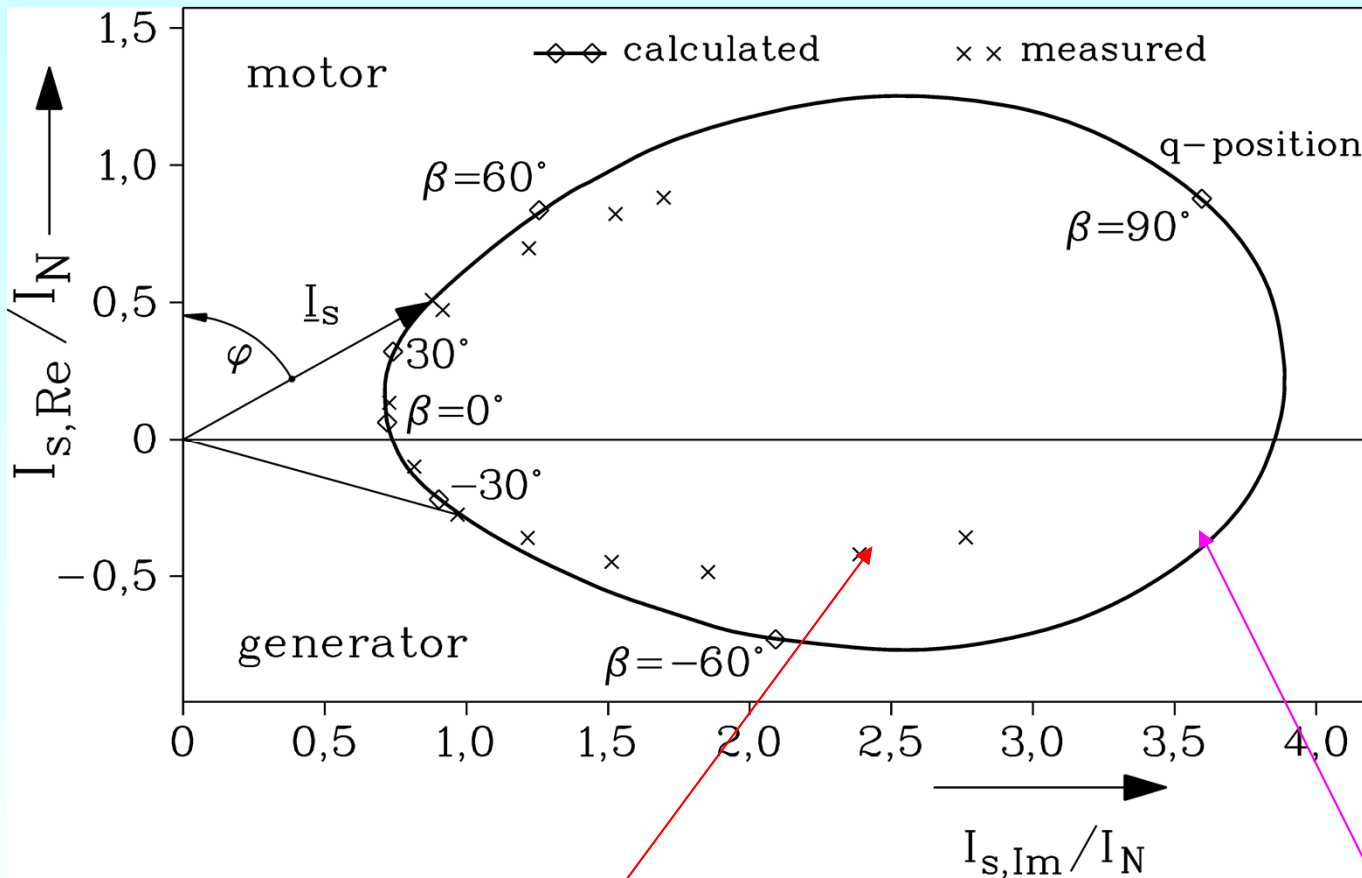
- (1) Measured values: points
- (2) Calculated: with consideration of "magnetic coupling" of  $d$ - and  $q$ -axis

**Example:** Rated voltage and current:  
 $U_N = 380$  V, Y,  $I_N = 9$  A, 50 Hz, 2.2 kW,  
 1500/min, frame size 112 mm,  
 pole count  $2p = 4$

Torque, electrical power, power factor, current, efficiency



# Current root locus of saturated machine



**Example:** Rated voltage and current:  
 $U_N = 380 \text{ V}$ , Y,  $I_N = 9 \text{ A}$ , 50 Hz, 2.2 kW,  
 1500/min, frame size 112 mm,  
 pole count  $2p = 4$

Comparison of **measured (points)** and **calculated locus** of stator phasor current; four pole synchronous reluctance machine

# Calculation of saturated reluctance machines

- *Saturation and two-dimensional flux density distribution has to be taken into account for reliable calculation results*
- *Numerical field calculation is needed for calculating reluctance machines.*
- *Due to magnetic “cross coupling of d- and q-axis” by common flux path in the stator yoke, which adds to total saturation, it is necessary to calculate the total flux linkage for each current phasor.*
- *Considering d- and q-flux independently (= neglecting “magnetic coupling”) is yielding too big flux for positions between d- and q-axis.*



# Comparison of power-to-weight ratio of motors

*Steady state torque per volume by 30% to 50% lower for synchronous reluctance machines, when compared with induction machines.*

380 V Y, 50 Hz	<i>Induction motor</i>	<i>Reluctance motor</i>
Output power $P_m$ / Rated current $I_N$	4 kW / 8.7 A	2.2 kW / 9.3 A
Power factor $\cos \varphi$	0.83	0.46
Efficiency $\eta$	84 %	78 %
Rotational speed $n_N$	1447 /min	1500 /min

$$P_m/S = \cos \varphi \eta$$

0.7

TOO high  
magnetizing  
current!

0.36

4-pole machines, identical stator and cooling

shaft height 112 mm, 36 stator slots

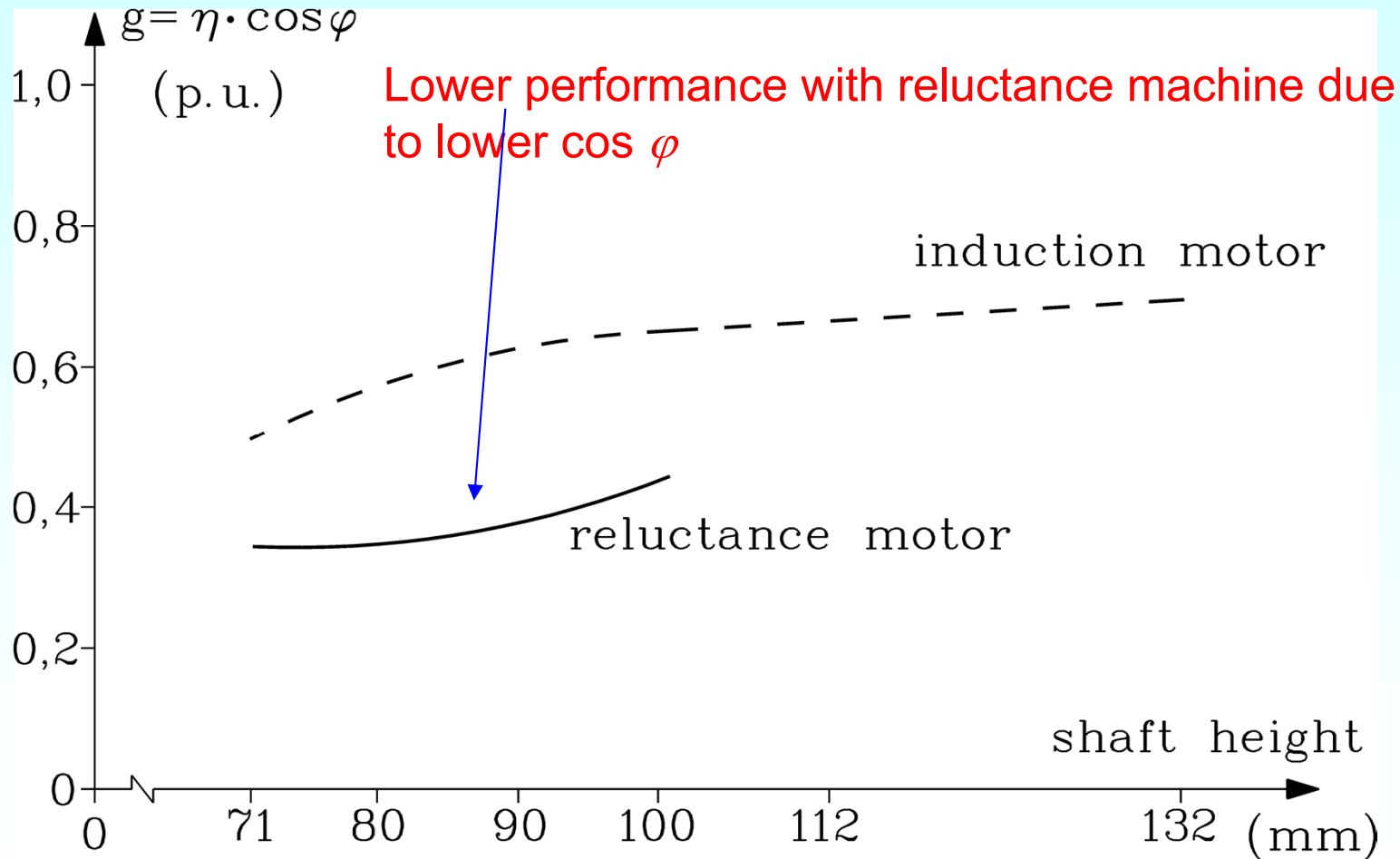
totally enclosed, fan cooled (TEFC), 380 V Y, 9 A, 50 Hz

For increased power output special rotor design (expensive) is necessary !

# Product of rated efficiency and power factor $g$

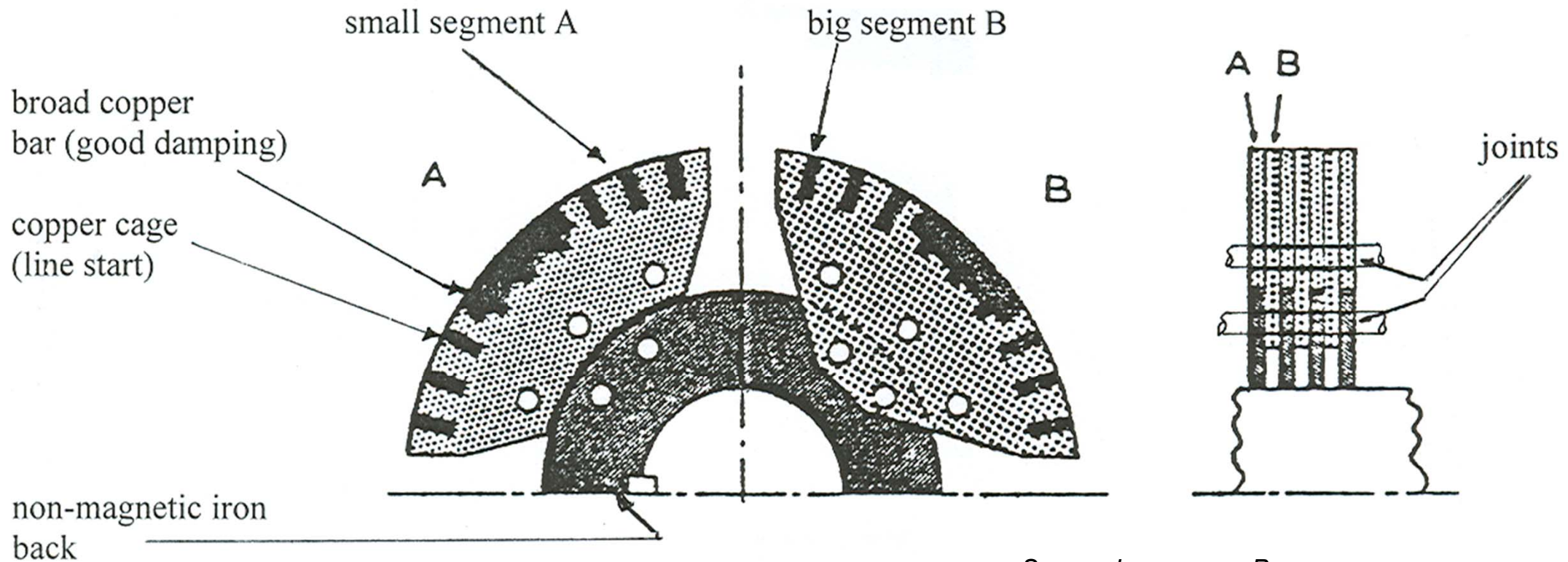
Comparison of 4-pole machines:

Line-operated synchronous reluctance machine vs. induction motor





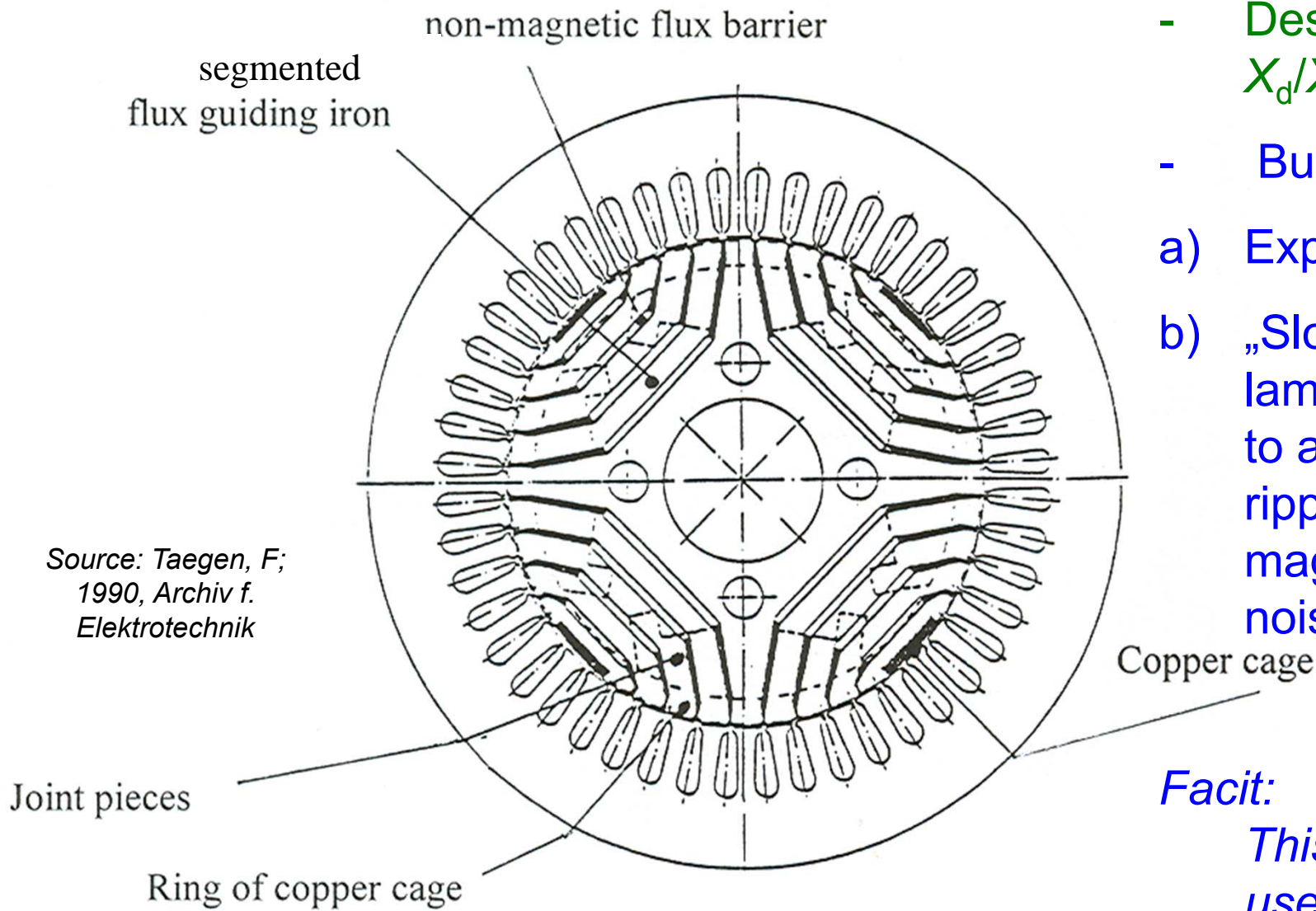
# Special segmented sheet rotor design for increased ratio $X_d/X_q$



Source: Lawrenson, P;  
Gupta, S, IEE, 1967

- $X_d/X_q$  can be increased up to 10 !
- Rotor construction is very expensive, so it is not used in industry !

# Segmented reluctance rotor for increased $X_d/X_q$



Source: Taegen, F;  
1990, Archiv f.  
Elektrotechnik

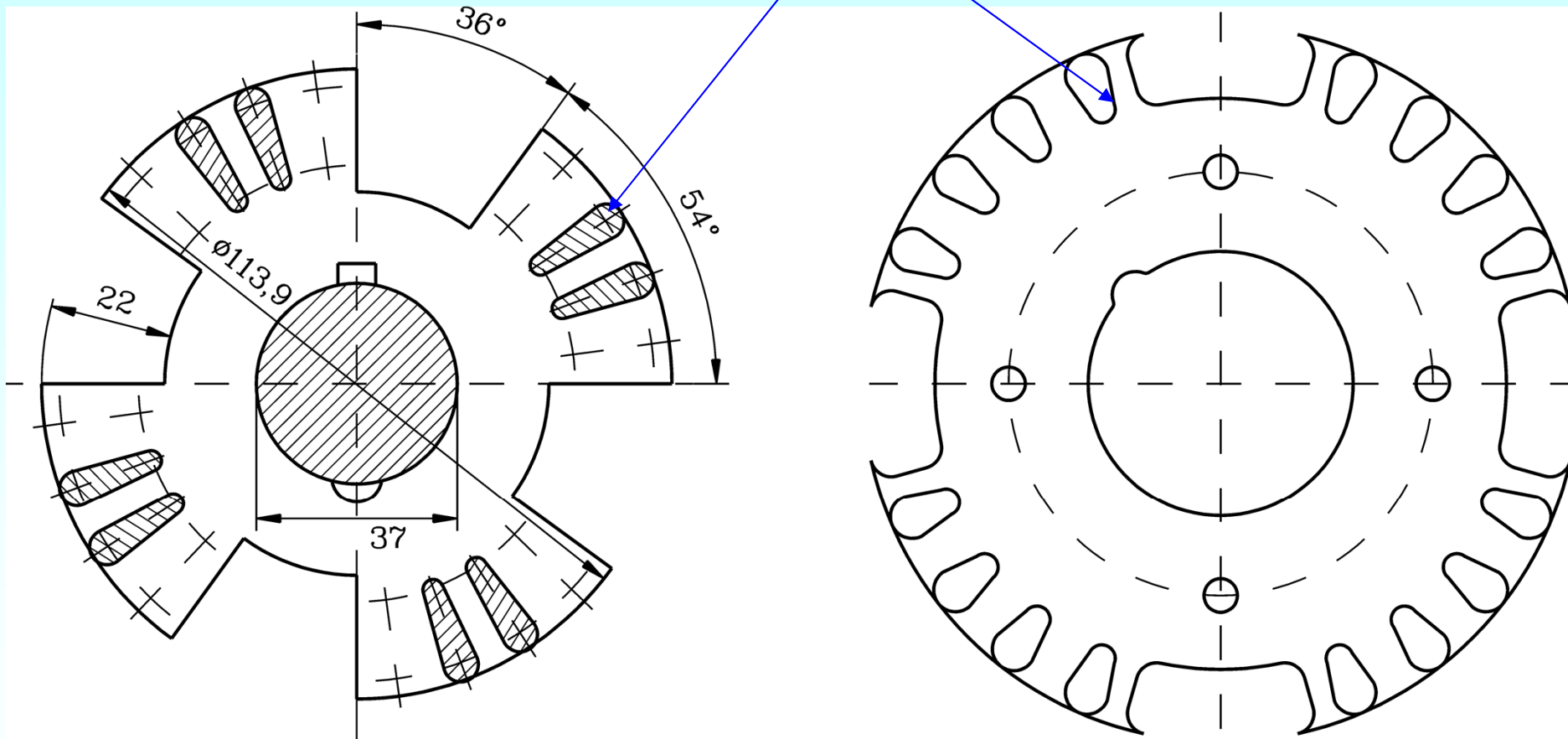
- Design gives big ratio  $X_d/X_q$  of about 10 !
- But:
  - a) Expensive rotor design
  - b) „Slotting“ due to axially laminated rotor gives rise to air gap flux density ripple, which causes magnetically excited noise.

*Facit:*

*This rotor design is not used in industry.*

# Starting cage for synchronous reluctance machines

Die-cast **aluminum cage** for asynchronous starting

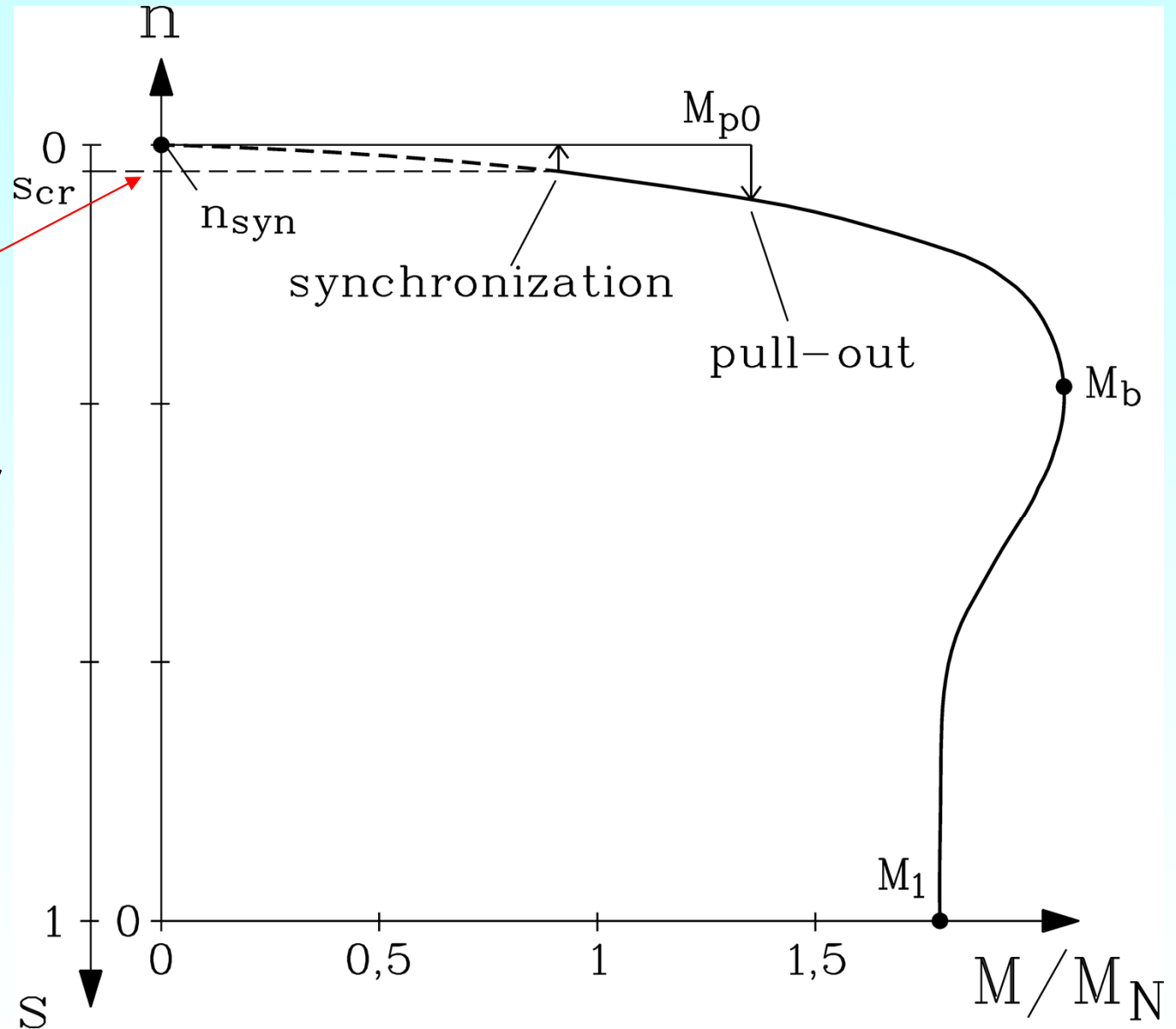


Source: A. Schmidt, TU  
Wien, 1988

Source: Siemens AG.  
Germany

# Asynchronous starting and synchronization (pull-in)

- Minimum slip (below critical slip  $s_{cr}$ ) necessary for pull-in
- Asynchronous torque at this slip lower than synchronous pull-out torque
- **Critical slip** depends on rotor cage data and rotor inertia !

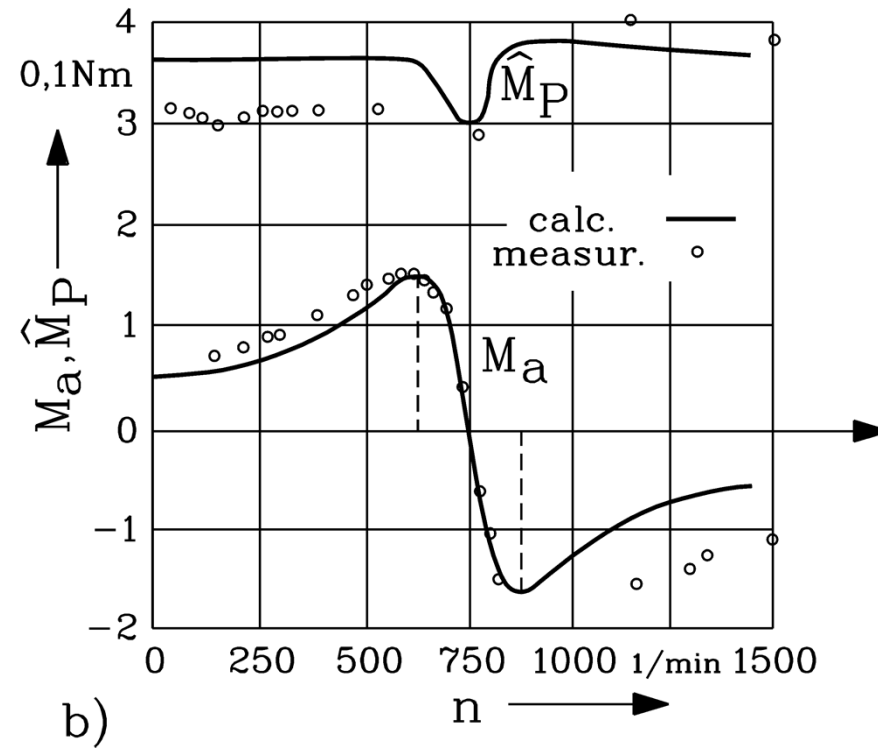
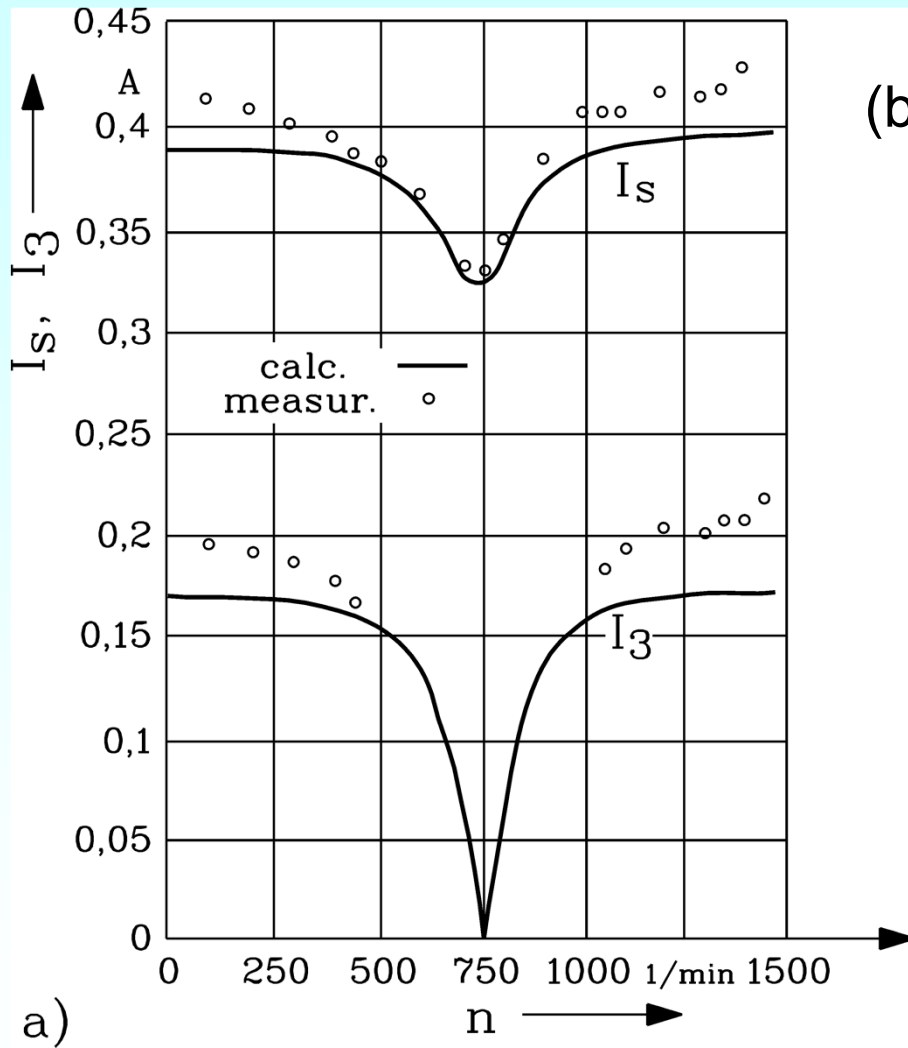


Source: Siemens AG.  
Germany



# Asynchronous starting of reluctance machines

- (a) Calculated and measured (dots) stator and additional stator current  $I_3$ ,
- (b) Asynchronous reluctance torque  $M_a$  and pulsating torque amplitude  $\hat{M}_P$



Source:  
Bausch,  
Jordan et al,  
ETZ-A

# Asynchronous reluctance torque $M_a$ and pulsating torque $M_p$

- Rotor reluctance modulates stator air gap field, resulting

$$B_{\delta}(\gamma, t) = \mu_0 V_s(\gamma, t) / \delta(\gamma, t) = \mu_0 V_s \cos(\gamma - \omega_s t) \cdot \left[ \frac{1}{\delta_0} + \frac{1}{\delta_1} \cdot \cos(2\gamma - 2(1-s)\omega_s t) \right]$$

- stator fundamental with average air gap:  $B_{s,1} = (\mu_0 V_s / \delta_0) \cos(\gamma - \omega_s t)$
- additional field with different frequency:  $B_{s,3} = (\mu_0 V_s / 2\delta_1) \cos(\gamma - (1-2s)\omega_s t)$

Additional field induces in the stator windings a voltage system  $U_3$  with frequency

$$f_3 = (1 - 2s) f_s$$

which causes an additional (small) stator current  $I_3$ .

a) Constant part of **asynchronous reluctance torque**:  $M_a \sim I_s I_3$

b) **Pulsating torque amplitude**:  $M_p \sim I_s I_3, I_s^2, I_3^2$  with frequency  $|f_s - f_3| = 2s f_s$



# GOERGES phenomenon of reluctance machines

At half synchronous speed  $n = n_{syn} / 2 \Leftrightarrow s = 0.5$

$f_3$  is zero, so in that point  $I_3 = 0$ .

Asynchronous reluctance torque  $M_a$  vanishes

Pulsating torque has a minimum, now depending only on  $I_s^2$

(**Goerges-phenomenon**)

a) The current  $i_3(t) = \hat{I}_3 \cdot \sin((1-2s)\omega_s t)$  changes sign at  $s = 0.5$ , therefore the real power flow of this current is also changing direction,

(1) being **motor** at  $n < n_{syn}/2$

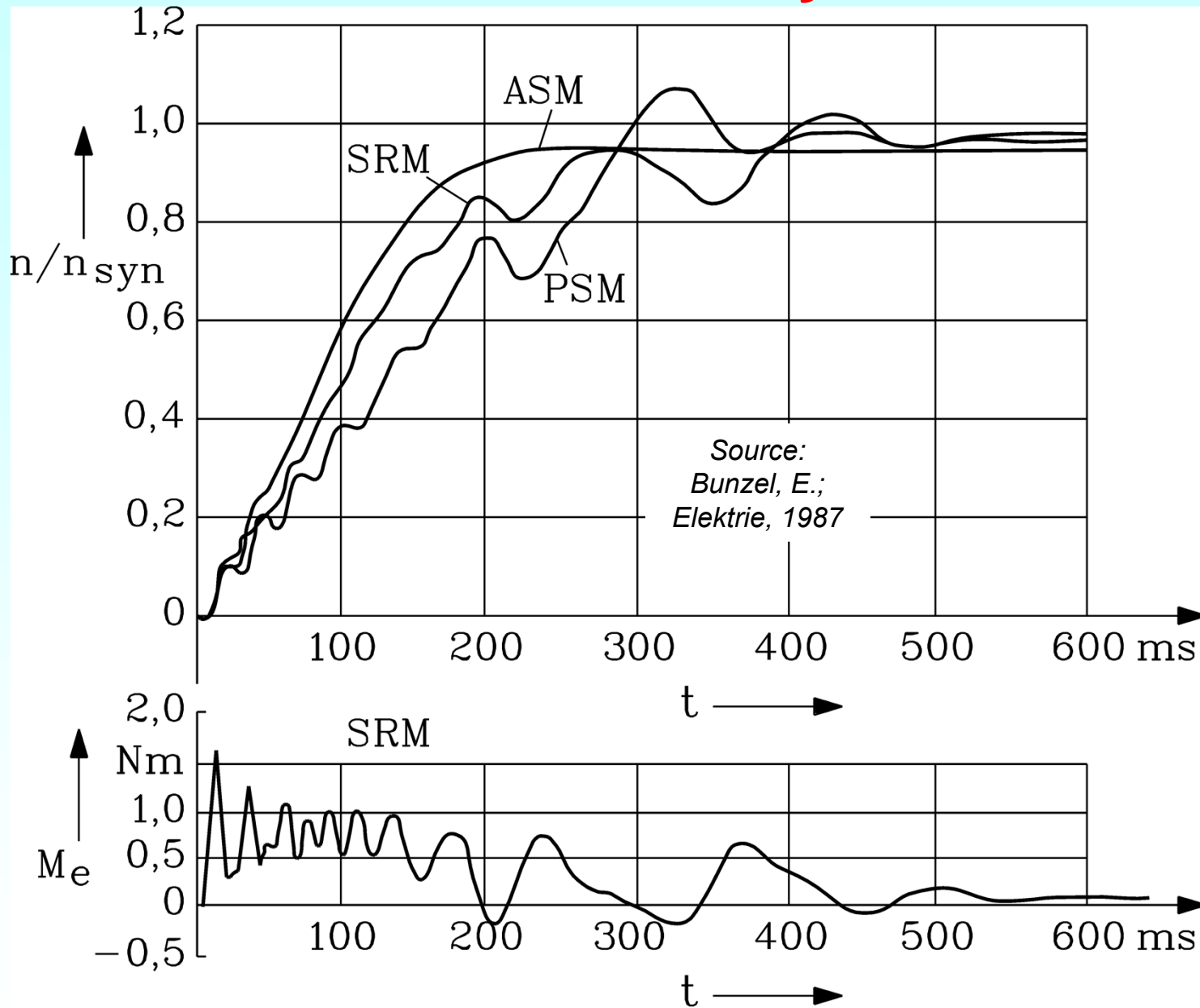
(2) **generator** at  $n > n_{syn}/2$ .

(b) Therefore the asynchronous reluctance torque is a

(1) **driving** (positive) torque for  $n < n_{syn}/2$  and

(2) a **braking** (negative) torque for  $n > n_{syn}/2$ .

# Calculated asynchronous starting



Comparison of

- induction machines (ASM),

- Synchronous reluctance machine (SRM)

- Permanent magnet synchronous machines with rotor cage (PSM)

- Pulsating torque with decreasing frequency

$$|f_s - f_3| = 2sf_s$$

clearly visible.

# Synchronization after asynchronous start-up

- At synchronous speed the slip is zero: The asynchronous torque of the cage is zero.
- The speed of stator fundamental field wave and of the rotor with its variable reluctance is identical, so the field modulation effect vanishes. Hence the asynchronous reluctance torque is zero.
- The frequency of the stator current system  $I_3$  is:  $f_3 = (1 - 2s)f_s = f_s$
- Hence current  $I_s$  and  $I_3$  unite as the total stator current  $I_s$  at synchronous speed.
- **The pulsating torque becomes the constant reluctance torque:**

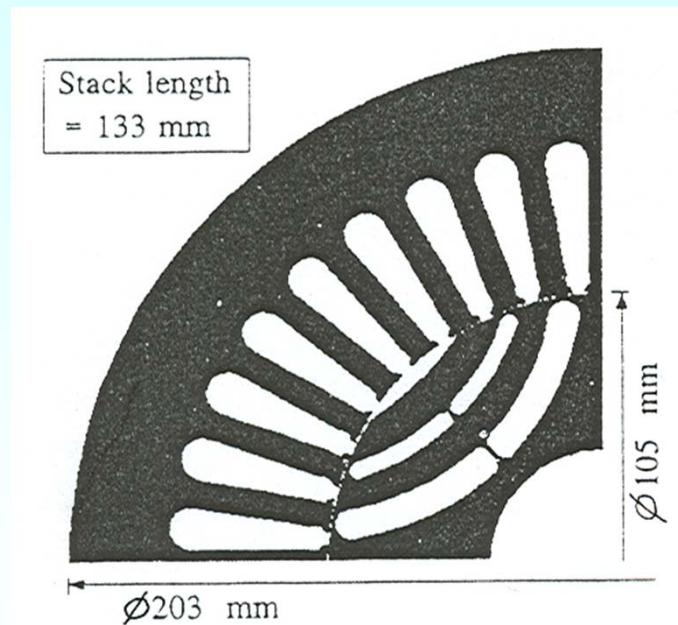
$$|f_s - f_3| = 2sf_s = 0 \quad M_P \sim I_s I_3, I_s^2, I_3^2 \sim U_s^2 = M_e$$

- At  $s \ll 1$  the frequency  $2s \cdot f_s$  corresponds with a very slowly increasing load angle  $\mathcal{G}(t)$ :  $\hat{M}_P \cdot \sin(2 \cdot (2\pi \cdot sf_s \cdot t + \mathcal{G})) \Rightarrow \hat{M}_e \cdot \sin(2\mathcal{G})$

$$M_e = -\frac{p \cdot m}{\omega_s} \cdot \frac{U_s^2}{2} \cdot \left( \frac{1}{X_q} - \frac{1}{X_d} \right) \cdot \sin(2\mathcal{G})$$

## 2. Reluctance machines

### 2.2.2 Inverter-operated synchronous reluctance machines



Source: M. Kamper,  
WCRR Conf, 1997

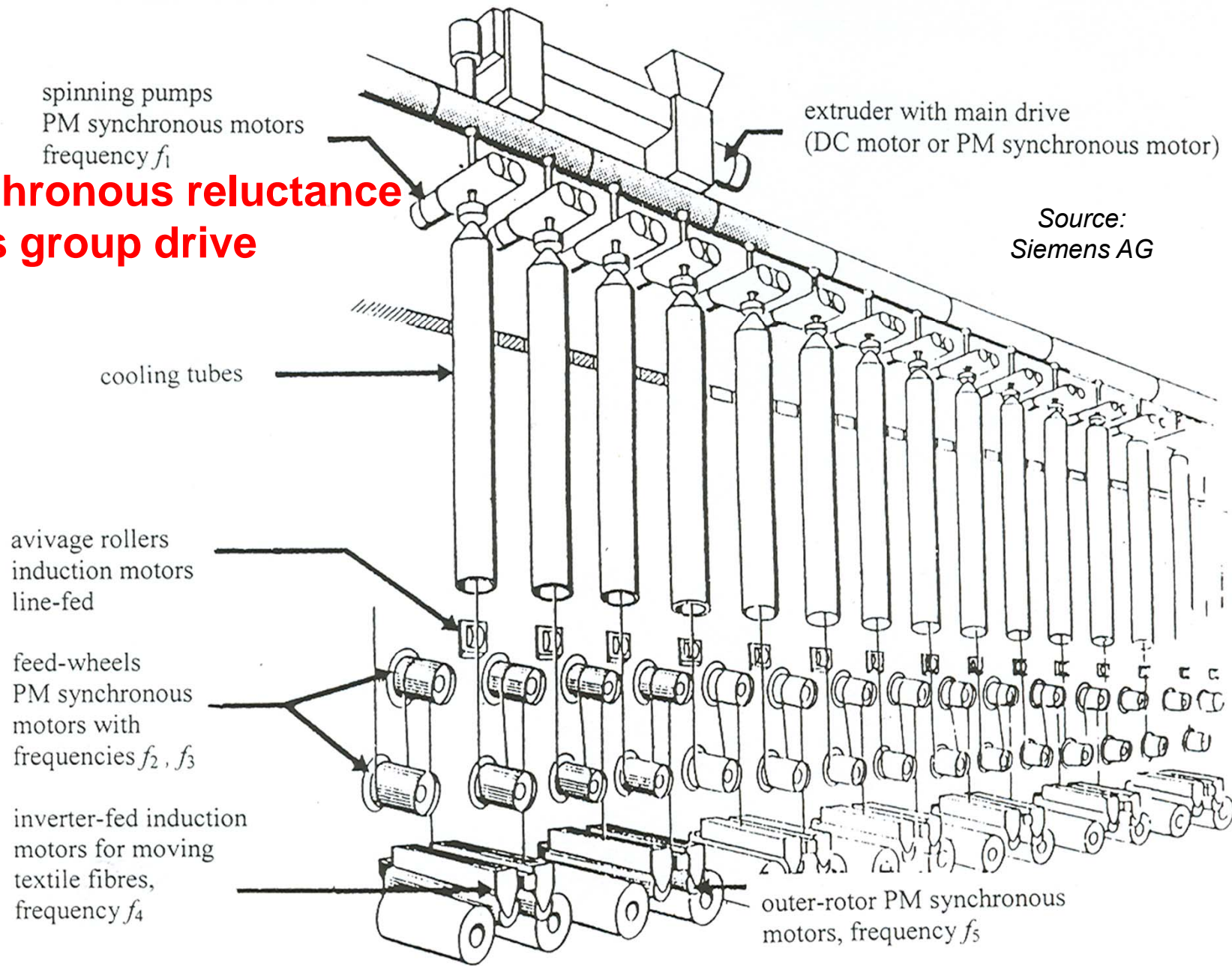
# Synchronous reluctance machines for group drives

- **Application:** Fabrication of textile fibers
- **Group drive:** One big converter feeds ca. 100 synchronous reluctance machines in parallel
- All motors rotate synchronously **without any speed control**
- **Feed forward  $U/f$ -converter operation** with fixed voltage and frequency
- If one drive fails, it is stopped, while the others keep operating. After fault-clearing the stopped drive **starts asynchronously** via its starting cage at the group converter with fixed stator voltage and frequency.



## Application of synchronous reluctance machines as group drive

- Fabrication of textile fibers
- One big thread, coming from extruder, is separated into ca. 100 parallel thin threads
- Parallel and SYNCHRONOUS up-winding of threads is done by cheap reluctance motors or PM synchronous motors
- Motors must start separately, hence asynchronous start up

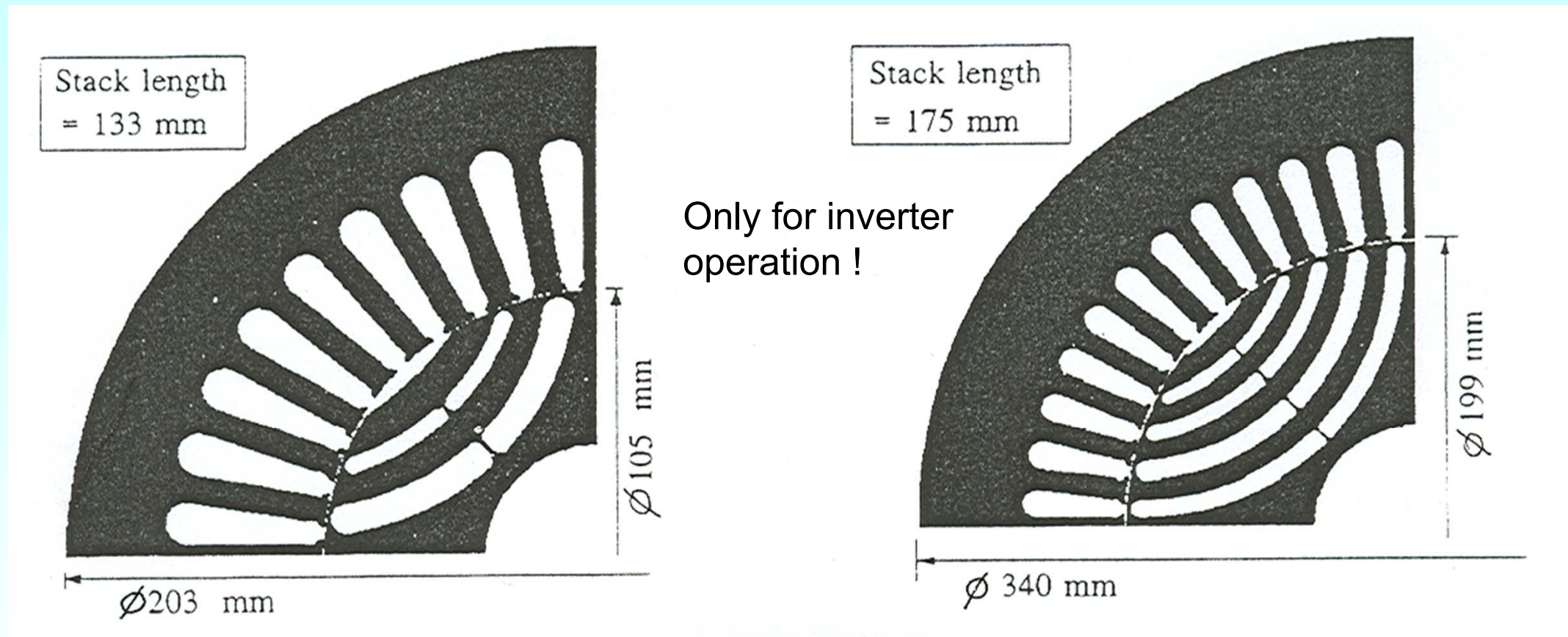




# Variable speed synchronous reluctance drives without starting cage

- Special rotor design for big ratio  $X_d/X_q = \text{ca. } 8 \dots 10$  allows motor utilization similar to cage induction machines
- These motors are operated as variable speed drives with IGBT voltage source inverters and rotor position control. So no group drive operation possible.
- Motors have nearly no rotor losses, so efficiency is higher than with comparable inverter-operated cage induction machines
- Synchronous motor operation without speed control possible
- Due to the big ratio  $X_d/X_q$  the power factor is increased up to 0.7 ... 0.8
- Field-oriented control ( $I_d, I_q$ ) is possible, so high dynamic performance is inherently given.

# Flux barrier rotor design for increased ratio $X_d/X_q$ without cage

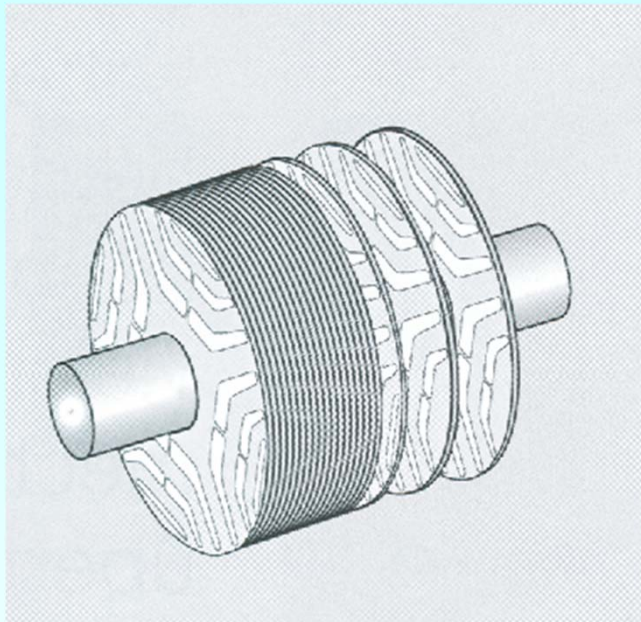


-  $X_d/X_q$  can be increased from about 5 to 8 ... 10

Source: M. Kamper,  
WCRR Conf, 1997

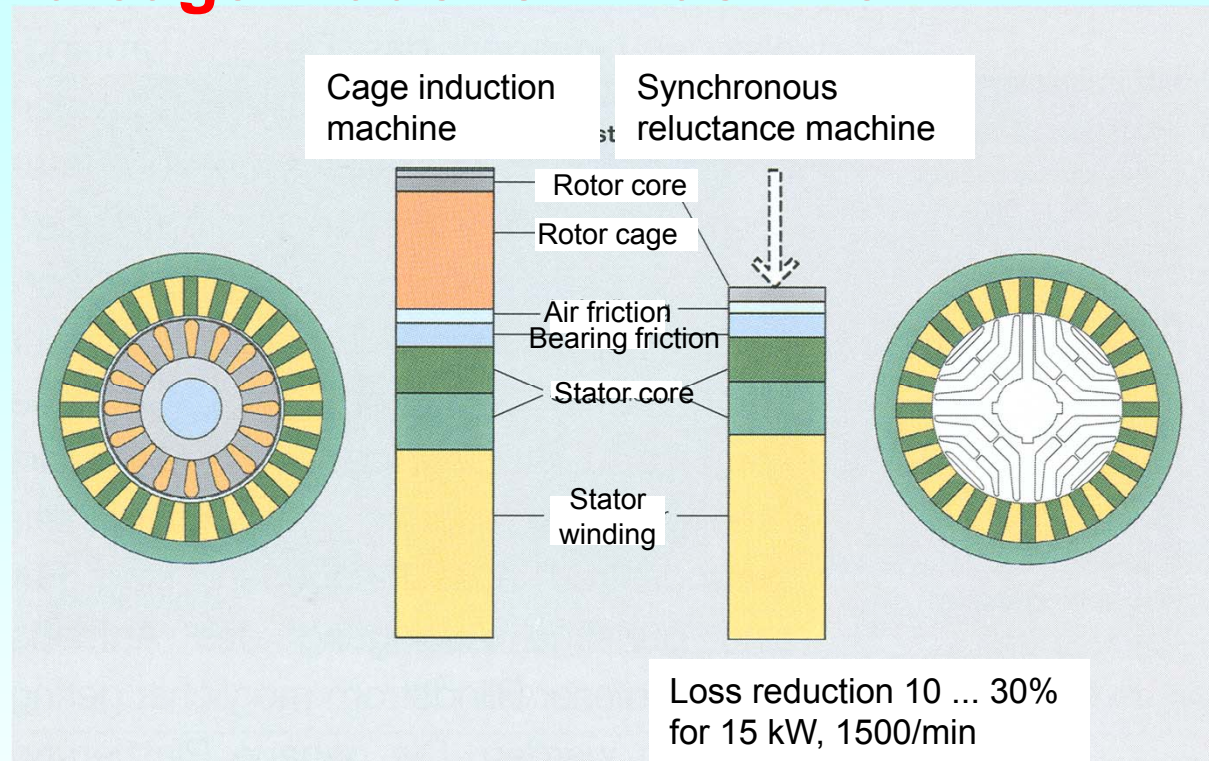
- Power factor increased up to 0.7 ... 0.8, thus nearly reaching the value of induction machines. An efficiency of 0.85 ... 0.9 is possible.

# Comparison of losses for a 4-pole sync. reluctance machine with a cage induction machine



4-pole laminated reluctance rotor with flux barriers

Source: Lendenmann H,  
ABB review 2011



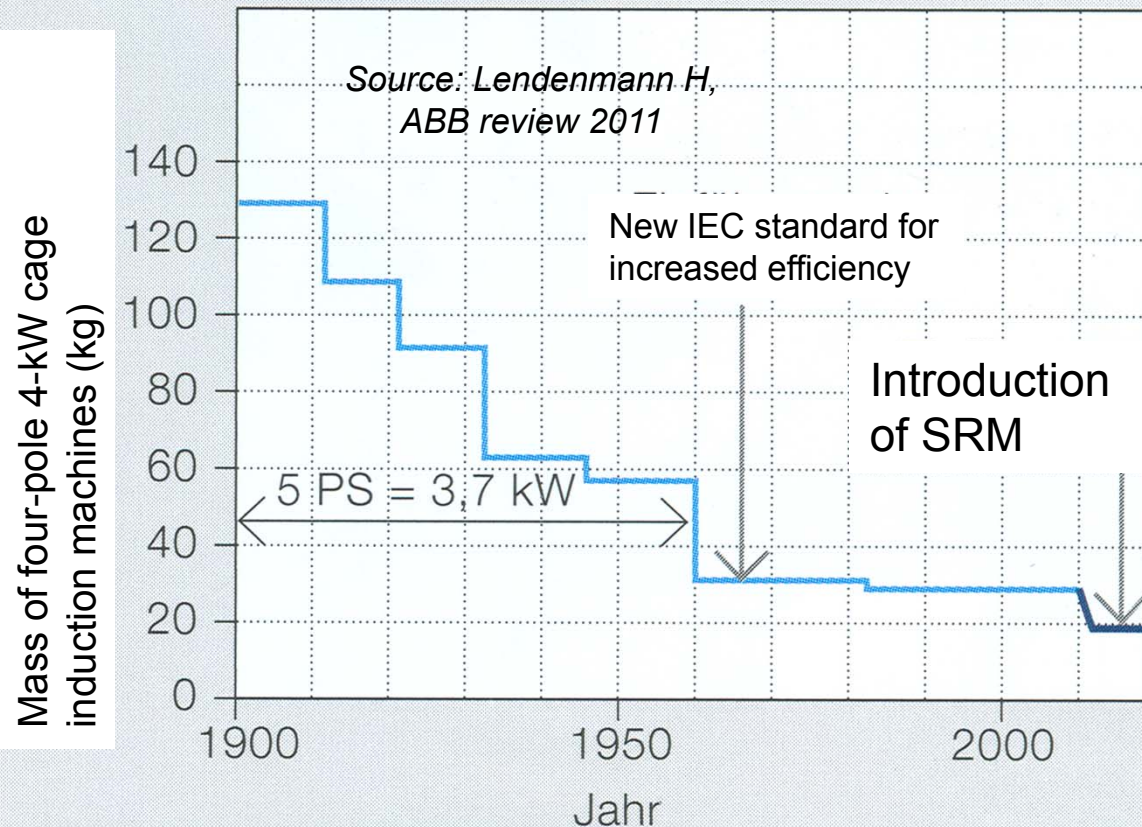
4-pole cage induction motor

4-pole synchronous reluctance motor

- Comparison at: 15 kW, 1500/min, 50 Hz: Due to the missing rotor  $I^2R$  losses the nominal efficiency of the synchronous reluctance machine is higher than for the cage induction machine, as the total losses are reduced by 10% ... 30%.



# Comparison of mass and output power of 4-pole synchronous reluctance machine to cage induction machine



Frame size	Cage induction machine	Syn. Rel. machine	Output power
100	3,3 kW $\eta=83\%$	4,3 kW $\eta=90\%$	+30–45%
160	22 kW	29 kW	+32%
280	90 kW	110 kW	+22%

Comparison of output power

Motor mass reduction of induction machines due to increased motor utilization

Further mass reduction due to replacement by inverter-fed synchronous reluctance machines (SRM)

Increase of nominal power due to reduced losses within a given frame size of 20% ... 30% with SRM

Efficiency increase with SRM



# Comparison of nominal efficiency of inverter-fed 4-pole sync. reluctance machine to cage induction machines

